# Inferring Types and Effects via Static Single Assignment

Leonardo Rigon, Paulo Torrens, Cristiano Vasconcellos

Department of Computer Science Santa Catarina State University

SAC - 2020/03/24



- While we could argue that functional languages are based on expressions, imperative languages make a syntactic distinction between expressions and statements
  - Expressions are, statements do
  - Even impure functional languages that support loops and sequencing treat those as expressions (e.g., OCaml, Scheme)
- Most functional languages will offer some features to write more imperative-like code, but may still miss some features such as early return and arbitrary control flow
- Given an algorithm capable of translating statements into equivalent expressions, it should be possible to use control structures in a functional language
  - This algorithm exists: the algorithm for turning structured code into SSA



- While we could argue that functional languages are based on expressions, imperative languages make a syntactic distinction between expressions and statements
  - Expressions are, statements do
  - Even impure functional languages that support loops and sequencing treat those as expressions (e.g., OCaml, Scheme)
- Most functional languages will offer some features to write more imperative-like code, but may still miss some features such as early return and arbitrary control flow
- Given an algorithm capable of translating statements into equivalent expressions, it should be possible to use control structures in a functional language
  - This algorithm exists: the algorithm for turning structured code into SSA



- While we could argue that functional languages are based on expressions, imperative languages make a syntactic distinction between expressions and statements
  - Expressions are, statements do
  - Even impure functional languages that support loops and sequencing treat those as expressions (e.g., OCaml, Scheme)
- Most functional languages will offer some features to write more imperative-like code, but may still miss some features such as early return and arbitrary control flow
- Given an algorithm capable of translating statements into equivalent expressions, it should be possible to use control structures in a functional language
  - This algorithm exists: the algorithm for turning structured code into SSA



- While we could argue that functional languages are based on expressions, imperative languages make a syntactic distinction between expressions and statements
  - Expressions are, statements do
  - Even impure functional languages that support loops and sequencing treat those as expressions (e.g., OCaml, Scheme)
- Most functional languages will offer some features to write more imperative-like code, but may still miss some features such as early return and arbitrary control flow
- Given an algorithm capable of translating statements into equivalent expressions, it should be possible to use control structures in a functional language
  - This algorithm exists: the algorithm for turning structured code into SSA



- While we could argue that functional languages are based on expressions, imperative languages make a syntactic distinction between expressions and statements
  - Expressions are, statements do
  - Even impure functional languages that support loops and sequencing treat those as expressions (e.g., OCaml, Scheme)
- Most functional languages will offer some features to write more imperative-like code, but may still miss some features such as early return and arbitrary control flow
- Given an algorithm capable of translating statements into equivalent expressions, it should be possible to use control structures in a functional language
  - This algorithm exists: the algorithm for turning structured code into SSA



- While we could argue that functional languages are based on expressions, imperative languages make a syntactic distinction between expressions and statements
  - Expressions are, statements do
  - Even impure functional languages that support loops and sequencing treat those as expressions (e.g., OCaml, Scheme)
- Most functional languages will offer some features to write more imperative-like code, but may still miss some features such as early return and arbitrary control flow
- Given an algorithm capable of translating statements into equivalent expressions, it should be possible to use control structures in a functional language
  - This algorithm exists: the algorithm for turning structured code into SSA



- SSA is a common form used by intermediate languages for imperative programs, introduced by Cytron et al.
- Source programs are split into basic blocks, a basic unit of flow composed of atomic operations (e.g., assignments) that are necessarily sequential
- Each assignment to a local variable makes a new copy of it, and, upon control flow, phi functions are inserted to chose the live version of a variable
- SSA is a functional form described by a graph: blocks are mutually recursive abstractions, phi functions are parameters, and dominance information describes the lexical scope

- SSA is a common form used by intermediate languages for imperative programs, introduced by Cytron et al.
- Source programs are split into basic blocks, a basic unit of flow composed of atomic operations (e.g., assignments) that are necessarily sequential
- Each assignment to a local variable makes a new copy of it, and, upon control flow, phi functions are inserted to chose the live version of a variable
- SSA is a functional form described by a graph: blocks are mutually recursive abstractions, phi functions are parameters, and dominance information describes the lexical scope

- SSA is a common form used by intermediate languages for imperative programs, introduced by Cytron et al.
- Source programs are split into basic blocks, a basic unit of flow composed of atomic operations (e.g., assignments) that are necessarily sequential
- Each assignment to a local variable makes a new copy of it, and, upon control flow, phi functions are inserted to chose the live version of a variable
- SSA is a functional form described by a graph: blocks are mutually recursive abstractions, phi functions are parameters, and dominance information describes the lexical scope

- SSA is a common form used by intermediate languages for imperative programs, introduced by Cytron et al.
- Source programs are split into basic blocks, a basic unit of flow composed of atomic operations (e.g., assignments) that are necessarily sequential
- Each assignment to a local variable makes a new copy of it, and, upon control flow, phi functions are inserted to chose the live version of a variable
- SSA is a functional form described by a graph: blocks are mutually recursive abstractions, phi functions are parameters, and dominance information describes the lexical scope

```
algorithm fib(var n) {
 var a = 0;
 var b = 1;
 for(var i = 0; i < n; i++) {
   var c = b;
   b = a + b;
   a = c;
 return a:
```



```
algorithm fib(var n) {
                                                       proc fib(n<sub>1</sub>) {
  var a = 0;
                                                            goto L1;
  var b = 1;
                                                       L1: a_1 \leftarrow 0;
 for(var i = 0; i < n; i++) {
                                                           b_1 \leftarrow 1;
     var c = b:
                                                           goto L2;
     b = a + b;
                                                      L2: i_1 \leftarrow 0;
     a = c;
                                                           goto L3:
                                                       L3: a_2 \leftarrow \phi(L2: a_1, L5: a_3);
  return a:
                                                           b_2 \leftarrow \phi(L2: b_1, L5: b_3);
                                                           i_2 \leftarrow \phi(L2: i_1, L5: i_3);
                                                           if i_2 < n_1 then
                                                                 goto L4
                                                            else
                                                                 goto L6;
                                                       L4: c_1 \leftarrow b_2:
                                                           b_3 \leftarrow a_2 + b_2;
                                                           a_3 \leftarrow c_1;
                                                           goto L5;
                                                      L5: i_3 \leftarrow i_2 + 1;
                                                           goto L3;
                                                       L6: return a2
```



```
algorithm fib(var n) {
                                                           proc fib(n<sub>1</sub>) {
   var a = 0:
                                                                 goto L1;
   var b = 1;
                                                           L1: a_1 \leftarrow 0;
  for(var i = 0; i < n; i++) {
                                                                 b_1 \leftarrow 1;
      var c = b:
                                                                goto L2;
      b = a + b:
                                                           L2: i_1 \leftarrow 0;
      a = c;
                                                                 goto L3:
                                                           L3: a_2 \leftarrow \phi(L2: a_1, L5: a_3);
   return a:
                                                                 b_2 \leftarrow \phi(L2: b_1, L5: b_3);
                                                                i_2 \leftarrow \phi(L2: i_1, L5: i_3);
      L1:
                                                                if i_2 < n_1 then
         a_1 \leftarrow 0
                                                                      goto L4
                                                                 else
         b_1 \leftarrow 1
                                                                      goto L6;
                                                           L4: c_1 \leftarrow b_2:
      L2: •
                                 L5:
                                                                b_3 \leftarrow a_2 + b_2;
                                                                 a_3 \leftarrow c_1;
         i_1 \leftarrow 0
                                     i_3 \leftarrow i_2 + 1
                                                                 goto L5;
                                                           L5: i_3 \leftarrow i_2 + 1;
                                                                 goto L3;
                                 L4:
                                                           L6: return a2
L3: φa<sub>2</sub>.φb<sub>2</sub>.φi<sub>2</sub>.
                                  c_1 \leftarrow \, b_2
                                  b_3 \leftarrow a_2 + b_2
       (i_2 < n_1)?
                                  a_3 + c_1
L6:
       return a2
```



```
algorithm fib(var n) {
                                                           proc fib(n<sub>1</sub>) {
   var a = 0:
                                                                 goto L1;
   var b = 1;
                                                           L1: a_1 \leftarrow 0;
  for(var i = 0; i < n; i++) {
                                                                 b_1 \leftarrow 1;
      var c = b:
                                                                goto L2;
      b = a + b:
                                                           L2: i_1 \leftarrow 0:
      a = c;
                                                                 goto L3:
                                                           L3: a_2 \leftarrow \phi(L2: a_1, L5: a_3);
   return a:
                                                                 b_2 \leftarrow \phi(L2: b_1, L5: b_3);
                                                                i_2 \leftarrow \phi(L2: i_1, L5: i_3);
      L1:
                                                                if i_2 < n_1 then
         a_1 \leftarrow 0
                                                                      goto L4
                                                                 else
         b_1 \leftarrow 1
                                                                      goto L6;
                                                           L4: c_1 \leftarrow b_2:
      L2: •
                                  L5:
                                                                b_3 \leftarrow a_2 + b_2;
                                                                 a_3 \leftarrow c_1;
         i_1 \leftarrow 0
                                     i_3 \leftarrow i_2 + 1
                                                                 goto L5;
                                                           L5: i_3 \leftarrow i_2 + 1;
                                                                 goto L3;
                                 L4:
                                                           L6: return a2
L3: λa<sub>2</sub>.λb<sub>2</sub>.λi<sub>2</sub>.
                                  c_1 \leftarrow \, b_2
                                  b_3 \leftarrow a_2 + b_2
       (i_2 < n_1)?
                                  a_3 + c_1
L6:
       return a2
```



- As it's possible to apply a syntactic translation from the SSA form to the lambda calculus, it's possible to use control flow statements in a functional setting
- If we consider a source language with just local assignment and local control flow (including goto), the resulting lambda term remains purely functional
  - As the SSA algorithm removes local mutability and control flow, these should not be viewed as computational effects, but rather as "syntactic sugar"
- Could a type and effect system, such as the one used by Koka, be used on the resulting term? If so, such a language could use restricted side effects akin to an imperative language

- As it's possible to apply a syntactic translation from the SSA form to the lambda calculus, it's possible to use control flow statements in a functional setting
- If we consider a source language with just local assignment and local control flow (including goto), the resulting lambda term remains *purely functional* 
  - As the SSA algorithm removes local mutability and control flow, these should not be viewed as computational effects, but rather as "syntactic sugar"
- Could a type and effect system, such as the one used by Koka, be used on the resulting term? If so, such a language could use restricted side effects akin to an imperative language

- As it's possible to apply a syntactic translation from the SSA form to the lambda calculus, it's possible to use control flow statements in a functional setting
- If we consider a source language with just local assignment and local control flow (including goto), the resulting lambda term remains *purely functional* 
  - As the SSA algorithm removes local mutability and control flow, these should not be viewed as computational effects, but rather as "syntactic sugar"
- Could a type and effect system, such as the one used by Koka, be used on the resulting term? If so, such a language could use restricted side effects akin to an imperative language

- As it's possible to apply a syntactic translation from the SSA form to the lambda calculus, it's possible to use control flow statements in a functional setting
- If we consider a source language with just local assignment and local control flow (including goto), the resulting lambda term remains *purely functional* 
  - As the SSA algorithm removes local mutability and control flow, these should not be viewed as computational effects, but rather as "syntactic sugar"
- Could a type and effect system, such as the one used by Koka, be used on the resulting term? If so, such a language could use restricted side effects akin to an imperative language

 As exploratory research, a prototype has been implemented to apply the SSA translation in an imperative-like source syntax, followed by the syntactic translation into the lambda calculus

```
e ::=
                                                  terms
                                                        variables
        x
                                                        unit value
                                                        numbers
                                                        booleans
       \lambda x.e
                                                        functions
                                                        application
       e1 e2
        if e_1 then e_2 else e_3
                                                        conditional
       let x = e_1 in e_2
                                                        let bind
       e \text{ where } \{ x_1 = e_1; ...; x_n = e_n \}
                                                        where bind
  ::=
                                                  types
                                                        variable
        \alpha
        unit
                                                        unit type
       int
                                                        integer
       bool
                                                        boolean
        \tau_1 \rightarrow \epsilon \ \tau_2
                                                        function
```

 The target calculus has a specialized where clause, meant to represent basic blocks: nested, mutually recursive abstractions



 As exploratory research, a prototype has been implemented to apply the SSA translation in an imperative-like source syntax, followed by the syntactic translation into the lambda calculus

```
e ::=
                                                  terms
                                                        variables
                                                        unit value
                                                        numbers
                                                        booleans
       \lambda x.e
                                                        functions
                                                        application
       e1 e2
        if e_1 then e_2 else e_3
                                                        conditional
       let x = e_1 in e_2
                                                        let bind
       e \text{ where } \{ x_1 = e_1; ...; x_n = e_n \}
                                                        where bind
  ::=
                                                  types
                                                        variable
        \alpha
        unit
                                                        unit type
       int
                                                        integer
       bool
                                                        boolean
        \tau_1 \rightarrow \epsilon \ \tau_2
                                                        function
```

• The target calculus has a specialized where clause, meant to represent basic blocks: nested, mutually recursive abstractions



- On the resulting lambda term, a type and effect inference algorithm based on effect rows is applied
- Most rules are standard and similar to those of the Hindley-Milner type system; effect rows inspired by those of Leijen's Koka language
- A special rule is adapted for the where rule, which binds mutually recursive terms that are monomorphic and don't perform any effects

```
\frac{\Gamma \vdash e_1 : bool ! \epsilon \qquad \Gamma \vdash e_2 : \tau  ! \epsilon \qquad \Gamma \vdash e_3 : \tau  ! \epsilon}{\Gamma \vdash \mathbf{if} \ e_1 \ \mathbf{then} \ e_2 \ \mathbf{else} \ e_3 : \tau  ! \epsilon} \text{ (IF)}
\frac{\Gamma \vdash e_1 : \tau_1 ! \ \langle \rangle \qquad \sigma = gen(\tau_1, \Gamma) \qquad \Gamma, x : \sigma \vdash e_2 : \tau_2 ! \epsilon}{\Gamma \vdash \mathbf{let} \ x = e_1 \ \mathbf{in} \ e_2 : \tau_2 ! \epsilon} \text{ (LET)}
\forall i \in 1...n. \ \Gamma, \ x_1 : \tau_1, ..., x_n : \tau_n \vdash e_1 : \tau_i ! \ \langle \rangle \qquad \Gamma, \ x_1 : \tau_1, ..., x_n : \tau_n \vdash e : \tau  ! \epsilon}
\Gamma \vdash e \ \mathbf{where} \ \{ x_1 = e_1 : ... : x_n = e_n \} : \tau  ! \epsilon 
(WHERE)
```



- On the resulting lambda term, a type and effect inference algorithm based on effect rows is applied
- Most rules are standard and similar to those of the Hindley-Milner type system; effect rows inspired by those of Leijen's Koka language
- A special rule is adapted for the where rule, which binds mutually recursive terms that are monomorphic and don't perform any effects

```
\frac{\Gamma \vdash e_1 \colon bool \, ! \; \epsilon \qquad \Gamma \vdash e_2 \colon \tau \, ! \; \epsilon \qquad \Gamma \vdash e_3 \colon \tau \, ! \; \epsilon}{\Gamma \vdash \mathbf{if} \; \mathbf{e}_1 \; \mathbf{then} \; e_2 \; \mathbf{else} \; e_3 \colon \tau \, ! \; \epsilon} \; (\text{IF})
\frac{\Gamma \vdash e_1 \colon \tau_1 \, ! \; \langle \rangle \qquad \sigma = gen(\tau_1, \Gamma) \qquad \Gamma, x \colon \sigma \vdash e_2 \colon \tau_2 \, ! \; \epsilon}{\Gamma \vdash \mathbf{let} \; x = e_1 \; \mathbf{in} \; e_2 \colon \tau_2 \, ! \; \epsilon} \; (\text{LET})
\forall i \in 1...n. \; \Gamma, \; x_1 \colon \tau_1, ..., x_n \colon \tau_n \vdash e_i \colon \tau_i \, ! \; \langle \rangle \qquad \Gamma, \; x_1 \colon \tau_1, ..., x_n \colon \tau_n \vdash e \colon \tau \, ! \; \epsilon}{\Gamma \vdash e \; \textbf{where} \; \{ \; x_1 = e_1 \colon ... \colon x_n = e_n \; \} \colon \tau \, ! \; \epsilon} \; (\text{WHERE})
```



- On the resulting lambda term, a type and effect inference algorithm based on effect rows is applied
- Most rules are standard and similar to those of the Hindley-Milner type system; effect rows inspired by those of Leijen's Koka language
- A special rule is adapted for the where rule, which binds mutually recursive terms that are monomorphic and don't perform any effects

```
\frac{\Gamma \vdash e_1 \colon bool \mid \epsilon \qquad \Gamma \vdash e_2 \colon \tau \mid \epsilon \qquad \Gamma \vdash e_3 \colon \tau \mid \epsilon}{\Gamma \vdash \mathbf{if} \ \mathbf{e}_1 \ \mathbf{then} \ e_2 \ \mathbf{else} \ e_3 \colon \tau \mid \epsilon} \ (\text{IF})
\frac{\Gamma \vdash e_1 \colon \tau_1 \mid \langle \rangle \qquad \sigma = gen(\tau_1, \Gamma) \qquad \Gamma, x \colon \sigma \vdash e_2 \colon \tau_2 \mid \epsilon}{\Gamma \vdash \mathbf{let} \ x = e_1 \ \mathbf{in} \ e_2 \colon \tau_2 \mid \epsilon} \ (\text{LET})
\forall i \in 1...n. \ \Gamma, \ x_1 \colon \tau_1, ..., x_n \colon \tau_n \vdash e_i \colon \tau_i \mid \langle \rangle \qquad \Gamma, \ x_1 \colon \tau_1, ..., x_n \colon \tau_n \vdash e \colon \tau \mid \epsilon} \ \Gamma \vdash e \ \text{where} \ \{ x_1 = e_1 \colon ... \colon x_n = e_n \} \colon \tau \mid \epsilon \ (\text{WHERE})
```



- Some small-scale programs were written in an imperative-like source syntax and run through the type inference algorithm
- The source syntax contained local mutability, control flow (including goto), and effect and handler declaration
- Preliminary results show functions to receive the expected types; basic blocks are well behaved in the sense that each block becomes a lambda abstraction with the same returning type and same effect
  - Phi functions guarantee that each block has and is called with the correct arity
- Algebraic effects freely compose inside the source program, giving an imperative look and feel, while still working on a purely functional setting (i.e., arbitrary side effects and mutability still forbidden!)



- Some small-scale programs were written in an imperative-like source syntax and run through the type inference algorithm
- The source syntax contained local mutability, control flow (including goto), and effect and handler declaration
- Preliminary results show functions to receive the expected types; basic blocks are well behaved in the sense that each block becomes a lambda abstraction with the same returning type and same effect
  - Phi functions guarantee that each block has and is called with the correct arity
- Algebraic effects freely compose inside the source program, giving an imperative look and feel, while still working on a purely functional setting (i.e., arbitrary side effects and mutability still forbidden!)



- Some small-scale programs were written in an imperative-like source syntax and run through the type inference algorithm
- The source syntax contained local mutability, control flow (including goto), and effect and handler declaration
- Preliminary results show functions to receive the expected types; basic blocks are well behaved in the sense that each block becomes a lambda abstraction with the same returning type and same effect
  - Phi functions guarantee that each block has and is called with the correct arity
- Algebraic effects freely compose inside the source program, giving an imperative look and feel, while still working on a purely functional setting (i.e., arbitrary side effects and mutability still forbidden!)



- Some small-scale programs were written in an imperative-like source syntax and run through the type inference algorithm
- The source syntax contained local mutability, control flow (including goto), and effect and handler declaration
- Preliminary results show functions to receive the expected types; basic blocks are well behaved in the sense that each block becomes a lambda abstraction with the same returning type and same effect
  - Phi functions guarantee that each block has and is called with the correct arity
- Algebraic effects freely compose inside the source program, giving an imperative look and feel, while still working on a purely functional setting (i.e., arbitrary side effects and mutability still forbidden!)



- Some small-scale programs were written in an imperative-like source syntax and run through the type inference algorithm
- The source syntax contained local mutability, control flow (including goto), and effect and handler declaration
- Preliminary results show functions to receive the expected types; basic blocks are well behaved in the sense that each block becomes a lambda abstraction with the same returning type and same effect
  - Phi functions guarantee that each block has and is called with the correct arity
- Algebraic effects freely compose inside the source program, giving an imperative look and feel, while still working on a purely functional setting (i.e., arbitrary side effects and mutability still forbidden!)



```
algorithm fib(var n) {
                                                            proc fib(n<sub>1</sub>) {
    var a = 0;
                                                                  goto L1;
   var b = 1:
                                                            L1: a_1 \leftarrow 0;
   for(var i = 0; i < n; i++) {
                                                                  b_1 \leftarrow 1:
      var c = b;
                                                                  goto L2:
      b = a + b;
                                                            L2: i_1 \leftarrow 0;
       a = c:
                                                                  goto L3;
                                                            L3: a_2 \leftarrow \phi(L2: a_1, L5: a_3);
    return a;
                                                                  b_2 \leftarrow \phi(L2: b_1, L5: b_3);
                                                                  i_2 \leftarrow \phi(L2: i_1, L5: i_3);
      L1: () → T
                                                                  if i_2 < n_1 then
          a_1 \leftarrow 0
                                                                        goto L4
          b_1 \leftarrow 1
                                                                  else
                                                                        goto L6;
                                                            L4: c_1 \leftarrow b_2;
       L2: √0 → T
                                  L5:
                                                () → T
                                                                  b_3 \leftarrow a_2 + b_2;
                                                                  a<sub>3</sub> ← c<sub>1</sub>;
          i_1 \leftarrow 0
                                      i_3 \leftarrow i_2 + 1
                                                                  goto L5:
                                                            L5: i_3 \leftarrow i_2 + 1;
                                                                  goto L3:
                                  L4:
                                                () → T
                                                            L6: return a<sub>2</sub>
L3: \alpha \rightarrow \beta \rightarrow y \rightarrow \tau
                                   c_1 \leftarrow b_2
       (i_2 < n_1)?
                                   b_3 \leftarrow a_2 + b_2
                                   a_3 + c_1
L6:
                    () → T
       return a2
```



```
algorithm fib(var n) {
                                                              proc fib(n<sub>1</sub>) {
   var a = 0;
                                                                    goto L1;
   var b = 1:
                                                              L1: a_1 \leftarrow 0;
   for(var i = 0; i < n; i++) {
                                                                   b_1 \leftarrow 1:
      var c = b;
                                                                    goto L2:
      b = a + b;
                                                              L2: i_1 \leftarrow 0;
       a = c:
                                                                    goto L3;
                                                              L3: a_2 \leftarrow \phi(L2: a_1, L5: a_3);
   return a;
                                                                   b_2 \leftarrow \phi(L2: b_1, L5: b_3);
                                                                   i_2 \leftarrow \phi(L2: i_1, L5: i_3);
      L1:() \rightarrow int
                                                                   if i_2 < n_1 then
         a_1 \leftarrow 0
                                                                          goto L4
         b_1 \leftarrow 1
                                                                    else
                                                                          goto L6;
                                                              L4: c_1 \leftarrow b_2;
       L2: √() → int
                                   L5:
                                                 () \rightarrow int
                                                                    b_3 \leftarrow a_2 + b_2;
                                                                    a<sub>3</sub> ← c<sub>1</sub>;
                                      i_3 \leftarrow i_2 + 1
          i<sub>1</sub> ← 0
                                                                    goto L5:
                                                              L5: i_3 \leftarrow i_2 + 1;
                                                                    goto L3:
                                   L4:
                                                 () \rightarrow int
                                                              L6: return a<sub>2</sub>
L3. int \rightarrow int \rightarrow int
                                    c_1 \leftarrow b_2
       (i_2 < n_1)?
                                 b_3 \leftarrow a_2 + b_2
                                    a_3 + c_1
L6:
              \downarrow () \rightarrow int
       return a2
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe<a>
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe<a>
algorithm safediv(var a, var b) {
    if(b == 0) {
        print("Can't divide by zero!")
        raise();
    }
    return a / b;
}
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe<a>
algorithm safediv(var a, var b) {
    if(b == 0) {
        print("Can't divide by zero!")
        raise();
    }
    return a / b;
}
// safediv: int -> int -> <exception, console | e> int
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe <a>
algorithm safediv(var a, var b) {
    if(b == 0) {
        print("Can't divide by zero!")
       raise():
   return a / b:
7
// safediv: int -> int -> <exception, console | e> int
algorithm safe1(var a, var b) {
   return catch([] {
       return safediv(a, b):
   });
7
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe <a>
algorithm safediv(var a, var b) {
    if(b == 0) {
        print("Can't divide by zero!")
        raise():
   return a / b:
7
// safediv: int -> int -> <exception, console | e> int
algorithm safe1(var a, var b) {
   return catch([] {
        return safediv(a, b):
   });
7
// safe1: int -> int -> <console | e> maybe<int>
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe <a>
algorithm safediv(var a, var b) {
    if(b == 0) {
        print("Can't divide by zero!")
        raise():
   return a / b:
7
// safediv: int -> int -> <exception, console | e> int
algorithm safe1(var a, var b) {
   return catch([] {
        return safediv(a, b):
   });
7
// safe1: int -> int -> <console | e> maybe<int>
algorithm safe2(var a, var b) {
   inject catch();
   return safediv(a, b);
```



```
// Context:
// print: string -> <console | e> unit
// raise: unit -> <exception | e> unit
// catch: (unit -> <exception | e> a) -> e maybe <a>
algorithm safediv(var a, var b) {
    if(b == 0) {
        print("Can't divide by zero!")
        raise():
   return a / b:
7
// safediv: int -> int -> <exception, console | e> int
algorithm safe1(var a, var b) {
   return catch([] {
        return safediv(a, b):
   });
7
// safe1: int -> int -> <console | e> maybe<int>
algorithm safe2(var a, var b) {
    inject catch();
    return safediv(a, b);
// safe2: int -> int -> <console | e> maybe<int>
```



- It's possible to write functional programs with local mutability and control flow; the SSA conversion algorithm translates statements into equivalent pure expressions
- The resulting lambda term may have its type inferred by a standard type inference algorithm (such as Hindley-Milner's
- Algebraic effect inference, when used with the SSA algorithm, compose freely giving an imperative look-and-feel in a still functional language, hopefully helping in writing algorithms described in an imperative way
- As the translation from SSA form to the lambda calculus is syntactical, it should be possible to adapt a type inference system to SSA syntax with basic blocks, skipping a step
- Could inference algorithms applied in SSA form help in type inference for actual imperative languages?



- It's possible to write functional programs with local mutability and control flow; the SSA conversion algorithm translates statements into equivalent pure expressions
- The resulting lambda term may have its type inferred by a standard type inference algorithm (such as Hindley-Milner's)
- Algebraic effect inference, when used with the SSA algorithm, compose freely giving an imperative look-and-feel in a still functional language, hopefully helping in writing algorithms described in an imperative way
- As the translation from SSA form to the lambda calculus is syntactical, it should be possible to adapt a type inference system to SSA syntax with basic blocks, skipping a step
- Could inference algorithms applied in SSA form help in type inference for actual imperative languages?



- It's possible to write functional programs with local mutability and control flow; the SSA conversion algorithm translates statements into equivalent pure expressions
- The resulting lambda term may have its type inferred by a standard type inference algorithm (such as Hindley-Milner's)
- Algebraic effect inference, when used with the SSA algorithm, compose freely giving an imperative look-and-feel in a still functional language, hopefully helping in writing algorithms described in an imperative way
- As the translation from SSA form to the lambda calculus is syntactical, it should be possible to adapt a type inference system to SSA syntax with basic blocks, skipping a step
- Could inference algorithms applied in SSA form help in type inference for actual imperative languages?



- It's possible to write functional programs with local mutability and control flow; the SSA conversion algorithm translates statements into equivalent pure expressions
- The resulting lambda term may have its type inferred by a standard type inference algorithm (such as Hindley-Milner's)
- Algebraic effect inference, when used with the SSA algorithm, compose freely giving an imperative look-and-feel in a still functional language, hopefully helping in writing algorithms described in an imperative way
- As the translation from SSA form to the lambda calculus is syntactical, it should be possible to adapt a type inference system to SSA syntax with basic blocks, skipping a step
- Could inference algorithms applied in SSA form help in type inference for actual imperative languages?



- It's possible to write functional programs with local mutability and control flow; the SSA conversion algorithm translates statements into equivalent pure expressions
- The resulting lambda term may have its type inferred by a standard type inference algorithm (such as Hindley-Milner's)
- Algebraic effect inference, when used with the SSA algorithm, compose freely giving an imperative look-and-feel in a still functional language, hopefully helping in writing algorithms described in an imperative way
- As the translation from SSA form to the lambda calculus is syntactical, it should be possible to adapt a type inference system to SSA syntax with basic blocks, skipping a step
- Could inference algorithms applied in SSA form help in type inference for actual imperative languages?

