General Equations

- KCL: $\sum I_{in} = \sum I_{Out} \rightarrow$ Node's Input Current = Node's Output Current
- KVL: $\sum V = 0 \rightarrow$ Voltage across a loop totals to 0.
- Ohm's Law: $V = IR$

Phasors

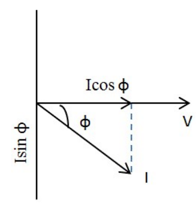
Phasors will only show us the steady state response of the circuit, not the transient response.
Eq: $v(t) = V_M \cos(\omega t + \theta) \leftrightarrow \bar{V} = V_M \angle \theta_v = V_M e^{\jmath \theta_v} = V_M (\cos\theta_v + \jmath \sin\theta_v)$
You can use phasors with Nodal Analysis, Mesh/Loop Analysis, Superposition, and Thevenin and Norton Equivalencies.

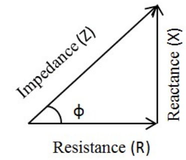
$z_1 = x_1 + \jmath y_2 = r_1 \angle \phi_1,\ z_2 = x_2 + \jmath y_2 = r_2 \angle \phi_2$

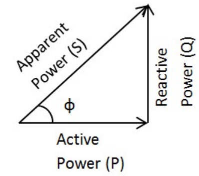
Addition	$z_1 + z_2 = (x_1 + x_2) + \jmath (y_1 + y_2)$
Subtraction	$z_1 - z_2 = (x_1 - x_2) + \jmath (y_1 - y_2)$
Multiplication	$z_1 z_2 = r_1 r_2 \angle (\phi_1 + \phi_2)$
Division	$\frac{z_1}{z_2} = \frac{r_1}{r_2} \angle (\phi_1 - \phi_2)$
Reciprocal	$\frac{1}{z_1} = \frac{1}{z_1} \angle - \phi_1$
Square Root	$\sqrt{z_1} = \sqrt{r_1} \angle \frac{\phi_1}{2}$
Complex Conjugate	$z_1^* = x - \jmath y = r \angle - \phi_1 = r e^{-\jmath \phi_1}$

RMS/Complex Power/Max Power Transfer

- $X_{rms} = \sqrt{\frac{1}{T} \int_0^T x(t)^2 dt}$
- $P_{avg} = \frac{1}{2} \mathrm{Re}\{\mathbf{VI}^*\} = \frac{1}{2} V_m I_m \cos(\theta_v - \theta_i)$
- $\mathbf{S} = I_{rms}^2 \mathbf{Z} = \frac{V_{rms}^2}{\mathbf{Z}^*} = \mathbf{V}_{rms} \mathbf{I}_{rms}^*$
- $\sum_{k=1}^{n} S_k$
- $C = \frac{Q_C}{\omega V_{rms}^2} = \frac{P(\tan\theta_1 - \tan\theta_2)}{\omega V_{rms}^2}$
- $L = \frac{V_{rms}^2}{\omega (Q_1 - Q_2)}$







Name	**Symbol**	**Equation(s)**	**Units**
Complex Power	$\mathbf{S}$	$\frac{P}{Pf} \angle \arccos(Pf) = P + \jmath Q = \mathbf{V}_{rms} \mathbf{I}_{rms}^* = \lvert\mathbf{V}_{rms}\rvert \lvert\mathbf{I}_{rms}\rvert \angle (\theta_v - \theta_i)$	VA
Apparent Power	S	$\lVert\mathbf{S}\rVert = \lvert\mathbf{V}_{rms}\rvert \lvert\mathbf{I}_{rms}\rvert = \sqrt{P^2 + Q^2}$	VA
Real Power	P	$\mathrm{Re}\{\mathbf{S}\} = S * Pf = S \cos(\theta_v - \theta_i)$	W
Reactive (Imaginary) Power	Q	$\mathrm{Im}\{\mathbf{S}\} = S \sin(\theta_v - \theta_i)$	VAR
Power Factor	Pf	$\frac{P}{S} = \cos(\theta_v - \theta_i)$	Lead/Lag

Elements

Relation	R	C	L
v-i i-v	$V = IR$ $I = \frac{V}{R}$	$v = \frac{1}{C} \int_{t_0}^{t} i(x)dx + v(t_0)$ $i = C \frac{dv}{dt}$	$v = L \frac{di}{dt}$ $i = \frac{1}{L} \int_{t_0}^{t} v(x)dx + i(t_0)$
P or W	$P = I^2 R = \frac{V^2}{R}$	$P = \frac{1}{2} C v_c^2$	$W = \frac{1}{2} L i_l^2$
Series Parallel	$R_{eq} = R_1 + R_2 + \ldots + R_n$ $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \ldots + \frac{1}{R_n}$	$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \ldots + \frac{1}{C_n}$ $C_{eq} = C_1 + C_2 + \ldots + C_n$	$L_{eq} = L_1 + L_2 + \ldots + L_n$ $\frac{1}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2} + \ldots + \frac{1}{L_n}$
@ Steady State	Same (Nothing Happens)	Open Circuit	Short Circuit
Phasors	$Z_R = R$	$Z_C = \frac{1}{j\omega C}$	$Z_L = j\omega L$

Methods to Solve Equations

Nodal Analysis

1. # of Nodes? $\rightarrow n$
2. Make one node the reference node. Assign $n-1$ nodal voltages
3. For a **voltage** source, write a CONSTRAINT EQUATION (Con. Eq.). If there is a voltage source between 2 non-reference nodes, make that a **SUPERNODE**.
4. Write KCL at each node. $(n-1)$ equations.
5. Solve Equations.

Mesh/Loop Analysis

1. # of Nodes? $\rightarrow n$ # of Branches? $\rightarrow b$ # of meshes/loops? $\rightarrow b-n+1=l$
2. Assign l loop currents.
3. For **current** sources, write a CONSTRAINT EQUATION (Con. Eq.). If there is a current source between 2 meshes, that's a **SUPERMESH**.
4. Write KVL for each mesh.
5. Solve Equations.

Superposition

- # of sources, n, determines the number of equations you will have.
- Shut off each source, one at a time, solving for the term that you want.
  - Voltage Source = S.C.
  - Current Source = O.C.
- Sum each of the individual terms together. $\sum_{i=1}^{n} x_i$
- **THIS IS THE ONLY WAY TO SOLVE FOR A CIRCUIT WITH MULTIPLE SOURCES!!**

Source Transformations

ALL source transformations obey Ohm's Law. $V = IR$. This will **ONLY** work on impedances in series with **VOLTAGE** sources, or impedances in parallel with **CURRENT** sources.

Thevenin and Norton Equivalencies

- ONLY independent sources - Zero all sources, find $\mathbf{Z}_{eq}$.
  - 0-ing Current Sources = O.C., 0-ing Voltage Sources = S.C.
  - Look at circuit from load's perspective for $\mathbf{Z}_{eq}$
  - $\mathbf{V}_{Th} = \mathbf{V}_{OC}$, $\mathbf{I}_N = \mathbf{I}_{SC}$
- BOTH dependent and independent sources
  - Find $\mathbf{V}_{Th} = \mathbf{V}_{OC}$, $\mathbf{I}_N = \mathbf{I}_{SC}$
  - Solve $\mathbf{Z}_{Th} = \frac{\mathbf{V}_{OC}}{\mathbf{I}_{SC}}$
- ONLY dependent sources
  - $\mathbf{V}_{Th} = 0$, $\mathbf{I}_N = 0$
  - $\mathbf{Z}_{Th} = \mathbf{Z}_N \rightarrow$ Attach test source @ load.
    * If voltage test source, find current. If current test source, find voltage
  - $\mathbf{Z}_{Th} = \frac{\mathbf{V}_{Test}}{\mathbf{I}_{Test}}$

Maximum Power Transfer - AC

- $\mathbf{Z}_{Load} = \mathbf{Z}_{Th}^{*}$, $R_{Th} = \mathrm{Re}\{\mathbf{Z_{Th}}\}$, $R_L = |\mathbf{Z}_{Th}| = \sqrt{R_{Th}^2 + (X_{Th} + X_L)^2}$
- $P_{max} = \frac{|\mathbf{V}_{Th}|^2}{8R_{Th}}$

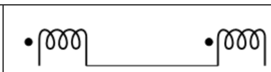
3-Phase Circuits

Δ-Y Conversion

You want to get everything into Y formation, because the common neutral allows you to do single-phase analysis.

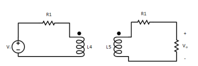
Mutual Inductance

Equivalent Mutual Inductance

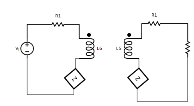
Series-**Aiding** Connection	$L = L_1 + L_2 + 2M$	
Series-**Opposing** Connection	$L = L_1 + L_2 - 2M$	

Solving Disjoint Coupled Circuits

1. Apply KVL
2. Don't forget about the Mutual Inductance Voltage Difference because of the first current
3. There is a second way to thing about these, shown in the Figure below.



(a) Original Circuit



(b) Circuit "Simplified" by Adding Dependent Sources

The sign on the dependent sources depends on which side of the inductor the current is going into. Use the Dot Convention to determine which direction the source's voltage should go.