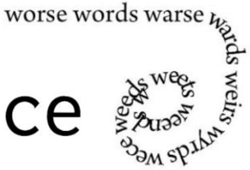
7. Language as a Sequence

Mariana Romanyshyn, *Grammarly, Inc.*

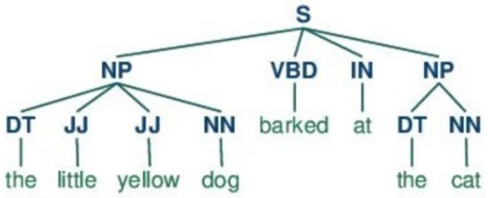
NLP Viewpoints

* Bag-of-words



* Sequence

* Tree



* Graph

Contents

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1. Sequence Labeling

Bag of words vs. sequence

Trump beat Clinton in the election.

= or ≠

Clinton beat Trump in the election.

Sequence Labeling

Part-of-speech tagging:

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

Borrowed from Marek Rei: https://goo.gl/iixm6D

Sequence Labeling

Named-entity recognition:

```
PER _      _   _      _  ORG  ORG   _  TIME _
Jim bought 300 shares of Acme Corp. in 2006 .
```

Borrowed from Marek Rei: https://goo.gl/iixm6D

Sequence Labeling

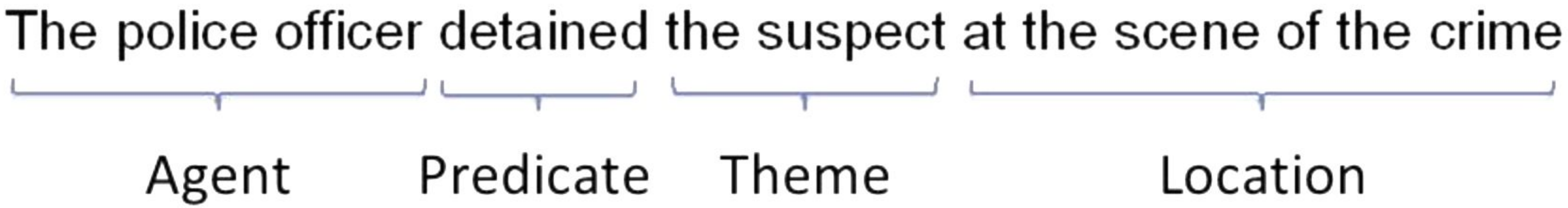
Error detection:

+	+	+	x	+	+	+	+	+	x	+
I	like	to	playing	the	guitar	and	sing	very	louder	.

Borrowed from Marek Rei: https://goo.gl/iixm6D

Sequence Labeling

Semantic role labeling:



Sequence Labeling

Genome analysis:

intron exon intron exon intron

AGCTAACGTTCGATACGGATTACAGCCT

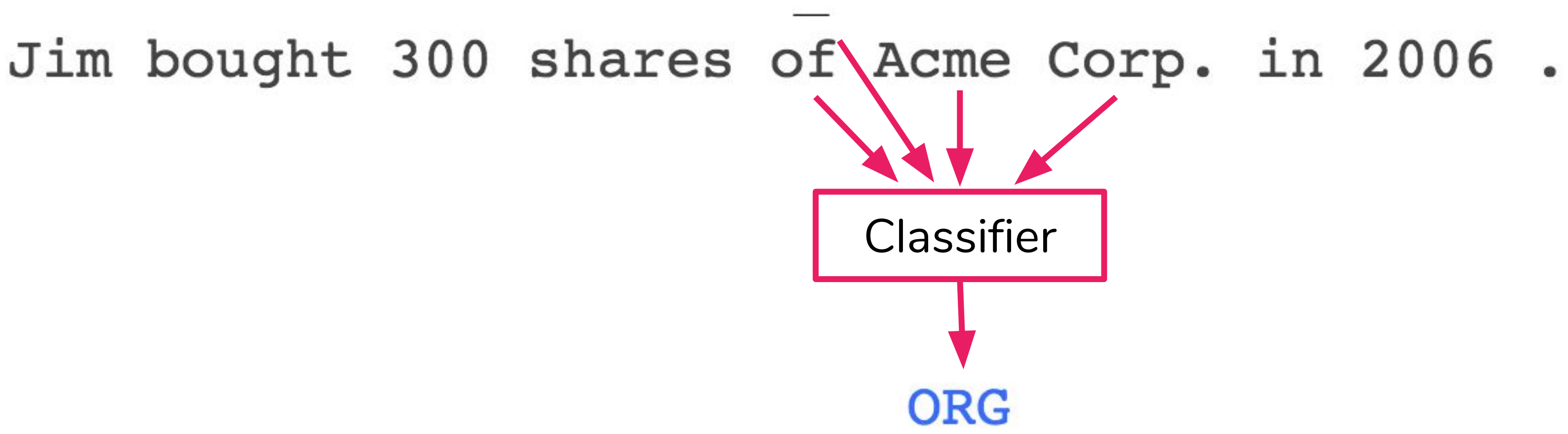
Sequence Labeling

There's more:

- Dialogue act tagging
- Pitch accent detection
- Word segmentation
- Sentence segmentation
- Chunking

Sequence Labeling

Sequence labeling is essentially a ***classification*** of each incoming element taking into account left and right context.



Sequence Labeling

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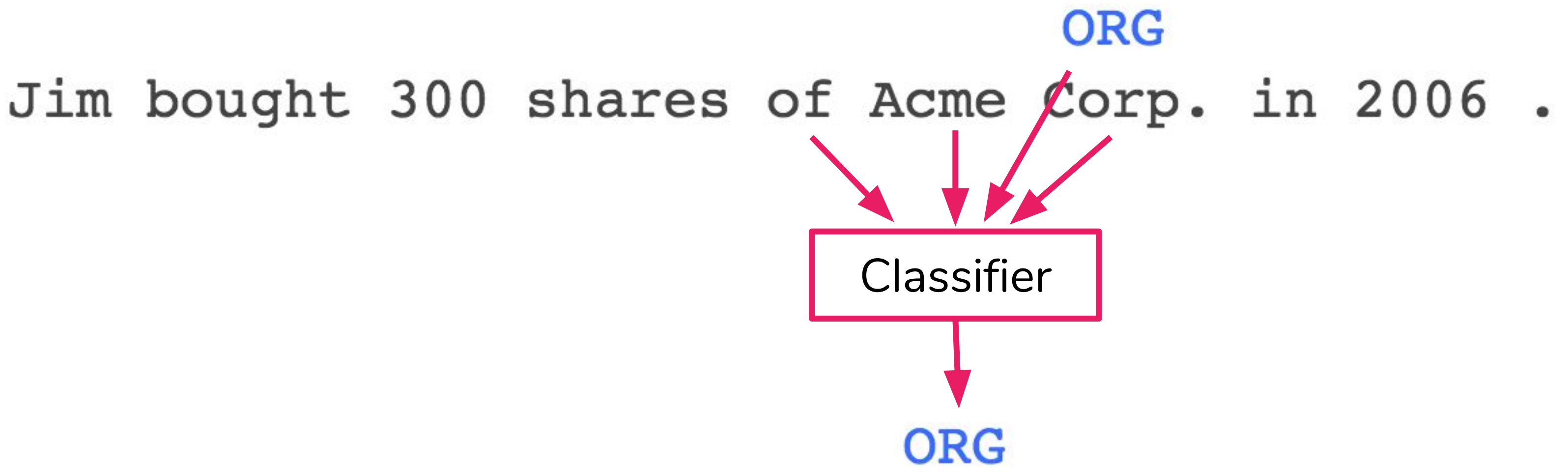


2. Hidden Markov Model

Hidden Markov Model

HMM - a ***generative*** *probabilistic sequence model used for:*

- *speech recognition*
- *segmentation (words, sentences, genomes)*
- *NER*
- *POS tagging*

HMM for POS tagging: notation

V - vocabulary

T - POS tags

x - sentence (observation)

y - tag sequences (state)

S - all sentence/tag-sequence pairs $\{x_1 \ldots x_n, y_1 \ldots y_n\}$

- $n > 0$
- $x_i \in V$
- $y_i \in T$

HMM for POS tagging

S - all sentence/tag-sequence pairs $\{x_1 \dots x_n, y_1 \dots y_n\}$

x:	Chewie	,	we	're	home	.
y:	NNP	,	PRP	VBP	RB	.
	NN	,	PRP	VBP	RB	.
	NNP	,	PRP	VBP	NN	.
	NN	,	PRP	VBP	NN	.
	…					

Aim: find $\{x_1 \dots x_n, y_1 \dots y_n\}$ with the highest probability.

Hidden Markov Model: assumptions

- Markov Assumption: "*The* ***future*** *is independent of the* ***past*** *given the* ***present***."
  - Trigram HMM: each state depends only on the previous two states in the sequence

- Independence assumption:
  - the state of $\mathbf{x}_i$ depends only on the value of $\mathbf{x}_i$, independent of the previous observations and states

Hidden Markov Model: assumptions

S - all sentence/tag-sequence pairs $\{x_1 \ldots x_n, y_1 \ldots y_n\}$

x:	Chewie	,	we	're	home	.
y:	NNP	,	PRP	VBP	RB	.
	NN	,	PRP	VBP	RB	.
	NNP	,	PRP	VBP	NN	.
	NN	,	PRP	VBP	NN	.
	...					

Trigram Hidden Markov Model: parameters

$$p(x_1 \ldots x_n, y_1 \ldots y_{n+1}) = \prod_{i=1}^{n+1} q(y_i | y_{i-2}, y_{i-1}) \prod_{i=1}^{n} e(x_i | y_i)$$

- q(s|u, v) - the probability of tag s after the tags (u, v)
  - s, u, v ∈ T

- e(x|s) - the probability of observation x paired with state s
  - x ∈ V, s ∈ T

Trigram Hidden Markov Model: parameters

- q(s|u, v) - the probability of tag s after the tags (u, v)

$$q(s|u, v) = \frac{c(u, v, s)}{c(u, v)}$$

- e(x|s) - the probability of observation x paired with state s

$$e(x|s) = \frac{c(s \leadsto x)}{c(s)}$$

For example

x:	Chewie	,	we	're	home	.
y:	NNP	,	PRP	VBP	RB	.

p(x, y) = ?

For example

x:	Chewie	,	we	're	home	.
y:	NNP	,	PRP	VBP	RB	.

p(x, y) = c(NNP,|,|,PRP) / c(NNP,|,|) * c(|,|,PRP, VBP) / c(|,|,PRP) *
c(PRP, VBP,RB) / c(PRP,VBP) * c(VBP,RB,|.|) / c(VBP,RB) *
c(NNP->Chewie) / c(NNP) * c(|,|->,) / c(|,|) *
c(PRP->we) / c(PRP) * c(VBP->’re) / c(VBP) *
c(RB->home) / c(RB) * c(|.|->.) / c(|.|)

One thing missing

x: Chewie , we 're home .

y: <S> <S> NNP , PRP VBP RB . </S>

p(x, y) = c(NNP,|,|,PRP) / c(NNP,|,|) * c(|,|,PRP, VBP) / c(|,|,PRP) *
c(PRP, VBP,RB) / c(PRP,VBP) * c(VBP,RB,|.|) / c(VBP,RB) *
c(<S>,<S>,NNP) / c(<S>,<S>) * c(<S>,NNP,|,|) / c(<S>,NNP) *
c(RB,|.|,</S>) / c(RB,|.|)* c(NNP->Chewie) / c(NNP) * c(|,|->,) / c(|,|) *
c(PRP->we) / c(PRP) * c(VBP->'re) / c(VBP) *
c(RB->home) / c(RB) * c(|.|->.) / c(|.|)

HMM: problem 1

Enumerating all possible tag sequences is not feasible — $\boldsymbol{T^n}$.

44 tags ** 6-token sentence = 7,256,313,856 tag sequences

Ideas:

- use dynamic programming (the Viterbi algorithm) - $\boldsymbol{n*T^3}$
- limit the number of candidates with a dictionary - $\boldsymbol{n*8^3}$

HMM: problem 2

Zero probabilities can occur because of OOV or rare words.

Idea: use smoothing!

- ***add-1:*** pretend you saw each word (or each new word) one more time
- ***Good-Turing:*** reallocate the probability of ngrams that occur *r+1* times to the ngrams that occur *r* times
- ***Kneser-Ney:*** when the bigram count is near 0, rely on unigram

HMM: problem 3

Limited features taken into account:

- ***p(tag|word)*** could be informative
- incorporating lemmas, grammatical properties, spelling properties, etc. is hard

3. Feature Encoding

Encode part of speech: one-hot encoding

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

"losses"/NNS:

[0,	1,	0,	0,	0,	0,	0,	0,	...]
DT	NNS	VB	VBD	VBN	VBP	JJ	VBZ	

Encode part of speech: key-value

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

“losses”/NNS:

{“tag”: “NNS”}

Encode neighbors: feature template

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

“losses”/NNS:
{“word-2”: “pound”,
 “word-1”: “extended”,
 “word+1”: “against”,
 “word+2”: “both”}

“losses”/NNS:
{“tag-2”: “NN”,
 “tag-1”: “VBD”,
 “tag+1”: “IN”,
 “tag+2”: “DT”}

Encode neighbors: feature template

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

[1, 1, 0, ...]

word-2=pound word-1=extended word+1=hello

Encode neighbors: feature template

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

“losses”/NNS:

{“wt-2”: “pound_NN”,
“wt-1”: “extended_VBD”,
“wt+1”: “against_IN”,
“wt+2”: “both_DT”}

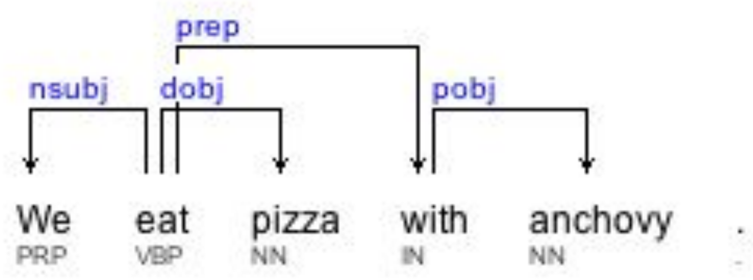
Encode context (ngrams)

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

“losses”/NNS:

{“left-bigram”: “pound extended”,
“right-bigram”: “against both”,
“context”: “extended losses against both”}

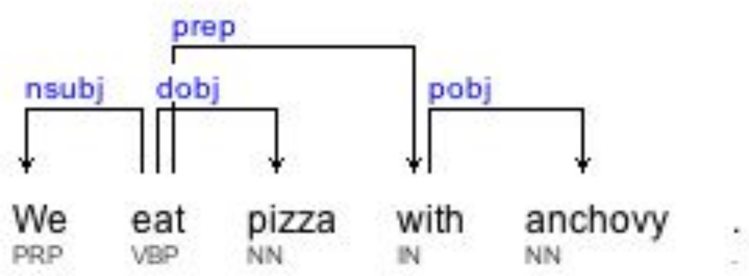
Encode dependencies



“eat”/VBP:

[1,	*0,*	*0,*	*1,*	*0,*	*1,*	*0,*	*0,*	*…]*
nsubj	*acl*	*relcl*	*dobj*	*pobj*	*prep*	*punct*	*xcomp*	

Encode dependencies



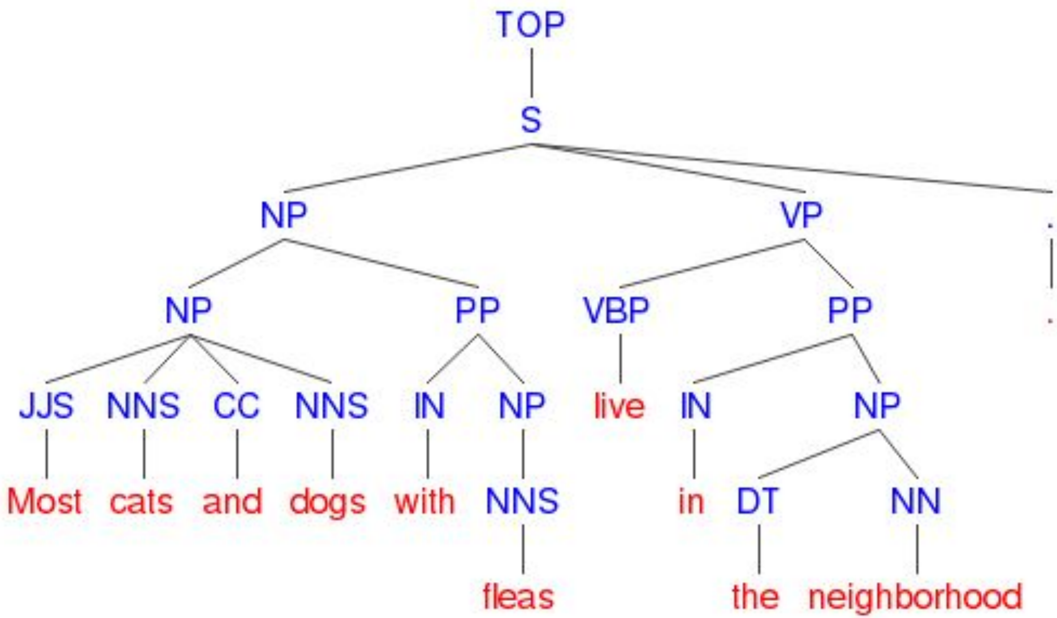
“eat”/VBP:

- *nsubj_We, dobj_pizza, prep_with*
- *nsubj_PRP, dobj_NN, prep_IN*
- *nsubj_We, dobj_pizza, prep_with_pobj_anchovy*

Encode constituents

“fleas”/NNS:

{“label”: “NP”,
 “anc-left”: ”PP”,
 “anc-right”: ”S”,
 “span-start”: 5,
 “span-end”: 6}



More features

- affixes
- coreference
- sentiment
- grammatical characteristics of various parts of speech:
  - countability of nouns
  - tense of verbs
  - degree of comparison of adjectives
  - pronoun type
  - conjunction type

More features

- *capitalized?*
- *hyphenated?*
- *compound?*
- *lemma*
- *sense id*
- *number of senses in WordNet*
- *is in X dictionary*
- *has X as a synonym*
- …

Example

```
DT  NN    VBD      NNS    IN      DT   DT  NN     CC  DT  NN   .
The pound extended losses against both the dollar and the euro .
```

Features:

- *word*
- *is the word capitalized*
- *word length*
- *word[-1]*
- *tag[-1]*
- *word_tag[+1]*

Example

DT	NN	VBD	NNS	IN	DT	DT	NN	CC	DT	NN	.
The	pound	extended	losses	against	both	the	dollar	and	the	euro	.

Features:

- *gold or predicted?*
- *what algorithms can use these features?*

4. Logistic Regression

Logistic Regression

Logistic regression - a **discriminative** linear model used for binary classification.

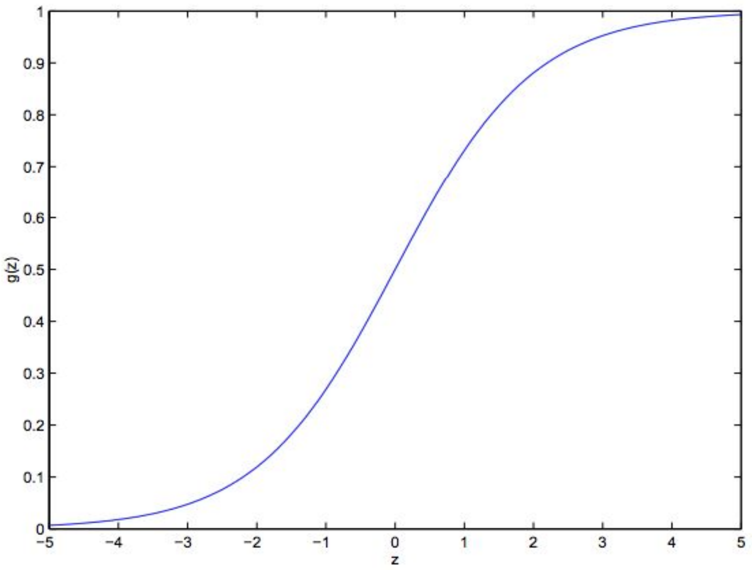
- like Perceptron, it's linear
- like NB, it extracts a set of weighted features, takes logs, and combines them linearly
- unlike NB, it's discriminative

Logistic Regression

We need a function that goes from 0 to 1.

E.g., a sigmoid function:

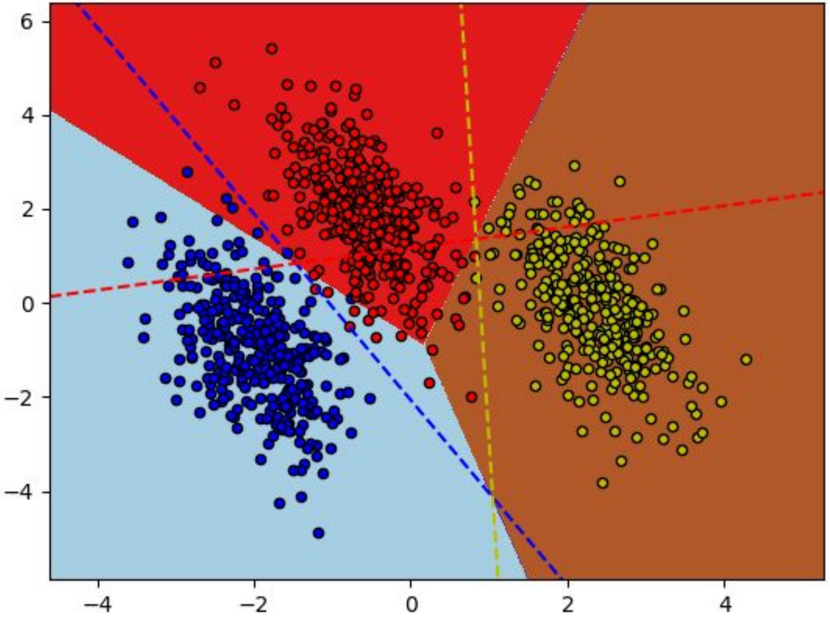
$$P(y_i = 1 \mid x_i) = \frac{1}{1 + \exp(-\mathbf{w}^T \mathbf{x}_i)}$$



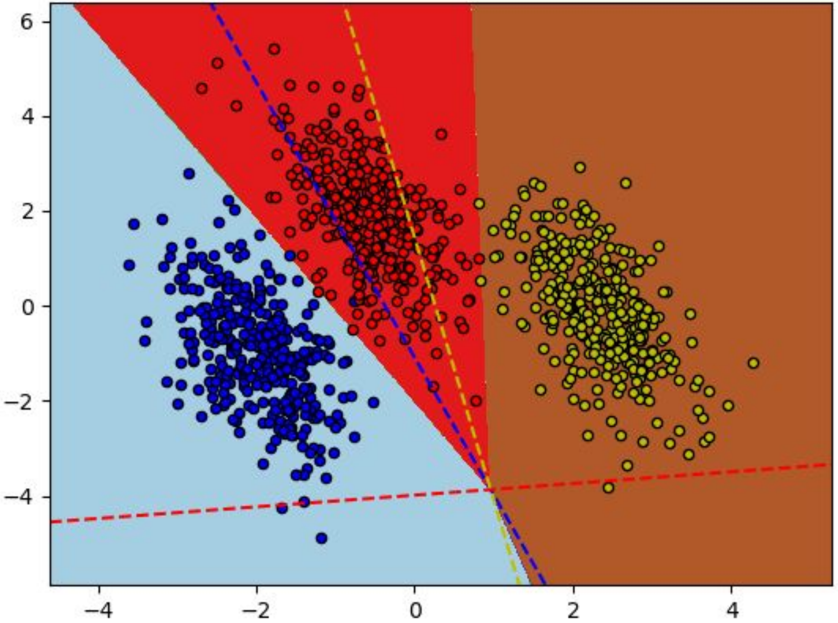
Borrowed from Andrew Ng: https://goo.gl/zGvb4W

Logistic Regression: multiclass

one vs. rest



multinomial (MaxEnt)



http://scikit-learn.org/stable/auto_examples/linear_model/plot_logistic_multinomial.htm

Logistic Regression

For multinomial logistic regression, use softmax:

$$p(c|x) = \frac{\exp\left(\sum_{i=1}^{N} w_i f_i(c,x)\right)}{\sum_{c' \in C} \exp\left(\sum_{i=1}^{N} w_i f_i(c',x)\right)}$$

Logistic Regression: example

Welcome to St . Paul ‘s Cathedral !

[Is this period a sentence end?]

Logistic Regression: example

Welcome to St . *Paul* ‘s Cathedral !

[Is this period a sentence end?]

y: {*is-end*, *is-not-end*}
x: {“*word+1_is_cap*”, “*word-1=hi*”, “*word-1=St*”, “*tag-1=PRP*”, “*tag+1=JJ*”}

Logistic Regression: example

Welcome to St . *Paul* ‘s Cathedral !

[Is this period a sentence end?]

y: *{is-end, is-not-end}*
x: {“word+1_is_cap”, “word-1=hi”, “word-1=St”, “tag-1=PRP”, “tag+1=JJ”}

$\mathbf{x}_j$: *[1, 0, 1, 0, 0]*

$\mathbf{w}_{\textbf{is-end}}$: *[2.9, 2.5, -0.9, 0, 0]*
$\mathbf{w}_{\textbf{is-not-end}}$: *[0.5, -0.7, 2.9, 0, 0]*

Logistic Regression: example

Welcome to St . Paul ‘s Cathedral !

[Is this period a sentence end?]

y: {is-end, is-not-end}
x: {“word+1_is_cap”, “word-1=hi”, “word-1=St”, “tag-1=PRP”, “tag+1=JJ”}

$\mathbf{x}_j$: [1, 0, 1, 0, 0]

$\mathbf{w}_{\text{is-end}}$: [2.9, 2.5, -0.9, 0, 0] **P(is-end|$\mathbf{x}_j$)** $= e^{2.9-0.9} / (e^{2.9-0.9} + e^{0.5+2.9}) = 0.2$
$\mathbf{w}_{\text{is-not-end}}$: [0.5, -0.7, 2.9, 0, 0] **P(is-not-end|$\mathbf{x}_j$)** $= e^{0.5+2.9} / (e^{2.9-0.9} + e^{0.5+2.9}) = 0.8$

Logistic Regression: weights

Learn weights:

- start with a vector of zeros
- move towards the gradient
- to maximize the probability

$$\hat{w} = \operatorname*{argmax}_{w} \sum_{j} \log P(y^{(j)} | x^{(j)})$$

5. Conditional Random Fields

Conditional Random Fields

CRFs = MaxEnt + HMM

- HMM - generative, **classifies the whole sequence at once**
  - $p(x, y)$
- MaxEnt - **discriminative**, classifies elements one by one
  - $p(y_i=1|x_i)$
- CRFs - **discriminative, classify the whole sequence at once**
  - $p(y|x)$

Conditional Random Fields

- MaxEnt

$$p(c|x) = \frac{\exp\left(\sum_{i=1}^{N} w_i f_i(c,x)\right)}{\sum_{c' \in C} \exp\left(\sum_{i=1}^{N} w_i f_i(c',x)\right)}$$

- CRF also learns transitions

$$p(l|s) = \frac{exp(\sum_{j=1}^{m} \sum_{i=1}^{n} w_j f_j(s, i, l_i, l_{i-1}))}{\sum_{l'} exp(\sum_{j=1}^{m} \sum_{i=1}^{n} w_j f_j(s, i, l'_i, l'_{i-1}))}$$

Conditional Random Fields

$$p(l|s) = \frac{exp(\sum_{j=1}^{m}\sum_{i=1}^{n} w_j f_j(s, i, l_i, l_{i-1}))}{\sum_{l'} exp(\sum_{j=1}^{m}\sum_{i=1}^{n} w_j f_j(s, i, l'_i, l'_{i-1}))}$$

s - sentence (list of words)
l - list of labels

i - index of a word in *s*
l_i - label of the word *i*
l_{i-1} - label of the word before *i*

6. More about Ngrams

What are ngrams

Ngram - a contiguous sequence of ***n*** items from a given text.

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So, if ***n* = 3**:

<S> Why did n’t you listen to me ? </S>

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Ngram - a contiguous sequence of ***n*** items from a given text.

So, if ***n*** **= 3**:

<S> Why did n’t you listen to me ? </S>

Token ngrams

Usually 1 ≥ n ≥ 5.

<S>   Why   did   n't   you   listen   to   me   ?   </S>

n = 1: *(<S>), (Why), (did), (n't), (you), (listen), (to), (me), (?)...*

n = 2: *(<S> Why), (Why did), (did n't), (n't you), (you listen), (listen to)...*

n = 3: *(<S> Why did), (Why did n't), (did n't you), (you listen to)...*

...

Character Ngrams

<S> Why did n’t you listen to me ? </S>

For words:

n = 3: *(<w> W h), (W h y), (h y </w>), (<w> d i), (d i d), (i d n), (d n ‘)…*

For sentences:

n = 3: *(W h y), (h y _), (y _ d), (_ d i), (d i d), (i d n), (d n ‘), (n ‘ t)…*

POS Ngrams

<S>	Why	did	n’t	you	listen	to	me	?	</S>
<S>	WDT	VDB	RB	PRP	VB	TO	PRP	.	</S>

POS:

***n* = 3**: *(<S>, WDT, VBD), (WDT, VBD, RB), (VBD, RB, PRP), (RB, PRP, VB)…*

Token+POS:

***n* = 2**: *(<S>_<S>, Why_WDT), (Why_WDT, did_VBD), (did_VBD, n’t_RB)…*

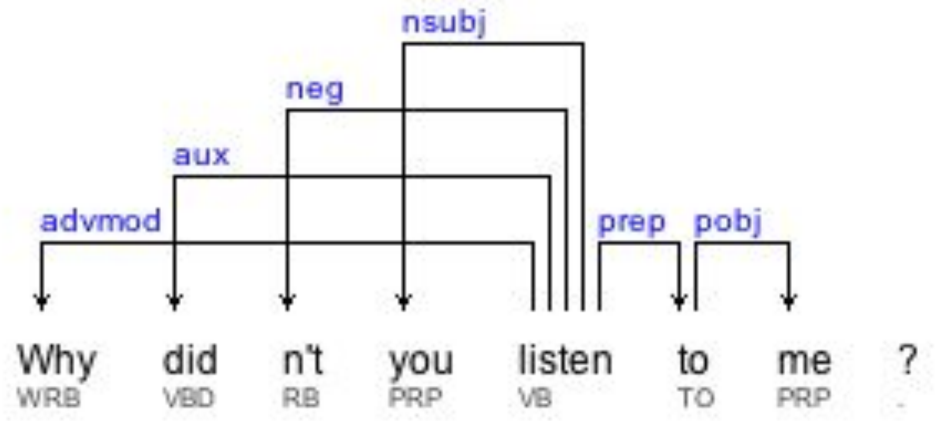
Token or POS:

***n* = 3**: *(<S>, WDT, did), (WDT, did, RB), (did, RB, PRP), (RB, PRP, listen)…*

Tree Ngrams

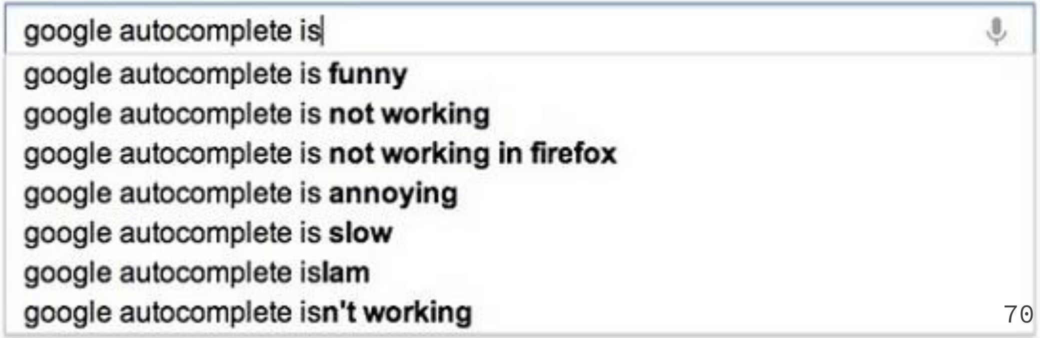
Head+dependency:
listen_nsubj
listen_nsubj_you
listen_prep_to_pobj_me

Head+POS+dependency:
listen/VB_nsubj
listen/VB_nsubj_you/PRP



Ngrams usage

1. Speech recognition
2. Handwriting recognition
3. Autocompletion



Ngrams usage

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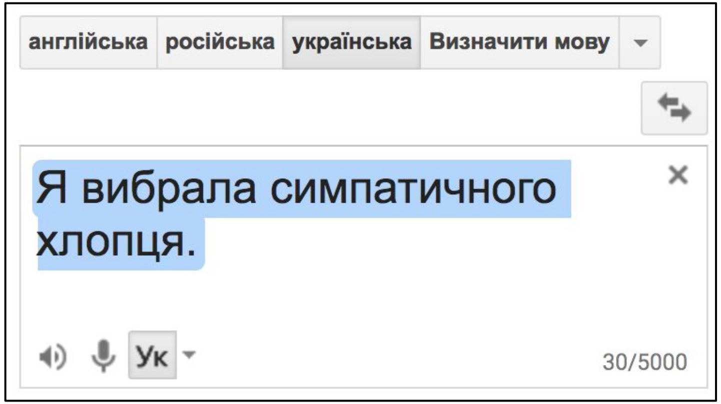
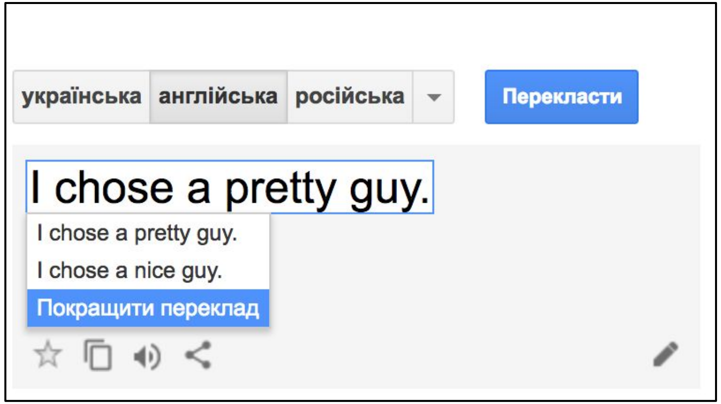




Ngrams usage

1. Speech recognition
2. Handwriting recognition
3. Autocompletion
4. Machine Translation
5. Spelling correction
6. (and GEC in general)

Ngrams as a feature

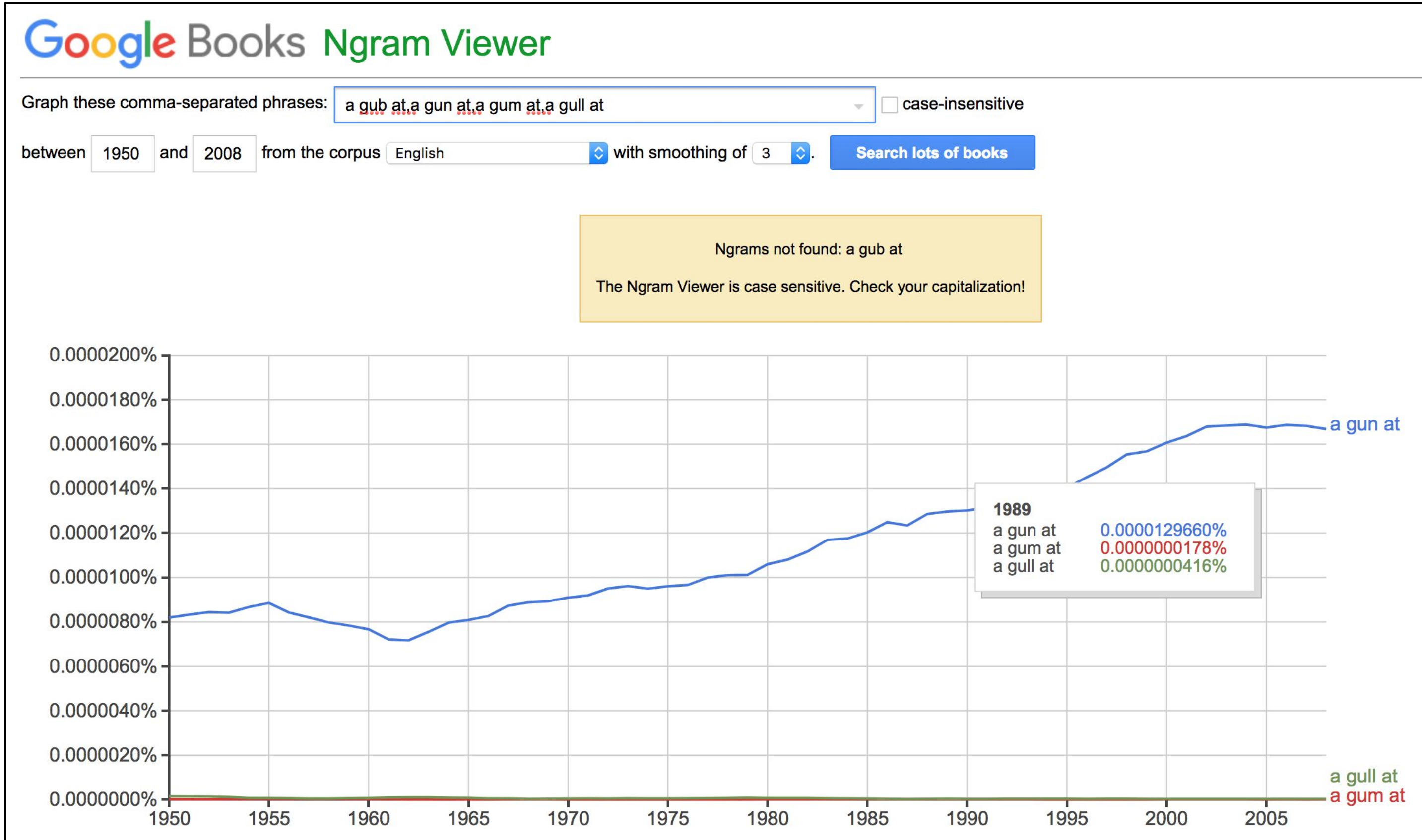
Frequency or probability:

a gub at

a gun at

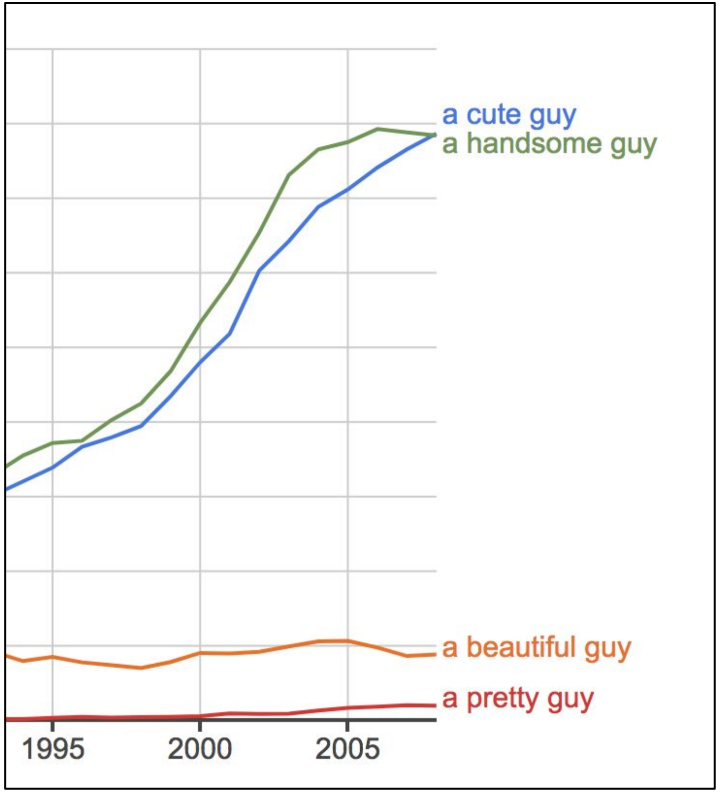
a gum at

a gull at



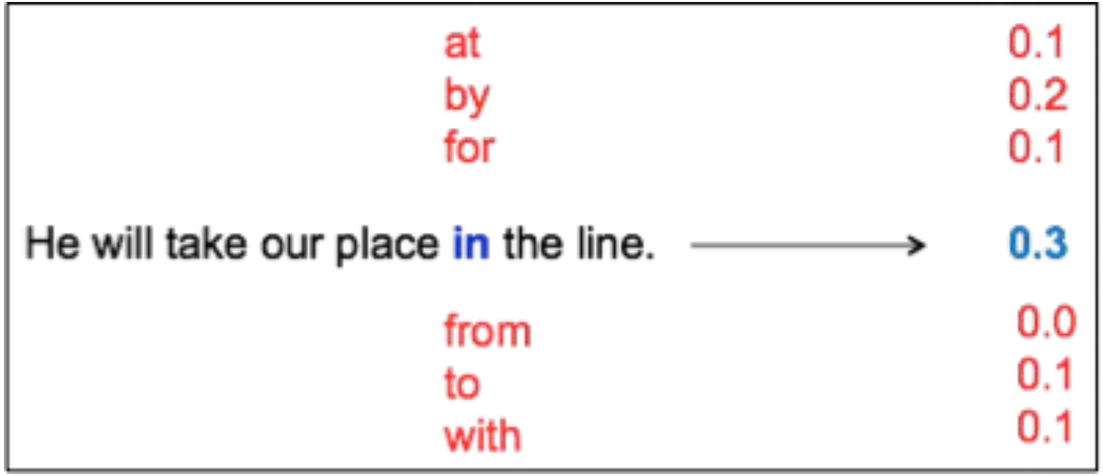
Ngrams as a feature

Frequency or probability



Ngrams as a feature

Frequency or probability



Ngrams as a feature

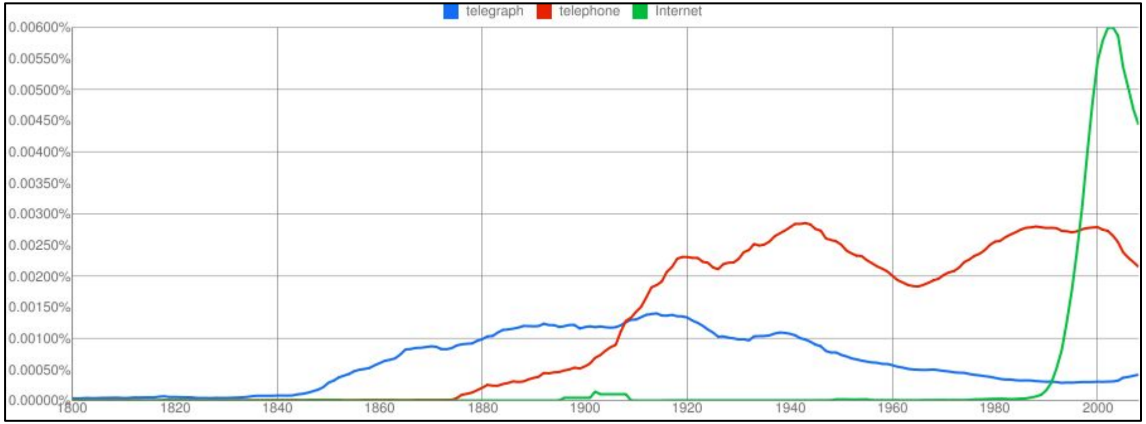
Conditional probability

$$P(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n)}{C(w_{n-1})}$$

To be continued on the lecture about language modeling…

Where to get ngrams

- 1 mln of 2/3/4/5-ngrams from COCA for free
- Google ngrams (and how to download)
- Google syntactic ngrams
- collect on your own



How to encode ngram frequencies

Ngrams:

"*met a cute*": 3250, "*a cute guy*": 25289, "*met a cute guy*": 600, ...
"*met a pretty*": 2925, "*a pretty guy*": *1159*, "*met a pretty guy*": 0, ...

- As additional vector to concatenate:
  - *[3250, 25289, 600, 2925, 1159, 0, ...]*

- As part of the feature dictionary:
  - {"left-3gr": 3250, "right-3gr": 25289, "middle-4gr": 600, "left-3gr-2": 2925, "right-3gr-2": *1159*, "middle-4gr-2": 0, ...}

References

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