a) 
$$\iint_{\mathbb{R}} \frac{x^2y}{y^2+4} dA$$
, and  $\mathbb{R} = [-2,2] \times [0,1]$ 

$$\iint_{R} \frac{x^{2}y}{y^{2}+4} dA = \iint_{-2} \frac{x}{y^{2}+4} dy dx$$

$$= \int_{-2}^{2} \frac{x}{2} ln(y^{2}+4) \int_{-2}^{1} dx$$

$$= \int_{-2}^{2} \frac{2}{x} \left[ \ln 5 - \ln 4 \right] dx = \frac{\ln 5 - \ln 4}{2} \cdot \frac{x^{3}}{3} \Big|_{-2}^{2}$$

$$= \frac{\ln 5 - \ln 4}{2} \left( \frac{8}{3} - \left( -\frac{8}{3} \right) \right) = \frac{16}{6} \left( \ln 5 - \ln 4 \right) = \frac{8}{3} \ln \left( \frac{5}{4} \right).$$

b) 
$$\iint x sen(xy) dV$$
, and  $B = CO_11/2 T \times CO_1 \pi T \times CO_1 \pi T = CO_11/2 T \times CO_1 \pi T = CO_1 \pi T =$ 

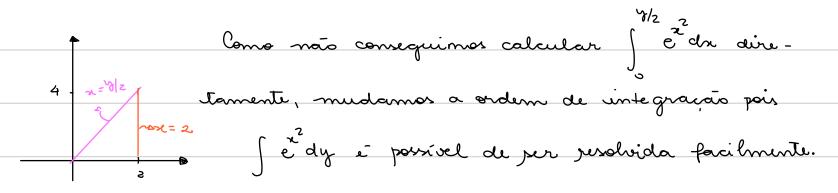
$$\iiint_{B} x \operatorname{sen}(xy) dV = \iiint_{B} \sqrt{2\pi} x \operatorname{sen}(xy) dy dx dz$$

$$= \int_{0}^{\pi/3} \int_{0}^{1/2} \cos(\pi x) dx dx = \int_{0}^{\pi/3} \int_{0}^{1/2} (1 - \cos(\pi x)) dx dx$$

$$= \int_{0}^{\pi/3} x - \frac{\sin(\pi x)}{\pi} \left| \frac{1/2}{2} - \frac{\sin(\pi/2)}{\pi} \right| dz$$

$$= \int_{0}^{\pi/3} \left( \frac{1}{2} - \frac{1}{\pi} \right) d3 = \frac{\pi}{3} \left( \frac{1}{2} - \frac{1}{\pi} \right) = \frac{\pi}{6} - \frac{1}{3}$$

Calcula a integral 
$$\int_{3}^{4} \int_{3}^{2} e^{x^{2}} dx dy$$



Assim, tracamos 
$$0 \le y \le 4 = y_2 \le x \le 2$$
 por  $0 \le x \le 2 = 0 \le y \le 2x$ 

Portanto,
$$\int_{0}^{4} \int_{0}^{2} e^{x^{2}} dx dy = \int_{0}^{2} \int_{0}^{2x} e^{x^{2}} dy dx = \int_{0}^{2} e^{x^{2}} dy dx$$

$$= \int_{0}^{2} x^{2} = 2x dx = e = e-1.$$

du = 22dx

Para calcular o volume de um polido E, basta calcular a integral III 1 dV. Urando esta informação, calcule o volume do polido = alimitado pelo paraholoide z=4-(x²+y²)

Temos que z está limitado pelas funções z=0 e z=4-(x²+y²)
Assim, 0 = z = 4-(x²+y²). Além disso, re ey estão limitados no disco

2+y ≤4. en coordinadas polares: D∈ R≤2 e D∈ Θ∈ 2π.

Calculando a integral utilizando coordenadas cilindricas:

$$= \int_{0}^{2\pi} \int_{0}^{2} (4\pi - \pi^{3}) d\pi d\theta = \int_{0}^{2\pi} \frac{2\pi^{2} - \pi^{4}}{4} \int_{0}^{2} d\theta = \int_{0}^{2\pi} 4 d\theta$$

e pelo plano z=0.

(4) Calaile III 3° dV, ende E e o pólido delimitado pelas pemi-

Vamos utilizer coordenadas esféricas:

Assum, temos

\* 
$$g^2 = \rho^2 \cos^2 \phi$$

$$\iiint_{E} 3^{2} dV = \iiint_{2\pi} \pi/2 \stackrel{3}{=} 2^{2} \cosh \phi \log \phi \log \phi$$

$$= \int_{0}^{2\pi} \int_{0}^{\pi/2} \int_{0}^{3} \cos^{2}\varphi \operatorname{pen}\varphi \varphi d\varphi d\varphi$$

$$= \int_{0}^{2\pi} \int_{0}^{\pi/2} \cos^{2}\varphi \sin\varphi \left(\frac{5}{5}\right)^{3} d\varphi d\varphi$$

$$= \int_{0}^{2\pi} \int_{0}^{\pi/2} \frac{242}{5} \cos \phi \sin \phi d\phi d\phi$$

$$= \int_{0}^{2\pi} \frac{2\pi}{5} \left( -\frac{2\pi}{3} + \frac{\pi}{2} \right) d\theta = \int_{0}^{2\pi} \frac{2\pi}{5} \cdot \frac{1}{3} d\theta = \frac{242}{15} \cdot \frac{1}{15} d\theta = \frac{242}{15} d\theta$$