Cheatsheets / Probability

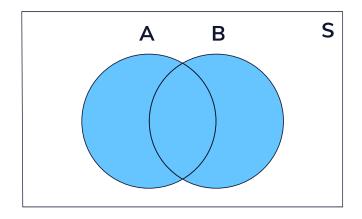
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Rules of Probability

Union

The *union* of two sets encompasses any element that exists in either one or both of them. We can represent this visually as a *venn diagram* as shown. Union is often represented as:

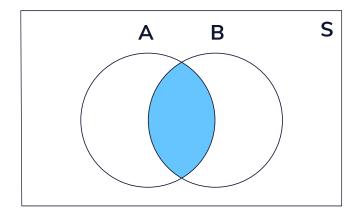
(A or B)



Intersection

The intersection between two sets encompasses any element that exists in BOTH sets and is often written out as:

 $(A \ and \ B)$



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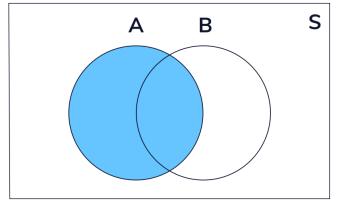
Addition Rule

If there are two events, A and B, the addition rule states that the probability of event A or B occurring is the sum of the probability of each event minus the probability of the intersection:

$$P(A \text{ or } B) = P(A) + P(A)$$

If the events are mutually exclusive, this formula simplifies to:

$$P(A \text{ or } B) = P(A) + P(A)$$



P(A or B) = P(A)



Multiplication Rule

The multiplication rule is used to find the probability of two events, *A* and *B*, happening simultaneously. The general formula is:

$$P(A \text{ and } B) = P(A) \cdot P(A)$$

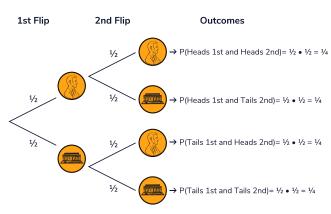
For independent events, this formula simplifies to:

$$P(A \text{ and } B) = P(A) \cdot P(A)$$

This is because the following is true for independent events:

$$P(B \mid A) = P(B)$$

The tree diagram shown displays an example of the multiplication rule for independent events.



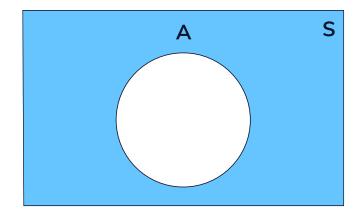
Sum of all possible outcomes = $\frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = 1$



Complement

The complement of a set consists of all possible outcomes outside of the set.

Let's say set A is rolling an odd number with a 6-sided die: $\{1, 3, 5\}$. The complement of this set would be rolling an even number: $\{2, 4, 6\}$. We can write the complement of set A as A^C . One key feature of complements is that a set and its complement cover the entire sample space. In this die roll example, the set of even numbers and odd numbers would cover all possible rolls: $\{1, 2, 3, 4, 5, 6\}$.

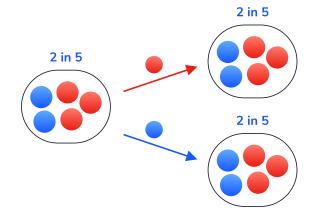


Independent Events

Two events are *independent* if the occurrence of one event does not affect the probability of the other one occurring.

Let's say we have a bag of five marbles: three are red and two are blue. If we select two marbles out of the bag WITH replacement, the probability of selecting a blue marble second is independent of the outcome of the first event.

The diagram below outlines the independent nature of these events. Whether a red marble or a blue marble is chosen randomly first, the chance of selecting a blue marble second is always 2 in 5.





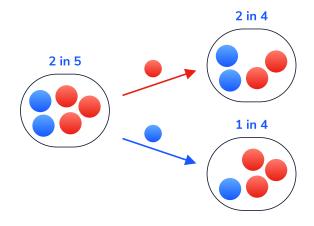
Dependent Events

Two events are *dependent* if the occurrence of one event does affect the probability of the other one occurring.

Let's say we have a bag of five marbles: three are red and two are blue. If we select two marbles out of the bag WITHOUT replacement, the probability of selecting a blue marble second depends on the outcome of the first event.

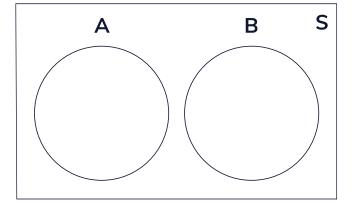
The diagram below outlines this dependency. If a red marble is randomly selected first, the chance of selecting a blue marble second is 2 in 4.

Meanwhile, if a blue marble is randomly selected first, the chance of selecting a blue marble second is 1 in 4.



Mutually Exclusive Events

Two events are considered *mutually exclusive* if they cannot occur at the same time. For example, consider a single coin flip: the events "tails" and "heads" are mutually exclusive because we cannot get both tails and heads on a single flip. We can visualize two mutually exclusive events as a pair of non-overlapping circles. They do not overlap because there is no outcome for one event that is also in the sample space for the other.



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Conditional Probability

Conditional probability is the probability of one event occurring, given that another one has already occurred. We can represent this with the following notation:

Probability of event A oc

For independent events, the following is true for events *A* and *B*:

$$P(A \mid B) = P(A)$$

and
 $P(B \mid A) = P(B)$



Bayes' Theorem

Bayes' theorem is a useful tool to find the probability of an event based on prior knowledge. The formula for Bayes' theorem is:

$$P(B \mid A) = \frac{P(A \mid B) \cdot P}{P(A)}$$

