

# Arbitrary gage function intuition

Let  $\delta$  be an arbitrary gage function.

Our rescaled equation (ignoring coefficients) is:

In[83]:= **govEq** =  $-t^2 + t^5 - \epsilon^{1/3}$

Out[83]=  $-t^2 + t^5 - \epsilon^{1/3}$

In[84]:= **gage** = **Expand**[**Collect**[**Expand**[- $t^2 + t^5 - \epsilon^{1/3}$  /.  $t \rightarrow \{t_0 + \delta_1 * t_1\}$ ],  $\delta_1$ ]] /.  $t_0 \rightarrow 0$

Out[84]=  $\{-\epsilon^{1/3} - t_1^2 \delta_1^2 + t_1^5 \delta_1^5\}$

Considering the dominant terms and dividing by  $\delta_1^2$ :

In[88]:= **Expand**[ $(-\epsilon^{1/3} - t_1^2 \delta_1^2) / \delta_1^2$ ]

Out[88]=  $-t_1^2 - \frac{\epsilon^{1/3}}{\delta_1^2}$

Least degenerative case

$$\frac{\epsilon^{1/3}}{\delta_1^2} = 1$$

$$\delta_1 = \epsilon^{1/6}$$