

1 General Stuff

- Density - $\rho = \frac{\Delta m}{\Delta V}$
 - Uniform Density - $\rho = \frac{m}{V}$
- Pressure - $p = \frac{\Delta F}{\Delta A}$
 - Uniform Force on Flat Area - $p = \frac{F}{A}$
 - Conversions - $1atm = 1.01 \times 10^5 Pa = 760torr = 14.7lb/in^2$
- Trig Relations are in Trigonometric Formulas, Section 6.1.

2 Fluids

We must satisfy several parameters to make life easier, and to use most of these formulae.

1. Incompressible - Density of the fluid is constant
2. Non-turbulent Flow - Think of fluids swirling around an object
3. Isostatic Pressure - Pressure inside the fluid is the same in all directions

- Pressure at Some Depth - $p_2 = p_1 + \rho g (y_1 - y_2)$
 - Pressure at Depth $h \rightarrow p = p_0 + \rho gh$
- Pascal's Principle - 2 Parts
 1. $\vec{F}_o = \vec{F}_i \frac{A_o}{A_i}$
 2. $d_o = d_i \frac{A_i}{A_o}$
- Archimede's Principle - $\vec{F}_{Up} = \vec{F}_{Down}$
 - $\vec{F}_{Bouyant} = m_{Floating}g$
- Continuity - $A_1 v_1 = A_2 v_2$
- Bernoulli's Equation - $p_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1 = p_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2$
 - Fluids at Rest - $p_2 = p_1 + \rho g (y_1 - y_2)$
 - Fluids not Changing Height - $p_1 + \frac{1}{2}\rho v_1^2 = p_2 + \frac{1}{2}\rho v_2^2$

3 Waves

Usually of form $y = y_m \sin(kx \pm \omega t)$

- y_m - Amplitude, m
- k - Angular Wave Number, rad/m
 - $k = \frac{2\pi}{\lambda}$
 - λ is wavelength, m
- ω - Angular Frequency, rad/s
 - $\omega = 2\pi f$
 - f is frequency, Hz
 - Sign of this goes the opposite the direction the wave is going
 1. Wave going in positive direction (+), then the sign should be negative (-)
 2. Wave going in negative direction (-), then the sign should be positive (+)
- $v = \lambda f$, Wave Velocity, m/s
 - $v = \frac{\omega}{2\pi} * \frac{2\pi}{k} = \frac{\omega}{k}$

Wave Interference

Waves are nice, and they just sum when they interfere. Let:

$$y_1(x, t) = y \sin(kx - \omega t) \quad (3.1)$$

$$y_2(x, t) = y \sin(kx + \omega t + \varphi) \quad (3.2)$$

$$Y(x, t) = y [\sin(kx - \omega t) + \sin(kx + \omega t + \varphi)] \quad (3.3)$$

You can usually use Equation 6.1 to simplify Equation 3.3.

Constructive/Destructive Interference

$$\phi = 2\pi \frac{\text{PathLengthDiff}}{\lambda} = 2\pi \frac{\Delta d}{\lambda}$$
$$n = \frac{2}{\pi} \phi = 4 \frac{\text{PathLengthDiff}}{\lambda}$$

- *PathLengthDiff* - Is the Difference in path lengths that the waves must travel
- *phi* - Angular Location of points of Complete Constructive/Destructive Interference
- *n* - Number of locations where there is Complete Constructive/Destructive Interference

Standing Waves

This is actually the superposition of 2 waves, traveling in opposite directions, on a medium that is fixed at both ends, i.e. a taut string held by a wall.

Location of Nodes and Antinodes

- Nodes - $x = n\frac{\lambda}{2}$ for $n = 0, 1, 2, \dots$
- Antinodes - $x = (n + \frac{1}{2})\frac{\lambda}{2}$ for $n = 0, 1, 2, \dots$

Resonant Frequencies/Harmonics

These can also be called harmonics. There is a resonant frequency for every number of nodes/antinodes on the standing wave.

$$f = \frac{v}{\lambda} = n \frac{v}{2L}$$

- L is the length of the medium (The String).
- λ is the wavelength of the wave formed.

This can be extended to find the base resonant frequency, if you know how many node levels are between the two resonant frequencies given, i.e. they say that the **NEXT** frequency, means $n + 1$.

$$f_{n+m} - f_n = (n+m) \frac{v}{2L} - n \frac{v}{2L} = m \frac{v}{2L}$$

Reflecting Sound

- $D = (n + 1) d = vt$
 - n is the number of reflections that occurred

Doppler Effect

$$f' = f \frac{v \pm v_D}{v \pm v_S}$$

- Moving **TOWARDS** each other: Frequency Increase
- Moving **AWAY** from each other: Frequency Decrease
- f - Initial Frequency, Hz
- v - Sound Speed, m/s
- v_D - Detector Speed, m/s
- v_S - Source Speed, m/s
- **For Numerator:**
 - If detector is moving towards the source, +
 - If detector is moving away from the source, –
- **For Denominator:**
 - If source is moving away from detector, +
 - If source is moving towards the detector, –

4 Thermodynamics

Definition: Study of energy transfer between two macroscopic bodies driven by temperature differences.

Laws of Thermodynamics

0th Law: If 2 bodies, A and B are in thermal equilibrium with a third body "T", then they are in thermal equilibrium with each other

1st Law: $dE_{Internal} = dQ - dT \leftarrow dQ$ and dT are inexact (path-dependent) differentials

Special Cases for the 1st Law of Thermodynamics:

- (a) Adiabatic Processes - $dE_{Int} = -dW$
 - No heat exchange
 - Insulating
 - Something happens too quickly for system to keep up
- (b) Isothermal Processes - $dT = 0 \rightarrow dE_{Int} = 0 \rightarrow dQ = dW$
- (c) Isobaric Processes - $dW = p dV$, p (pressure) is constant
- (d) Cyclical Processes - $dE_{Int} = 0 \rightarrow dQ = dW$
 - You end a cycle with the same internal energy when the cycle started

Heat and Work

- $dW = \vec{F} ds$
- $\vec{F} = p(V, T) dV$
- $W = \int p(V, T) dV$
- $W = \frac{dQ}{dt}$
- $W = \frac{\Delta Q}{\Delta t}$

Thermal Expansion

Occurs because the "springs" between each of the atoms in a lattice have energy applied by Heat (Temperature Change).

- $\frac{\Delta L}{L_0} = \alpha \Delta T$ (One-Dimensional Expansion)
- $\frac{dL}{L_0} = \alpha dT$ (One-Dimensional Expansion)
 - α is a material-specific constant

Specific Heat/Heat Capacity

- $C = \frac{dQ}{dT} \leftarrow$ Specific Heat
- $c = \frac{dQ}{m dT} \leftarrow$ Mass Specific Heat

Heat of Phase Transitions

This is a constant unique to the material and the phase transition it is going through.

- $Q = Lm$
- $Q = \int_{m_i}^{m_f} L_f dm$
- l_{Fusion} = Heat required to turn things from **SOLID TO LIQUID**
- l_{Vapor} = Heat required to turn things from **LIQUID TO GAS**

Conduction Heat Transfer

- $P_{Conduction} = \frac{(T_H - T_C)}{L} Ak$
 - L = Length
 - A = Cross-Sectional Area
 - k = Material's Thermal Conductivity

For multiple materials between 2 thermal reservoirs:

- $P_1 = P_2 = \dots = P_n$
- Heat will only flow as fast as the slowest thermal conductor

5 Quantum Mechanics

6 Reference Material

6.1 Trigonometric Formulas

$$\sin(\alpha) + \sin(\beta) = 2 \sin\left(\frac{\alpha + \beta}{2}\right) \cos\left(\frac{\alpha - \beta}{2}\right) \quad (6.1)$$