

DSA: A1, A2 and A3 Desk Checking Lab Exercises

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Abstract

The purpose of this documents is to provide you concrete preparation material for the examination of the practicum.

It contains pseudocode and code of the tasks from the assignment A1, A2 and A3. Remember that the practicum examination will also include A4 (due this week) and **will not include** pseudocode.

While the pseudocode is correct, the code may contain conceptual or minor syntax errors. Every task contains a series of questions regarding the previous code. At the end of every assignment you will also find multiple technical questions about the relevant topics.

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1 Assignment 1

1.1 Task 0: Operator overloading

This code creates a Vector class. Every Vector object is made of an x and a y value, they represent the coordinates of a vector in a 2D space. The class overloads the "+" operator and realizes a vector sum.

Pseudocode

```
1 Define Vector class
2     Define init(x, y)
3         Assign x to field x
4         Assign y to field y
5     Define add(other)
6         If other is instance of class Vector
7             then return the summed Vector
8         else
9             raise TypeError
10
11 # Main code
12 v1 = (1, 2)
13 v2 = (3, 4)
14 v3 = v1 + v2
```

Code

```
1 class Vector:
2     def __init__(self, x, y):
3         self.x = x
4         self.y = y
5
6     def __add__(self, other):
7         if isinstance(other, Vector):
8             return Vector(self.x + other.x, self.y + other.y)
9         else:
10            raise TypeError(
11                "Unsupported operand type for +: "+str((type(other)))
12            )
13
14 # Main code
15 v1 = Vector(1, 2)
16 v2 = Vector(3, 4)
17 v3 = v1 + v2
```

Which of the following statement(s) about the implementation ('code') above are **true**:

- ☐ The __add__ is wrongly named. In order to overload the plus operator, the function should be called __+__ instead.
- ☐ The overload of the + operator has been correctly implemented, the result will be a vector with coordinates (4, 6).
- ☐ The overload of the + operator has been correctly implemented, the result will be a vector with coordinates (3, 8).
- ☐ The implementation is wrong since the other variable used in the __add__ function is defined outside the function scope, therefore being not visible inside the function.

1.2 Task 1: Bubble sort

The code implements the Order class. An Order will contain 3 fields: `id`, `selection_time`, `shipping_time`. The `=`, `<`, `>` operators have been overloaded. A bubble sort algorithm has been implemented, the bubble sort algorithm is wrapped in the sort method that parses the data and creates Order objects to pass to the bubble sort core method.

Pseudocode

```
1 Define Order class
2   Define init(id, selection time, shipping time)
3     Assign id to field id
4     Assign selection time to field selection time
5     Assign shipping time to field shipping time
6   Define eq(other)
7     Return true if this object and other object have same fields value
8     else false
9   Define gt(other):
10    Return true if this object fields sum is greater than other object
11    fields sum else false
12
13 Define bubbleSort(array)
14   for each item in the array with i being the current index
15     for each element but the last i
16       swap current element with the following if the following is
17       smaller than the current
18
19 Define sort(data)
20   for each triplet in data
21     append order initialized with the triplet to the array
22   bubbleSort(array)
23
24   return list of [id of each order in array]
```

Code

```
1 class Order:
2     def __init__(self, id, selection_time, shipping_time):
3         self.id: int = id
4         self.selection_time: int = selection_time
5         self.shipping_time: int = shipping_time
6
7     def __eq__(self, other):
8         return (self.selection_time + self.shipping_time) == (other.
9             selection_time + other.shipping_time)
10
11     def __gt__(self, other):
12         return (self.selection_time + self.shipping_time) > (other.
13             selection_time + other.shipping_time)
14
15 def bubbleSort(array: List[Order]):
16     n = len(array)
17     for i in range(n-1):
```

```

18
19         for j in range(1, n-i-1):
20
21             if array[j] > array[j+1]:
22                 array[j], array[j+1] = array[j+1], array[j]
23
24 def sort(data: List[Tuple[int,int,int]]) -> List[int]:
25     arr: List[Order] = []
26
27     for id, selection_t, shipping_t in data:
28         arr.append(Order(id, selection_t, shipping_t))
29
30     bubbleSort(arr)
31
32     return [a.id for a in arr]

```

Which of the following statement(s) about the implementation ('code') above are **true**:

- ☐ On line 17, `range(n-1)` prevents the `i` index to traverse all the elements leaving the last element untouched.
- ☐ The implementation is correct and contains no bug.
- ☐ The `j` index is misused since it avoids comparing the first item of the list with the second.
- ☐ On line 22, a support variable should be used to swap the array values, otherwise the result could be non deterministic.

1.3 Task 2: Merge sort

The code implements the Order class just like in the previous example. We did not copy the Order class implementation, you can assume it's correct. The difference from the previous Task Order implementation is that there is a `Order.next` field in this class which represent the following Order (a pointer to the next element, just like in linked lists). The code implements a bottom up merge sort. The final `sort` method used in the previous Task code has been omitted, focus on the core merge sort algorithm instead.

Pseudocode

```
1  # Assume that the objects have a .next field that represent the following  
   element, None if there's none  
2  
3  Define merge_sort(head)  
4      if head is empty return None  
5  
6      arr = list of 32 Nones  
7      result, next = None  
8  
9      result = head  
10  
11     # Merge nodes into array  
12     while result is not null:  
13         Save the reference to the result next node into next  
14         Reset the result to None  
15         For each value of arr  
16             If current value is None then break  
17             result = merge(current value, result)  
18             Assign null to current value  
19         Assign result to the second last value of arr  
20         result = next  
21  
22     # Merge array into single list  
23     result = null  
24     For each item in arr  
25         result = merge(current value, result)  
26  
27     return result  
28  
29  Define merge(left, right)  
30     result = None  
31     ref = None  
32  
33     While left is not null and right is not null:  
34         If right greater or equal to left  
35             If result is not null then append left to the result  
36             else assign left to the result  
37             Assign the value after left to left  
38         else  
39             If result is not null then append right to the result  
40             else assign right to the result  
41             Assign the value after right to right  
42  
43     While there are elements remaining in left  
44         Append left to result
```

```

45         Assign the value after left to left
46
47     While there are elements remaining in right
48         Append right to result
49         Assign the value after right to right
50
51     Return the pointer to the start of the list

```

Code

```

1  def merge_sort(head: Union[Order, None]) -> Union[Order, None]:
2      if not head:
3          return None
4      arr: List[Union[Order, None]] = [None for _ in range(32)]
5      result: Union[Order, None] = None
6      next: Union[Order, None] = None
7      result = head
8
9      while result:
10         next = result.next
11         result.next = None
12         i = 0
13         for i in range(32):
14             if arr[i] is None:
15                 break
16             result = merge(arr[i], result)
17             arr[i] = None
18
19         arr[i] = result
20         result = next
21
22     result = None
23     for i in range(32):
24         result = merge(arr[i], result)
25
26     return result
27
28
29 def merge(left: Union[Order, None], right: Union[Order, None]) -> Union[Order,
None]:
30     result: Union[Order, None] = None
31     ref: Union[Order, None] = None
32
33     while left and right:
34         if left <= right:
35             if result:
36                 result.add_next(left)
37                 result = left
38             else:
39                 ref = left
40                 result = left
41
42         left = left.next
43
44     else:

```

```

45         if result:
46             result.add_next(right)
47             result = right
48         else:
49             ref = right
50             result = right
51
52         right = right.next
53
54     while left:
55         if result:
56             result.add_next(left)
57             result = left
58         else:
59             ref = left
60             result = left
61
62         left = left.next
63
64     while right:
65         if result:
66             result.add_next(right)
67             result = right
68         else:
69             ref = right
70             result = right
71
72         right = right.next
73
74     return ref

```

Which of the following statement(s) about the implementation ('code') above are **true**:

- ☐ At line 15, we should not **break** but instead **return result**, otherwise the code will never return once we are at the end.
- ☐ The implementation is correct and contains no bug.
- ☐ The code will only run for array of length divisible by 32.
- ☐ At line 35 we cannot use **while left and right:** since they are lists and will never have **True** or **False** as a value.

1.4 Task 3: Quick sort

The code implements the Order class just like in the previous examples. We did not copy the Order class implementation, you can assume it's correct. The code implements a quick sort.

Pseudocode

```
1 Define swap(arr, i, j)
2     Swap objects between the indexes i and j of the arr list
3
4 Define quicksort(arr, lo, hi)
5     If lo and hi are greater or equal to 0 and if lo is less than hi
6         Partition the array
7         Call the quicksort on the right partition
8         Call the quicksort on the left partition
9
10 Define partition(arr, lo, hi)
11     Pivot object is the object in the middle of the list
12
13     Set one counter (i) to the index before the lower index
14     Set one counter (j) to the index after the upper index
15
16     Loop forever
17         Update i by decreasing it by one
18         While the value in arr at index i is less than the pivot
19             Increase i (so that we are consider the next element in arr)
20         Update j by decreasing it by one
21         While the value in the arr at index j is greater that the pivot
22             Increase j (so that we are consider the previous element in arr)
23
24         If the indexes i and j have crossed (i>=j) then return j
25
26         Swap the element at index i with the one at index j
27
28 Define sort(data)
29     Create an empty support list
30
31     Fill the support list with the objects in data, converting them into an
        Order object
32
33     Call quicksort on the list
34
35     Return the id of every Order in the list
```

Code

```
1 def swap(arr: List[Order], i: int, j: int):
2     arr[i], arr[j] = arr[j], arr[i]
3
4 def quicksort(arr: List[Order], lo: int, hi: int):
5     if lo >= 0 and hi >= 0 and lo < hi:
6         p = partition(arr, lo, hi)
7         quicksort(arr, p + 1, hi)
8         quicksort(arr, 0, p)
9
```

```

10 def partition(arr: List[Order], lo: int, hi: int):
11     pivot = arr[(hi+lo)//2]
12
13     i = lo
14     j = hi
15
16     while(True):
17
18         i = i + 1
19         while arr[i] < pivot:
20             i = i + 1
21
22         j = j - 1
23         while arr[j] > pivot:
24             j = j - 1
25
26         if i >= j:
27             return j
28
29         swap(arr, i, j)
30
31
32 def sort(data: List[Tuple[int,int,int]])->List[int]:
33     arr: List[Order] = []
34
35     for id, selection_t, shipping_t in data:
36         arr.append(Order(id, selection_t, shipping_t))
37
38     quicksort(arr, 0, len(arr)-1)
39
40     return [a.id for a in arr]

```

Which of the following statement(s) about the implementation ('code') above are **true**:

- ☐ The implementation is correct and contains no bug.
- ☐ At line 2, the value swap between two variables cannot be done in that manner. It is necessary to rely on a temporary variable.
- ☐ At lines 12 and 13 the i and j indexes should be initialized as i = lo-1 and j = hi+1
- ☐ At lines 12 and 13 the i and j indexes should be initialized as i = lo+1 and j = hi-1
- ☐ At line 10, the pivot should be set as pivot = arr[lo], else the algorithm will not be able to sort correctly.

1.5 Task 4: Quick sort

The code implements the Order class just like in the previous example. We did not copy the Order class implementation, you can assume it's correct. The code implements a quick sort with out-of-place sorting since smaller and greater elements than the pivot are moved into new separate lists and not swapped within the starting list. In-place sorting would consist in moving the elements within the same original list, like we've done in the previous task. This process makes the code easier to understand but less memory efficient.

Pseudocode

```
1 Define swap(arr, i, j)
2     Swap values of arr at index i and j
3
4 Define quicksort(ar)
5     If there is one or less elements return ar
6
7     Pick the middle element as pivot
8     Create two empty lists, one for objects smaller and one for objects
   greater than the pivot
9     If you are analyzing the pivot then skip to the next object in list
10    Put elements greater or same as the pivot in the list for the greater
   objects
11    Put elements smaller than the pivot in the list for the smaller objects
12
13    Set as the left list the quicksorted list with objects smaller than the
   pivot
14    Set as the right list the quicksorted list with objects greater than the
   pivot
15    Return the left list, appending the pivot, appending the right list
```

Code

```
1 def swap(arr: List[Order], i: int, j: int):
2     tmp = arr[i]
3     arr[i] = arr[j]
4     arr[j] = tmp
5
6 def quicksort(ar: List[Order]):
7
8     if len(ar) <= 1:
9         return ar
10
11     mid = len(ar)//2
12     pivot = ar[mid]
13
14     smaller, greater = [], []
15
16     for i, val in enumerate(ar):
17         if i == mid:
18             continue
19         if val < pivot:
20             smaller.append(val)
21         elif val > pivot:
22             greater.append(val)
```

```
23
24     left  = quicksort(smaller)
25     right = quicksort(greater)
26     return left+[pivot]+right
```

Which of the following statement(s) about the implementation ('code') above are **true**:

- ☐ The implementation is correct and contains no bug.
- ☐ The case of `val == pivot` is not specified, for this reason all the values equal to the pivot will be lost at every iteration.
- ☐ The `pivot` is not included in the left sub-list nor the right sub-list, therefore its value will be lost during the execution.
- ☐ The variable `mid` defined at line 11 may be a decimal number when `len(ar)` is an odd number. Thus causing the code to fail, since we cannot use a decimal value as array index.

1.6 Task 5: Quick sort

The code implements the Job class just like in Assignment 1 Task 3. In the Job class, p stands for the processing time, w represents the importance. When a Job finishes at time t then the total cost is $t \cdot w$. The goal is to sequence the jobs in order to minimize the total cost of all the jobs. It uses Smith's rule, that is, schedule the jobs in the order of their ratio of processing time over weight. This greedy rule turns out to be optimal. The code implements a quick sort. This time, differently from the Assignment, we don't care if the order of equal jobs is the same both in the input and the output, if the jobs are equal according to $==$ then they can be in whatever order.

Pseudocode

```
1 Define the Job class
2     Define the Job constructor(self, id, p, w)
3
4     Override the greater or equal operator(self, other)
5         Return the result of self.p/self.w >= other.p/self.w
6
7     Override the less than operator(self, other)
8         Return the result of self.p/self.w < other.p/self.w
9
10    Override the greater than operator(self, other)
11        Return the result of self.p/self.w > other.p/self.w
12
13 Define quicksort(ar)
14     If there is one or less elements return ar
15
16     Pick the middle element as pivot
17     Create two empty lists, one for objects smaller and one for objects
18         greater than the pivot
19     If you are analyzing the pivot then skip to the next object in list
20     Put elements greater than the pivot in the list for the greater objects
21     Put elements smaller than the pivot in the list for the smaller objects
22     Put elements equal to the pivot in the greater or smaller list based on
23         their index
24
25     Set as the left list the quicksorted list with objects smaller than the
26         pivot
27     Set as the right list the quicksorted list with objects greater than the
28         pivot
29     Return the left list, appending the pivot, appending the right list
30
31 Define sort(data)
32     Define an empty array of jobs
33
34     For every value in data
35         Create a Job object starting from the three individual values (id, p
36             for processing time, w for importance) and add it to the list of
37             jobs
38
39     Run quicksort on the array
40
41     Return every id of the job in the sorted array
```

Code

```
1 class Job:
2     def __init__(self, id, p, w):
3         self.id: int = id
4         self.p: int = p
5         self.w: int = w
6
7     def __ge__(self, other):
8         return ((self.p / self.w) >= (other.p / other.w))
9
10    def __lt__(self, other):
11        return ((self.p / self.w) < (other.p / other.w))
12
13    def __gt__(self, other):
14        return ((self.p / self.w) > (other.p / other.w))
15
16
17 def quicksort(ar: List[Job]):
18
19     if len(ar) <= 1:
20         return ar
21
22     mid = len(ar)//2
23     pivot = ar[mid]
24
25     smaller, greater = [], []
26
27     for i, val in enumerate(ar):
28         if i == mid:
29             smaller.append(val)
30         if val < pivot:
31             smaller.append(val)
32         elif val > pivot:
33             greater.append(val)
34
35     else:
36         if i < mid:
37             greater.append(val)
38         else:
39             smaller.append(val)
40
41     left = quicksort(smaller)
42     right = quicksort(greater)
43     return left+[pivot]+right
44
45
46 def sort(data: List[Tuple[int, int, int]])->List[int]:
47     arr: List[Job] = []
48
49     for id, p, w in data:
50         arr.append(Job(id, p, w))
51
52     arr = quicksort(arr)
53
54     return [a.id for a in arr]
```

Which of the following statement(s) about the implementation ('code') above are **true**:

- ☐ The if statement at line 36, appends jobs equal to the pivot into the wrong list, preventing the correct sorting of the list.
- ☐ The implementation is correct and contains no bug.
- ☐ The code will duplicate the pivot value of the array passed to the **quicksort** method.
- ☐ The **greater** and **smaller** lists passed to **quicksort** will not be correctly unpacked, preventing the correct execution.

1.7 Questions

Which of the following statement(s) are true:

- ☐ There is no point in using quicksort over mergesort since quicksort worst case scenario is worse than the mergesort one ($O(n^2)$ versus $O(n \log(n))$).
- ☐ Recursive functions use more memory than their respective iterative counterpart.
- ☐ There's no difference between the way we choose the pivot in quicksort.

2 Assignment 2

2.1 Task 1

In this exercise we will implement a linked list and its remove method, used to remove the first occurrence of an object.

Pseudocode

```
1 Define class Node
2     Define init(value)
3         Set field value to value
4         Set field next to None
5
6 Define class LinkedList
7     Define init
8         Set head field to None
9
10    Define append(value)
11        Create a new node starting from the value parameter
12        If there is no value in the list, then set the new node to the head
13        field
14    else
15        Starting from the head
16        Reach the last node in the list
17        Attach the new node, referencing it in the next field of the
18        current last value
19
20    Define remove(value)
21        If there is no node, terminate
22        If the first element is the one to remove, then set the head to the
23        second node
24        Set the head as current node
25        While there is a next value in the next field of the current node
26            If the value of the next item is the one to remove then
27                Set the next field to reference the node after the next node
28            Terminate
29        Set the current node to the next node
```

Code

```
1 class Node:
2     def __init__(self, value):
3         self.value = value
4         self.next = None
5
6 class LinkedList:
7     def __init__(self):
8         self.head = None
9
10    def append(self, value):
11        new_node = Node(value)
12        if self.head is None:
13            self.head = new_node
14        else:
```



```

15         current = self.head
16         while current.next:
17             current = current.next
18         current.next = new_node
19         new_node.next = current
20
21     def remove(self, value):
22         if self.head is None:
23             return
24         if self.head.value == value:
25             self.head = self.head.next
26             return
27         current = self.head
28         while current.next:
29             if current.next.value == value:
30                 current.next = current.next.next.next
31                 return
32         current = current.next

```

Which of the following statement(s) about the implementation above are **true**:

- ☐ This is a correct implementation of a linked list and its append and remove methods
- ☐ On line 30, assigning `current.next.next.next` would cause the method to remove the correct value but also the value after it.
- ☐ The `append` method is bugged, since after adding a new item to a non empty list we set the last item's `next` field to the second last item, creating a loop among the two last nodes.
- ☐ The `__init__` method in the `LinkedList` class is bugged, since we cannot have an empty list because then we have no previous item to attach new nodes to.

2.2 Task 2

This task implements a binary search algorithm in a recursive fashion, we can assume that the arr array is sorted.

Pseudocode

```
1 Define binary_search(arr, x)
2   If the array is empty
3     Return -1
4   Set mid var to half of the array length
5   If the middle value of the array is the searched value, then return the
      middle index
6   Else if the middle value is smaller than the searched value
7     then set the result to binary_search(subarray starting from mid+1
      onward, x)
8     Return the result+index of the middle index+1, if result is -1 return
      -1
9   else return the result of binary_search(subarray from index 0 to mid-1, x)
```

Code

```
1 def binary_search(arr, x):
2   if not arr:
3     return -1
4
5   mid = len(arr) // 2
6
7   if arr[mid] == x:
8     return mid
9   elif arr[mid] < x:
10    result = binary_search(arr[mid+1:], x)
11    return result + mid + 1 if result != -1 else -1
12  else:
13    return binary_search(arr[:mid], x)
```

Which of the following statement(s) about the implementation above are **true**:

- ☐ The algorithm is sub-optimal, since on line 13, the array passed to binary_search also includes arr[mid] which we've already proven not equal to x.
- ☐ The code is correct but using a linked list would reduce the execution time.
- ☐ The code is correct and wouldn't be faster with a linked list.
- ☐ Line 11 is not correct Python syntax.
- ☐ Being a recursive algorithm, if no correct value is found, the algorithm would keep running in a loop.

2.3 Task 3

Heaps are commonly implemented with array, the positioning in the array determines the positioning in the tree, here's an example: [A, B, C, D, E, F] A has 2 leaves (B and C), B has 2 leaves (D and E), C has 1 leaf (F). Considering the lexicographical order this would be a min-heap since the children are always greater than the parent. Here's an implementation of min-heap and some of its main methods.

Pseudocode

```
1 Define class MinHeap
2     Define init()
3         Initialize heap field to an empty list
4
5     Define parent(i)
6         Return the index of the parent of the node at the i-th position
7
8     Define left_child(i)
9         Return the index of the left child of the node at the i-th position
10
11    Define right_child(i)
12        Return the index of the right child of the node at the i-th position
13
14    Define insert(value)
15        Append the new value at the end of the heap
16        Starting from the last element of the heap
17        While the element index is greater than 0 and the current element is
18            less than its parent
19            Swap the values of the current element and its parent
20
21    Define get_min()
22        If the heap has elements, then return the element of the heap field at
            index 0
        else return None
```

Code

```
1 class MinHeap:
2     def __init__(self):
3         self.heap = []
4
5     def parent(self, i):
6         return (i - 1) // 2
7
8     def left_child(self, i):
9         return 2 * i + 1
10
11    def right_child(self, i):
12        return 2 * i + 2
13
14    def insert(self, value):
15        self.heap.append(value)
16        i = len(self.heap) - 1
17        while i > 0 and self.heap[i] < self.heap[self.parent(i)]:
```

```
18         self.heap[i], self.heap[self.parent(i)] = self.heap[self.parent(i)
19             ], self.heap[i]
20         i = self.parent(i)
21     def get_min(self):
22         if len(self.heap) > 0:
23             return self.heap[0]
24         else:
25             return None
```

Which of the following statement(s) about the implementation above are **true**:

- ☐ The `parent` method is wrong, since it may return a non integer value.
- ☐ The while at line 18 stops as soon as the parent is greater than the child, but it should instead continue to verify that it is true throughout the whole hierarchy.
- ☐ The `get_min` method doesn't take into consideration lists with a negative number of values, it could break because of this.
- ☐ The `insert` method will break raising `IndexError:index out of range`.

2.4 Questions

Which of the following statement(s) are true:

- ☐ In a system where the free memory cells are sparse and not contiguous it's better to use a linked list rather than an array.
- ☐ Popping an item which is not the last element added to a stack is not the proper way to interact with a stack. But we can often do it since stacks are Abstract Data Types.
- ☐ The graph representations (edges list, adjacency list, adjacency matrix) have no effect on the efficiency of the algorithm we then implement on the graph. They are just a way for the developer to see the graph in a different manner.

3 Assignment 3

3.1 Task 1

In the following code the path from `start` to `end` is going to be searched with a depth-first algorithm. The `graph` passed to the function is an edge list, represented by a dictionary where the key is the vertex and its value is a list of the vertices it is connected to.

Pseudocode

```
1 Define dfs(graph, start, end)
2     Create the stack to track nodes and their paths
3     Put the start node in the stack with itself as the first node of the path
4     While there are values in the stack
5         Pop the stack, returning the starting node and the path
6         If the most recently extracted node is the end node, then return the
           path that was just returned
7         For every neighbour of the most recently returned node
8             If the neighbour is not in the path that was just returned, then
9                 append the neighbour node to the current path, and append the
                   node and the updated path to the top of the stack
10    Return None
```

Code

```
1 def dfs(graph, start, end):
2     stack = [(start, [start])]
3     while stack:
4         node, path = stack[-1]
5         del stack[-1]
6         if node == end:
7             return path
8         for neighbor in graph[node]:
9             if neighbor not in path:
10                 new_index = len(stack)
11                 stack[new_index] = (neighbor, path + [neighbor])
12    return None
```

Which of the following statement(s) about the implementation above are **true**:

- ☐ The pop at line 4 is not correctly implemented, we must use the `pop()` method instead. That code will prevent the correct popping.
- ☐ On line 4 and 5 we cannot return and delete the index `-1` since it will raise an `IndexError` not having the index `-1` in the list.
- ☐ On line 11 we cannot append to the list by using the index, we should use the `append()` method instead.
- ☐ This is not a depth-first search but a breadth-first search. In order to make it a DFS we should start from the bottom, which in this case is the `end` node.

3.2 Task 2

The following code implements a Breadth-First Search, it simply looks whether it is possible to reach the destination node starting from the source node.

Pseudocode

```
1 Define bfs(graph, start, target)
2     Create a set for the visited nodes
3     Create a queue with the start node
4     While there are nodes in the queue
5         Set the current node to the first node in the queue
6         If the current node is the target then return true
7         Add the current node to the visited set
8         For every neighbour of the current node
9             If the neighbour is not in the visited set add it to the queue
10    Return false
```

Code

```
1 def bfs(graph, start, target):
2     visited = set()
3     queue = [start]
4
5     while queue:
6         current_node = queue.pop(0)
7         if current_node == target:
8             return True
9
10        visited.add(current_node)
11
12        for neighbor in graph[current_node]:
13            if neighbor not in visited:
14                queue.append(neighbor)
15
16    return False
```

Which of the following statement(s) about the implementation above are **true**:

- ☐ The code will not work in case the graph is cyclical.
- ☐ The pop method does not have a parameter, it can just pop the last element.
- ☐ The method correctly implements a Breadth-First Search.
- ☐ The method would work only for directed graphs and not for undirected graphs.

3.3 Task 3

The code computes the shortest distance between the `start_id` node and any other node in the graph. The algorithm used is Dijkstra's algorithm.

Pseudocode

```
1 Define dijkstra(graph, start_id)
2     Create a distances dictionary, the values are the distance between the
      start_id node and the key (a node id)
3     Create a dictionary to store the parent of vertices found along the
      shortest path
4     Create a queue for vertices
5
6     For every vertex in the graph
7         Set its parent to -1
8         Add the node to the queue
9         Set the distance to infinity for all nodes, start_id distance set to 0
10
11
12     While there are values in the queue
13         Set the smallest known distance to infinity
14         Set the node the distance refers to, to the next smallest node in the
          queue (later called the current node)
15
16         The following for loop looks for the node with the shortest distance
          in the queue
17         For every node in the queue
18             If the distance between the start_id and the node is less than the
              smallest known distance, then set the current node to this
              node, together with its distance
19         Remove the current node from the queue
20
21         Now update the distances of the neighboring vertices passing by the
          current node
22         For every neighbour of the current node that is still in the queue
23             The distance from the neighbour to start_id passing by the current
              node is the distance of the current node from start_id + the
              distance of the current node and the neighbour
24             If this new distance is lower than the previous distance of the
              neighbour from start_id
25                 Then update the distance in the distances dictionary
26                 In the parents dictionary, set the current node as the current
                  neighbor parent
27
28     Return the distances and parent dictionaries
```

Code

```
1 def dijkstra(graph, start_id: int) -> Tuple[dict, dict]:
2     dist = {}
3     parent = {}
4     queue = []
5     for v in graph:
6         parent[v] = -1
```



```

7         queue.append(v)
8         dist[v] = float('inf') if v != start_id else 0
9
10        while queue:
11            u_val: float = float('inf')
12            u: Node = queue[0]
13            for q in queue:
14                u_val, u = (dist[q.id], q) if dist[q.id] > u_val else (u_val, u)
15            queue.remove(u)
16
17            children = [i for i in u.children if i in queue]
18            for v in children:
19                alt = v.weight
20                if alt < dist[v.id]:
21                    dist[v.id] = alt
22                    parent[v.id] = u.id
23        return dist, parent

```

Which of the following statement(s) about the implementation above are **true**:

- ☐ The ifs on line 8 and 14 are not a correct Python syntax.
- ☐ On line 14 a less than (<) should be used, since we want to get the node which distance is the shortest.
- ☐ On line 19, the new distance should be `dist[u.id] + v.weight` instead of only the last node weight (which is what we often call distance in this scenarios).
- ☐ This is a correct implementation of Dijkstra's algorithm.

3.4 Questions

Which of the following statement(s) are true:

- ☐ When looking for an element in a tree we must perform both a BFS and a DFS since the BFS will look for the items at the same level of the starting point and the DFS will look for the items on the branch starting from the starting point. Using only one of them may exclude some items from the search.
- ☐ Dijkstra's algorithm can find the shortest path only for acyclical graphs, if cycles are in the graph then we need to use A* that will instead follow its heuristic without being tricked into the cycles.
- ☐ Dijkstra's algorithm runs on an unweighted graph (every edge has the same weight), works just like a classic BFS search.