EDAN65: Compilers - Reference Sheet

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1 Introduction

There are numerous steps in the compilation process of a standard program. Each phase converts the program from one representation to another.

- 1. Lexical Analysis/Scanning
- 2. Syntactic Analysis (Parsing)
- 3. Semantic Analysis
- 4. Intermediate Code Generation
- 5. Optimization
- 6. Target Code Generation

Defn 1 (Syntactic Analysis (Parsing)). Syntactic Analysis or Parsing is the process where tokens are input and an AST (Abstract Syntax Tree) is created. This AST is generated based on the input source code and the Lexical Analysis (Scanning) that occurs.

This code would generate an error during the Syntactic Analysis (Parsing).

```
int r( {
    return 3;
}
```

This wouldn't fail during Lexical Analysis (Scanning) because the scanner doesn't care that the parentheses don't match. All that it cares about is that there are parentheses that it needs to mark. During the Syntactic Analysis (Parsing) we find out that the syntax would be wrong. This would happen because we can't line our tokens up correctly in our AST.

Remark 1.1. Syntactic Analysis (Parsing) ONLY handles the reading in of tokens and creating an Abstract Syntax Tree. It DOES NOT attach any meaning to anything. Therefore, this does not return an error during Syntactic Analysis (Parsing).

```
integer q() {
return 3;
}
```

However, it does return an error during Semantic Analysis.

Defn 2 (Semantic Analysis). Semantic Analysis is the phase of the compilation process that takes the AST (Abstract Syntax Tree) and attaches some semblance of meaning to the tokens in the tree. We determine what each "phrase" means, relate the uses of variables to their definitions, check types of expressions, and request translations of each "phrase". This is the point in the compilation process where the strings that were read in by the scanner and organized by the parser have any meaning. Before this, the only things that can be caught are token errors, and the like. So, this will generate an error that is caught during Semantic Analysis.

```
integer q() {
    return 3;
}
```

Because integer isn't a valid keyword in the Java language, at least not by default, and not capitalized like that, it gets caught during Semantic Analysis.

This would also generate an error during Semantic Analysis.

```
int p(int x) {
    int y;
    y = x * 2;
}
```

Both of these wouldn't be caught before the Semantic Analysis because the tokens read in during Lexical Analysis (Scanning) and organized during Syntactic Analysis (Parsing) do not have any meaning any earlier.

2 Lexical Analysis/Scanning

Defn 3 (Lexical Analysis (Scanning)). Lexical Analysis or Scanning is the phase of the compilation process that reads in the source code text. It breaks the things it reads into tokens.

Remark 3.1. Lexical Analysis (Scanning) ONLY handles the reading IN of source code and the outputting of tokens. It DOES NOT attach any meaning or put anything together.

This means that these are the **ONLY** types of errors that will be caught.

```
int #s() {
    return 3;
}
```

Because the # token isn't understood by the scanner, the whole thing fails. The Scanner is just a simple look up device. It can only find things that it knows about. If it sees something that it has no clue about, it fails.

There are several ways to implement a scanner. One of the most common ways is the use of a Finite State Automaton or Finite State Machine.

2.1 Finite State Automata

Finite state automata are used for regular expressions (regex's) to determine a matching word.

Defn 4 (Finite State Automaton). A *finite state automaton* or *finite state machine* is a mathematical model of computation. It is an abstract machine that can be in exactly one of a finite number of states at any given time. The FSM can change from one state to another in response to some external inputs; the change from one state to another is called a transition. An FSM is defined by a list of its states, its initial state, and the conditions for each transition.

There are 2 types of finite statue automata:

- 1. Deterministic Finite Automata (DFA)
- 2. Non-deterministic Finite Automata (NFA)

A deterministic finite state automata can be constructed to be equivalent to any non-deterministic one.

Remark 4.1. The plural of Finite State Automaton is Finite State Automata.

Defn 5 (Deterministic Finite Automata (DFA)). In a deterministic finite automaton, no two edges leaving from the same state are labeled with the same symbol. Additionally, there cannot be an edge that matches the empty string, ϵ . A deterministic finite automaton will eventually terminate when it steps through all of its states necessary to reach the accepting state. However, the key difference between a Deterministic Finite Automata (DFA) and a Non-deterministic Finite Automata (NFA) is that you can always figure out the path that a deterministic finite automaton will take.

Defn 6 (Non-deterministic Finite Automata (NFA)). A non-deterministic finite automaton is one that has multiple edges leaving a single state that have the same symbol. It may also have special edges labeled with the empty string ϵ , which is when a state is followed without "eating" any of the input string. A non-deterministic finite automaton may eventually terminate when it steps through all its states necessary to reach its accepting state. However, the key difference between a Non-deterministic Finite Automata (NFA) and a Deterministic Finite Automata (DFA) is that you can always figure out the path that a deterministic finite automaton will take.

2.1.1 Converting a NFA to a DFA

There are a few steps for converting a non-deterministic finite automaton to a deterministic one.

- 1. Start at the start state and enter it
- 2. Follow all the states that accept the empty string ϵ and combine them with the start state.
- 3. After that, read in the first character/word from the input and follow all the states that you combined.
 - This means that you will be following multiple states or edges at the same time.
- 4. Continue doing this until you combine all the states down to a deterministic finite automaton.
 - You can have multiple instances of the same state, i.e., you can have state 5 in two different state bubbles, so long as the list of states inside is unique.
- 5. The end states are found by taking the end states from the non-deterministic finite automaton and placing them in the deterministic finite automaton.
 - This means that if state 3 is and end state in the non-deterministic finite automaton, then every occurrence of state 3 in the deterministic finite automaton will be and end state.

3 Syntactic Analysis/Parsing

There are 2 kinds of parsing techniques:

- 1. LL Parsing
- 2. LR Parsing

The table below will help characterize the differences between them.

	LL(k)	LR(k)		
Parses Input	Left-to-Right			
Derivation	Leftmost	Rightmost		
Lookahead	k Symbols			
Build the Tree	Top Down	Bottom Up		
Select Rule	After seeing its first k tokens	After seeing all its tokens, and an addition k tokens		
Left Recursion	No	Yes		
Unlimited Common Prefix	No	Yes		
Resolve Ambiguities Through Rule Priority	Dangling Else	Dangling Else, Associativity, Priority		
Error Recovery	Trial-and-Error	Good Algorithms Exist		
Implement by Hand?	Possible	Too complicated. Use a generator.		

Table 3.1: LL vs. LR Parsing

3.1 LL Parsing

There are 5 basic steps in constructing an LL(1) parser.

- 1. Write the grammar in canonical form.
- 2. Compute Nullable, FIRST, and FOLLOW.
- 3. Use them to contruct a table. It shows what production to select given the current lookahead token.
- 4. Check for conflicts.
 - (a) If there are conflicts, then the grammar is not LL(1).
 - (b) If there are *no* conflicts, then there is a straight-forward implementation using table-driven parser or recursive descent.

Many times, you will encounter Fixed-Point Problems.

Defn 7 (Fixed-Point Problems). Fixed-point problems have the form:

$$x == f(x) \tag{3.1}$$

Can we find a value x for which the equation holds (i.e., a solution)? x is then called the *fixed point* of the function f(x). Fixed-Point Problems can (sometimes) be solved using iteration. The steps involved in *fixed-point iteration* are:

- 1. Guess an initial value x_0
- 2. Apply the function iteratively
- 3. Iterate until the fixed point is reached.

$$x_1 = f(x_0)$$

$$x_2 = f(x_1)$$

$$\vdots$$

$$x_n = f(x_{n-1})$$

You continue this iteration until $x_n = x_{n-1}$, and x_n is called the *fixed point*.

3.1.1 Nullable

Defn 8 (Nullable). For the production p, where $p: X \to \gamma$, and X and γ are nonterminals; p is Nullable if we can derive ϵ from γ .

More formally, this can be defined as $Nullable(\gamma)$ is true iff the empty sequence can be derived from γ :

$$Nullable(\gamma) = \begin{cases} True, & \exists (\gamma \Rightarrow * \epsilon) \\ False, & Otherwise \end{cases}$$

You can define an equation system for Nullable given that G = (N, T, P, S).

$$Nullable(\epsilon) == True \tag{3.2a}$$

$$Nullable(t) = False (3.2b)$$

where $t \in T$, i.e., t is a terminal symbol

$$Nullable(X) = Nullable(\gamma_1) \parallel \dots \parallel Nullable(\gamma_n)$$
(3.2c)

where $X \to \gamma_1, \dots, X \to \gamma_n$ are all the productions for X in P.

$$Nullable(s\gamma) = Nullable(s) \&\& Nullable(\gamma)$$
(3.2d)

where $s \in N \cup T$, i.e., s is a nonterminal or a terminal

Remark 8.1. The equations (3.2a) to (3.2d)) for Nullable are recursive. Therefore, you can't just calculate these recursively, because you might never terminate if the empty sequence is never reached. This is one set of Fixed-Point Problems.

3.1.2 FIRST

Defn 9 (FIRST). For the production p, where $p: X \to \gamma$, and X and γ are nonterminals. The FIRST(γ) are the tokens that occur FIRST in a sentence derived from γ .

More formally, this can be defined as: $FIRST(\gamma)$ is the set of tokens that can occur first in the sentences derived from γ .

$$FIRST(\gamma) = \{t \in T | \gamma \Rightarrow *t\delta\}$$

You can define an equation system for FIRST given that G = (N, T, P, S).

$$FIRST(\epsilon) = \emptyset \tag{3.3a}$$

$$FIRST(t) = \{t\} \tag{3.3b}$$

where $t \in T$, i.e., t is a terminal symbol

$$FIRST(X) = FIRST(\gamma_1) \cup \ldots \cup FIRST(\gamma_n)$$
(3.3c)

where $X \to \gamma_1, \dots, X \to \gamma_n$ are all the productions for X in P.

$$FIRST(s\gamma) = FIRST(s) \cup (if Nullable(s) then FIRST(\gamma) else \emptyset fi)$$
 (3.3d)

where $s \in N \cup T$, i.e., s is a nonterminal or a terminal

Remark 9.1. The equations (Equations (3.3a) to (3.3d)) for FIRST are recursive. Therefore, they might not terminate, so you must calculate this as another set of Fixed-Point Problems.

3.1.3 FOLLOW

Defn 10 (FOLLOW). For the production p, where $p: X \to \gamma$, and X and γ are nonterminals. The FOLLOW(X) are the tokens that FOLLOW immediately after an X-sentence.

More formally, this can be defined as: FOLLOW(X) is the set of tokens that can occur as the *first* token *following* X, in any Sentential Form derived from the start symbol S:

$$FOLLOW(X) = \{t \in T | S \Rightarrow \alpha X t \beta\}$$

The nonterminal X occurs on the right-hand side of a number of productions.

Let $Y \to \gamma X \delta$ denote such an occurrence, where γ and δ are arbitrary sequences of terminals and nonterminals. You can define an equation system for FOLLOW given that G = (N, T, P, S).

$$FOLLOW(X) = \bigcup FOLLOW(Y \to \gamma \underline{X} \delta)$$
 (3.4a)

over all occurrences $Y \to \gamma X \delta$, and where

$$FOLLOW(Y \to \gamma \underline{X}\delta) = FIRST(\delta) \cup (if Nullable(\delta) then FOLLOW(Y) else \emptyset fi)$$
(3.4b)

Remark 10.1. Again, the equations (Equations (3.4a) to (3.4b)) are recursive. Therefore, they might not terminate, so you must calculate this as another set of Fixed-Point Problems.

Remark 10.2 (Sentential Form). Sequence of terminal and nonterminal symbols.

One way to think about solving a problem asking about FOLLOW is shown below. I will use this grammar to demonstrate:

$$S \to Xa$$

$$X \to Y|Yb$$

$$Y \to YZc|\epsilon$$

$$Z \to d|\epsilon$$

- 1. Determine the nonterminal you are interested in, let's say Y.
- 2. Find all occurrences of that nonterminal on the *RIGHT-HAND SIDE* of the productions. In this case our nonterminal occurs in:
 - Production 2
 - Production 3
- 3. Find the nonterminals that can directly follow your nonterminal.
 - \bullet b, from Production 2
 - c, from Production 3
- 4. If there are nonterminals after the nonterminal you are interested in, follow them. In this case, we follow Z. Then, find the nonterminals that can directly follow that nonterminal and add them to you're list.
 - b, from Production 2
 - c, from Production 3
 - d, from Production 4
- 5. If no token follows the nonterminal you want, then go "backwards" through the production.
 - (a) Since Production 2 has $X \to Y$ as an option and nothing follows this Y
 - (b) Go backwards, up to the production(s) that produces X on the right-hand side
 - (c) Compute Follow on the right-hand side of that production. This produces:
 - a, from Production 1

This leaves us with our FOLLOW(Y) set: $\{a, b, c, d\}$, which is the solution.

3.1.4 Constructing an LL(1) Table

Using the information that was gathered from the Nullable, FIRST, and FOLLOW calculations, you can construct an LL(1) parse table with the following steps.

- 1. Look at each production $p: X \to \gamma$.
- 2. Compute the token set FIRST(γ). Add p to each corresponding entry for X.
- 3. Check if γ is Nullable.
 - (a) If so, compute the token set FOLLOW(X), and add p to each corresponding entry for X.
- **3.1.4.1 LL**(1) **Parse Table Conflicts** For every case where an LL(1) grammar fails, it can be illustrated by the parse table for the grammer. The table for any of these grammars with have a *conflict* in one of its cells, as shows when there are multiple productions in the cell. Some of the cases where this may happen are listed below:
 - 1. Ambiguous Grammar
 - 2. Left-Recursive
 - 3. Common Prefix

3.1.5 Eliminating Left Recursion

LL(1) cannot support left recursion, however, they can support right recursion. So, if we have a grammar with left recursion, and want to LL(1) parse it, we need to rewrite the grammar. We can introduce a new nonterminal, which allows us to recurse on the right side of the production, but not the left.

3.2 LR Parsing

LR(k) parsing stands for Left-to-right parse, rightmost-derivation, k-token lookahead. This parsing technique postpones the decision of which production to use until it sees the entire right-hand side of the production in question (and k more tokens beyond).

An LR parser has a stack and and input. The first k tokens of the input are the lookahead. Based on the contents of the stack and the lookahead, the parser performs 1 of 2 actions.

- 1. Shift
- 2. Reduce

Defn 11 (Shift). A *shift* operation corresponds to moving the first input token onto the top of the stack. This is equivalent to reading the token and moving it onto the stack, and advancing forward through the sentence.

Remark 11.1 (Accepting). Shifting over the EOF (End of File) marker, typically denoted \$, is called accepting and causes the parser to stop successfully.

Defn 12 (Reduce). A reduce operation corresponds to choosing a grammar rule $X \to ABC$; pop C, B, A off the top of the stack, and push X onto the stack.

Initially, the stack is empty and the parser is sitting at the beginning of the input.

In practice, k > 1 is not used. These would generate incredibly large tables that would be hard to used and hard to make. Most reasonable programming languages can be described by LR(1) grammars.

3.2.1 LR Finite State Automata

These automata are Deterministic Finite Automata (DFA). They are used in the parser to decide when to Shift and when to Reduce, and are applied to the stack.

They can be used to generate an LR Parse Table.

Each of the states consists of one ore more LR Items.

Defn 13 (LR Item). The parser uses a Deterministic Finite Automata (DFA) to decide whether to shift or reduce the expression that is has seen so far. The *states* in the DFA are sets of *LR Items*.

An example of an LR Item is shown in Equation (3.5).

$$X \to \alpha \bullet \beta \quad t, s$$
 (3.5)

An LR(1) item is a production extended with:

- A dot (•), corresponding to the position in the input sentence.
- One or more possible lookahead terminal symbols: t, s.
 - We will use? when the lookahead doesn't matter.

Remark 13.1. The stack that is referenced in this section is left side of the dot that is present in LR Items.

The LR(1) item corresponds to a state where (using Equation (3.5)):

- The topmost part of the stack is α
- The first part of the remaining input is expected to match either, in no particular order:
 - $-\beta t$
 - $-\beta s$

3.2.2 LR Parse Table

This table is generated after making an LR Finite State Automata. To make one, there are 4 actions to note in the table.

- 1. Shift Actions
- 2. Reduce Actions
- 3. Goto Actions
- 4. Accept Action
- 5. Errors are denoted by blank entries in the table.

- **3.2.2.1 Shift Actions** These are found by reading TOKENS. For each token edge, t, from state j to state k, add a **shift action** sk to table [j,t]. (This corresponds to reading a token and pushing it onto the stack.)
- **3.2.2.2 Reduce Actions** These are found when the **dot is at the end**. Add a *reduce action* $\mathbf{r}p$ (reduce p) to table [j, t], where p is the production and t is the lookahead token. (This corresponds to popping the right-hand side of a production off the stack and going backwards through the state machine.)
- **3.2.2.3** Goto Actions These are found by reading a **NONTERMINAL**. For each nonterminal edge, X, from state j to state k, add a **Goto** Action gk (goto state k) to table [j, X]. (This corresponds to pushing the left-hand side of a nonterminal production onto the stack.)
- **3.2.2.4** Accept Action These are found when in a state containing an LR item with your **dot on the left of \$**. If this is so, then add an *accept action* a to the table with indices table [j, \$]. (If we are about to perform a shift action over the EOF (End Of File) token, \$, then parsing has succeeded.)

3.2.3 LALR(1) Parsing Tables

Since LR(1) tables can get quite large, a smaller table can be made by merging any 2 states whose items are identical except for lookahead sets. The resulting parser is called a *Lookahead LR*(1) parser. For example, compare the same states, but different parser types as shown in Table 3.2a and Table 3.2b.

Productions	Lookahead Token		
$S' \to \bullet S$ \$?	Productions	Lookahead Token
$S \to \bullet V = E$	\$	$S' \to \bullet S$ \$?
S o ullet E	\$	$S \to \bullet V = E$	\$
E o ullet V	\$	$S \to ullet E$	\$
V o ullet x	\$	E o ullet V	\$
$V \to ullet *E$	\$	V o ullet x	\$,=
$V \to ullet x$	=	$V \to \bullet *E$	\$,=
$V \to \bullet * E$	=	(b) LALI	R(1) Table State

(a) LR(1) Table State

Table 3.2: LR(1) Table State vs LALR(1) Table State

3.2.4 Syntax Versus Semantics

There are some things that context-free grammars cannot describe, and thus cannot be parsed correctly. For instance, the expression

$$a + 5 \&\& b$$

The precedence here has the mathematical addition in greater priority than the logical AND operator. But logical and mathematical operators are not allowed in the same expression, because the types of the variables and operations don't make sense together. However, the context-free grammar and parser have no knowledge of the *types* of the variables and operators in play here. So, the solution is to let this expression pass through the parser, but it should be caught later, during the Semantic Analysis.

4 Semantic Analysis