



Convolutional Neural Networks (8DC00)

Friso G. Heslinga

Friso G. Heslinga MSc.

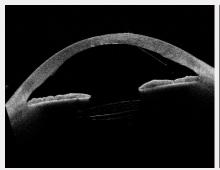


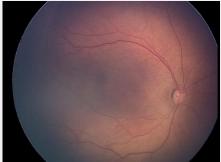
Background: BSc and MSc in Biomedical Engineering, MSc in Health Sciences (University of Twente).

Work/internship experience: University of Western Australia, University of California - Berkeley, Harvard Medical School

PhD Research: Deep learning, Medical image analysis, Ophthalmology





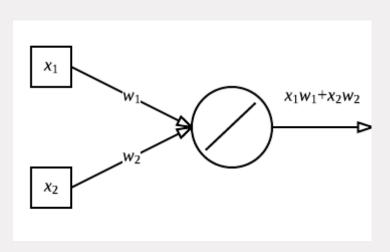




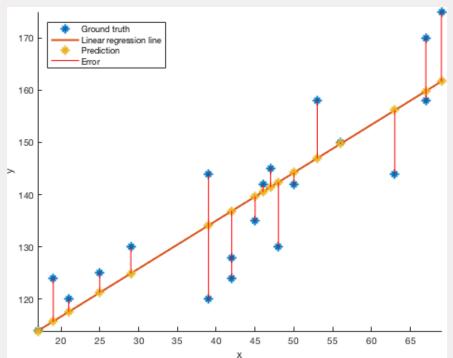


Week	Date	Lecturer	Topics
1	1 Sept.	Maureen	Course introduction; Software demo; Image registration (1)
	3 Sept.	Maureen	Image registration (2); Geometrical transformations
2	8 Sept.	Maureen	Point-based registration
	10 Sept.	Maureen	Intersity-based registration; Evaluation metrics
3	15 Sept.	Catch-up day (no lecture)	
	17 Sept.	Cornel Zachiu (UMCU)	Guest lecture 1: Image analysis for adaptive radiotherapy
4	22 Sept.	Mitko	Introduction to CAD; k-NN; Decision trees
	24 Sept.	Mitko	Generalization and overfitting
5	29 Sept.	Mitko	Logistic regression; Neural networks
	1 Oct.	Friso	Convolutional neural networks
6	6 Oct.	Friso	Deep learning frameworks and applications
	8 Oct.	Friso	Unsupervised machine learning
7	13 Oct.	Maureen	Deep learning for deformable image registration
	15 Oct.	Geert-Jan Rutten (ETZ)	Guest lecture 2: Image analysis in neurosurgery applications
8	20 Oct	Self-study (no lecture)	Active shape models
	22 Oct	Self-study (no lecture)	Active shape models

Previously – Linear regression

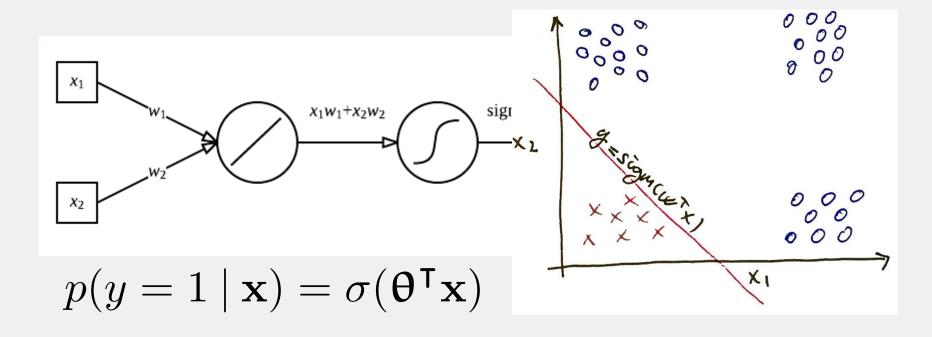


$$\hat{y} = \mathbf{\theta}^{\mathsf{T}} \mathbf{x}$$



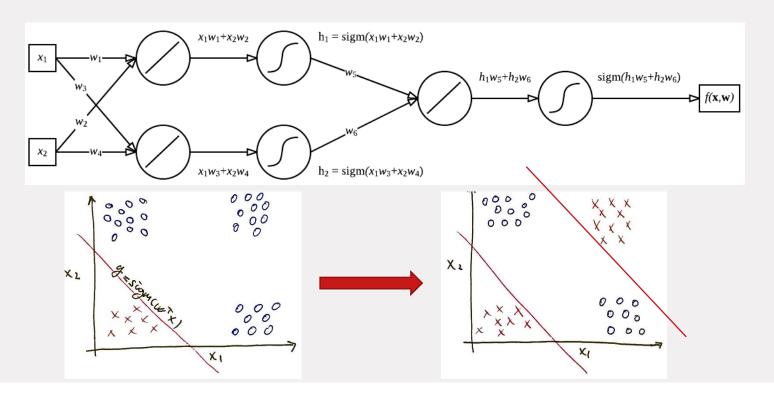


Previously – Logistic regression



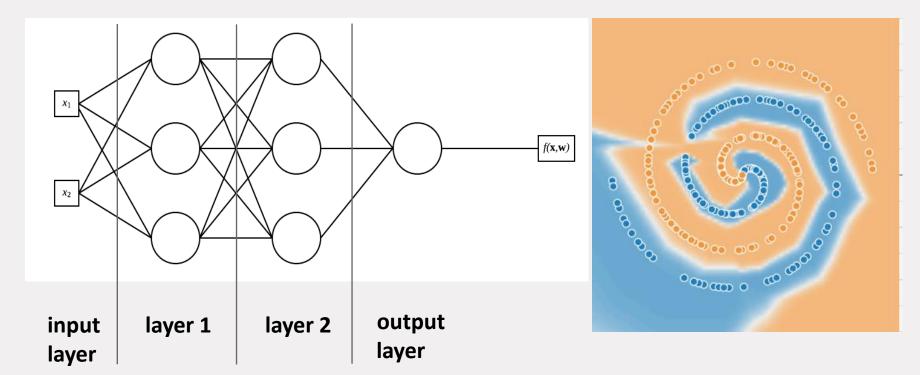


Previously – Neural networks





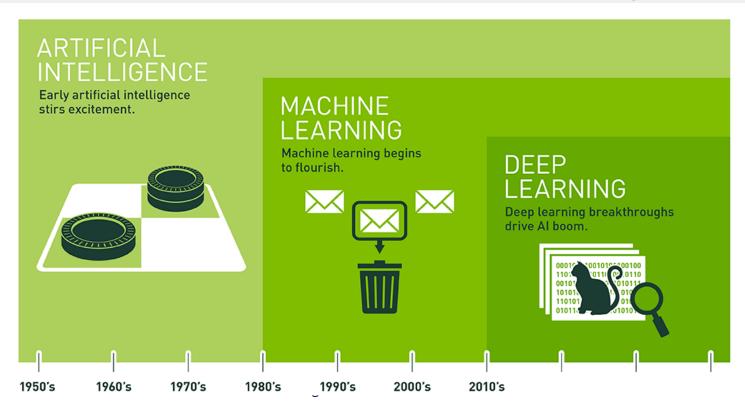
Previously – Neural networks





Previously – Machine learning

Figure source: nvidea.com





Today: Convolutional neural networks (CNN)

■ Neural networks → Convolutional neural networks

Building blocks for deep learning models for image analysis:

- Convolutional layer
- Max-pooling layer

Not needed for the project, but will be on the exam



Learning outcomes

- Student can explain the concept of convolutions in a neural network
- Student can describe why we can use a convolutional approach for (medical) images
- Student can explain why convolutions enable development of deep (and large) neural networks
- Students can explain and apply the max-pooling layer in a convolutional neural network
- Students can motivate the choice for a kernel size



Lecture outline

- Images as input to neural network
- Reducing # of weights
- 1D convolutions
- 2D convolutions
- Break (15 mins)
- Kernels
- Max-pooling
- Interactive example



Images as input to neural networks

24 pixels



3 color channels (red, green, blue)

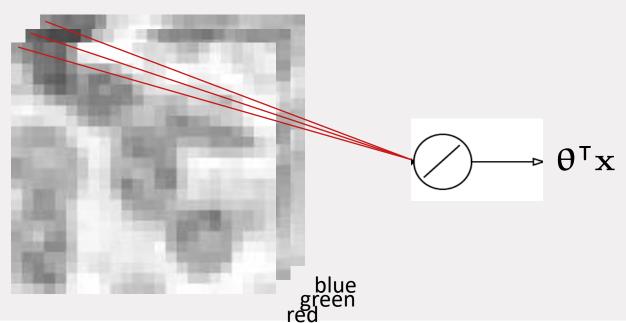
= 1728 features (\mathbf{x}_i are 1728 dimensional vectors)

If we train linear regression with these inputs (such as in the first practical), we will have 1728 weights w and a bias b.



Every pixel is an input

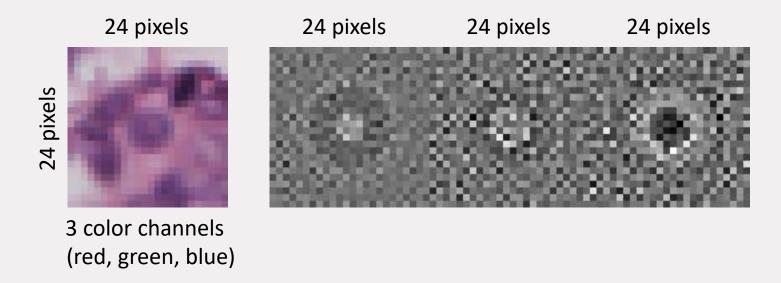
Every pixel from every color channel is multiplied by a weight





Post-training: visualizing what model has learned

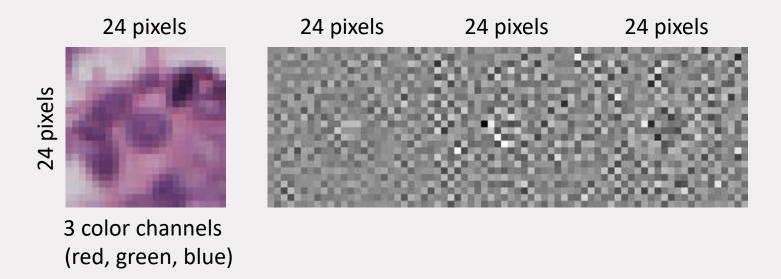
Reshape vector of parameters into 24x24x3 image





Post-training: visualizing what model has learned

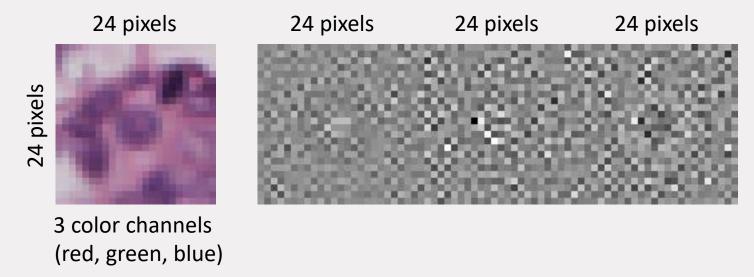
Only 25% of training samples.. Looks noisy!





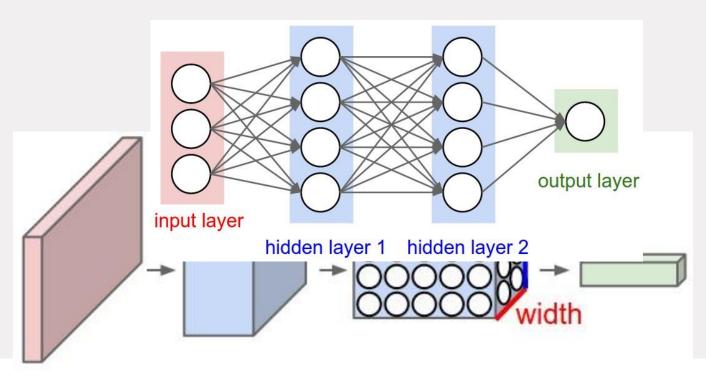
Post-training: visualizing what model has learned

You can think of it as "there is not enough training data to reliably estimate all model weights".



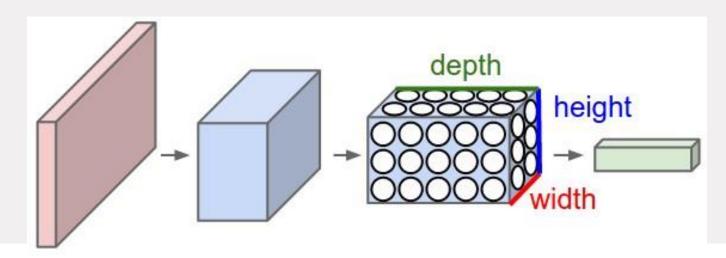


Many weights





With large inputs such as images and deep networks, the number of weights "explodes". We need a way to reduce the number of weights, without sacrificing performance.

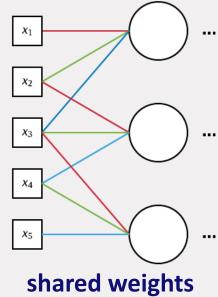




••• ... ••• "regular" NN 15 weights

receptive field ••• χ_3 ... ••• sparsely connected NN 9 weights

How many weights?

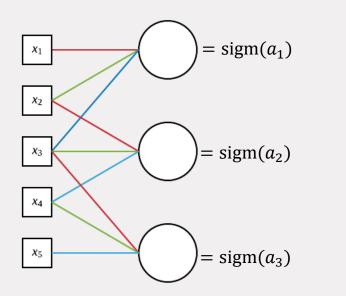


nared weights

3 weights



Shared weights



$$a_1 = x_1 w_1 + x_2 w_2 + x_3 w_3$$

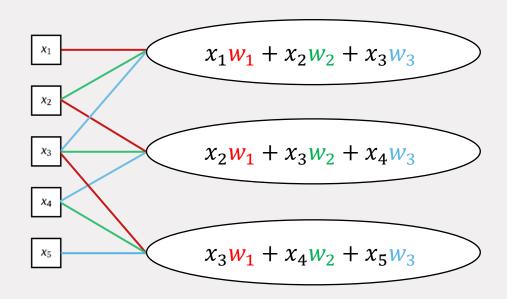
$$a_2 = x_2 w_1 + x_3 w_2 + x_4 w_3$$

$$a_3 = x_3 w_1 + x_4 w_2 + x_5 w_3$$

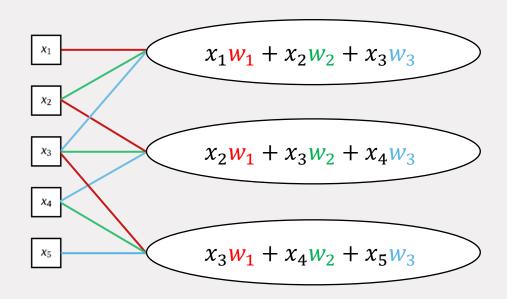
$$\begin{bmatrix} a_1 & a_2 & a_3 \end{bmatrix} = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 & x_5 \end{bmatrix} * \begin{bmatrix} \mathbf{w}_1 & \mathbf{w}_2 & \mathbf{w}_3 \end{bmatrix}$$

convolution, thus convolutional NN

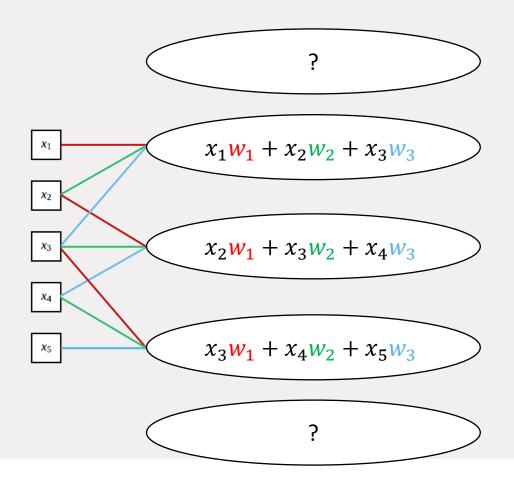






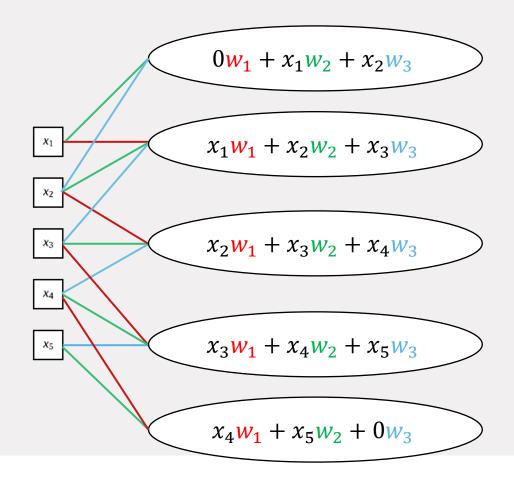






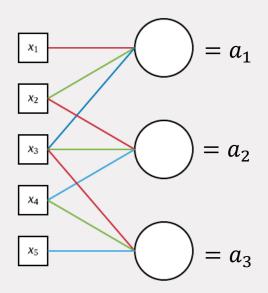
How can we keep the same number of features in hidden layer 1?





Zero-padding!





$$a_1 = x_1 w_1 + x_2 w_2 + x_3 w_3$$

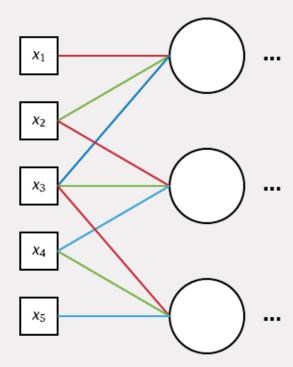
$$a_2 = x_2 w_1 + x_3 w_2 + x_4 w_3$$

$$a_3 = x_3 w_1 + x_4 w_2 + x_5 w_3$$



Properties of convolutional neural networks

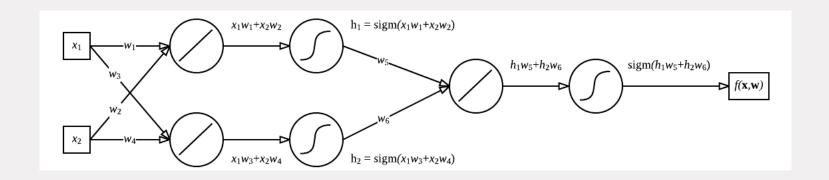
- Sparse connectivity
- Weight sharing
- Parallel computations





Why does this work?

- Multiple layers
- Hidden layers contain features calculated from previous layers



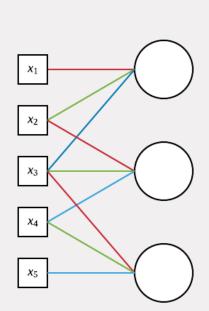


Why does this work?

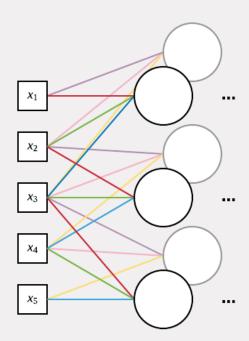
- Different layers contain different transformation
 - Simple (e.g. edges, colors)
 - Complex (final layers)

One added benefit is that the learned transformations will be equivariant with translation (if the features/image is shifted up/down the features will still be detected).







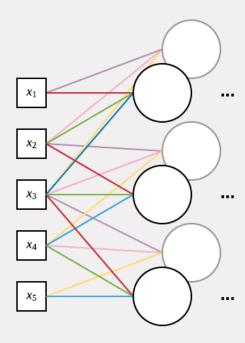


two sets shared weights
6 weights

We can add additional sets of weights that can learn additional interesting transformation of the input.

Note that the added neurons <u>are not</u> a new layer. They are part of layer 1.





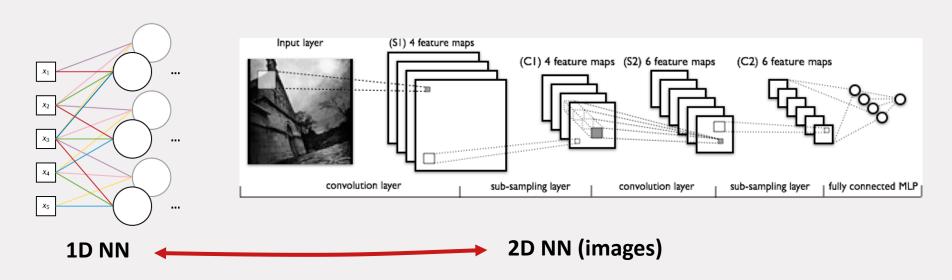
two sets shared weights
6 weights

$$\begin{bmatrix} a_{1,1} & a_{1,2} & a_{1,3} \end{bmatrix} = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 & x_5 \end{bmatrix} * \begin{bmatrix} w_{1,1} & w_{1,2} & w_{1,3} \end{bmatrix}$$
$$\begin{bmatrix} a_{2,1} & a_{2,2} & a_{2,3} \end{bmatrix} = \begin{bmatrix} x_1 & x_2 & x_3 & x_4 & x_5 \end{bmatrix} * \begin{bmatrix} w_{2,1} & w_{2,2} & w_{2,3} \end{bmatrix}$$

 $\begin{bmatrix} w_{1,1} & w_{1,2} & w_{1,3} \end{bmatrix}$, and $\begin{bmatrix} w_{2,1} & w_{2,2} & w_{2,3} \end{bmatrix}$ are **convolution kernels**. They extract <u>features</u>. However, they are not hand-designed features – they were <u>learned</u> by the neural network.

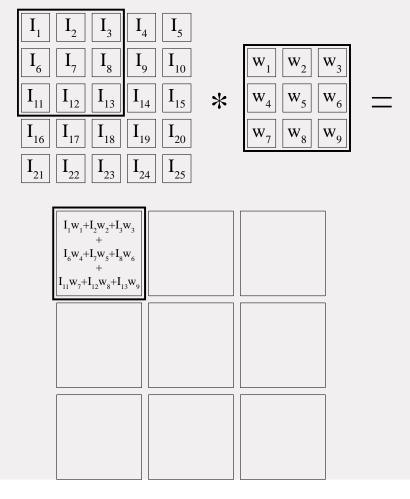


Convolutional neural networks are ideal for images

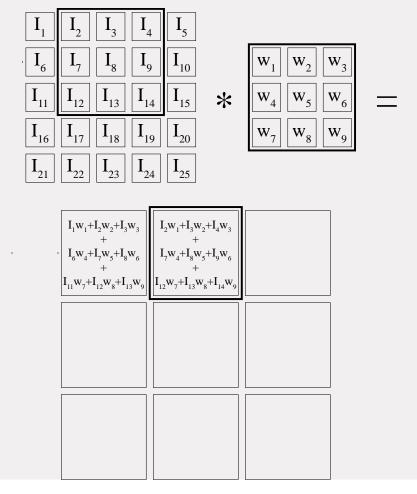


Because of the weight sharing, convolutional neural networks only work with structured data (such as images) as inputs.

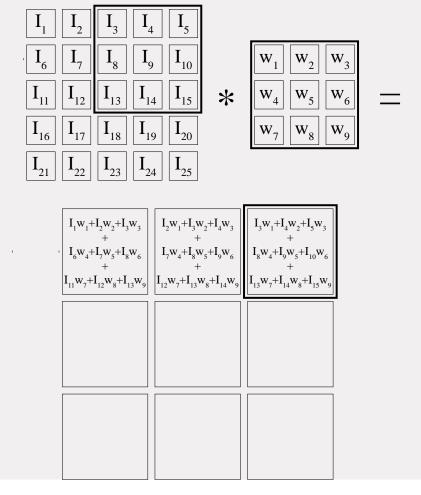




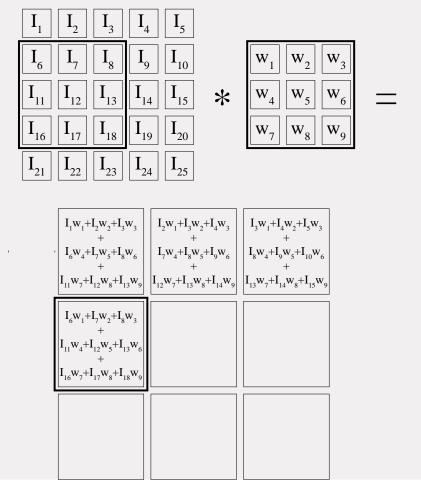




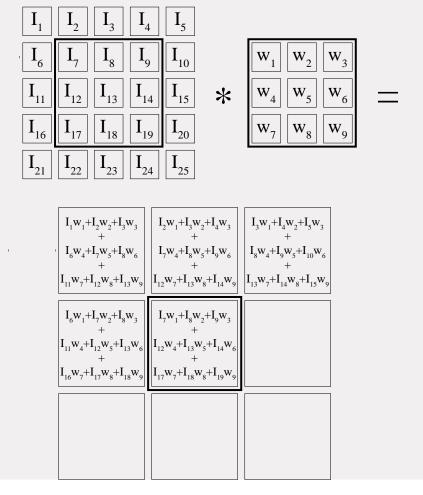




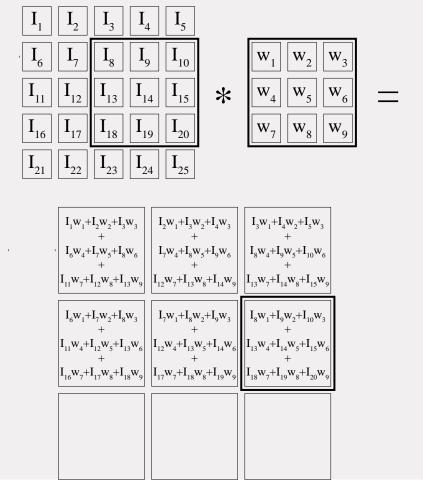




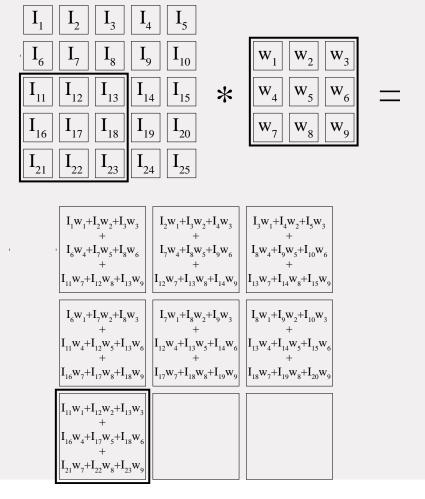




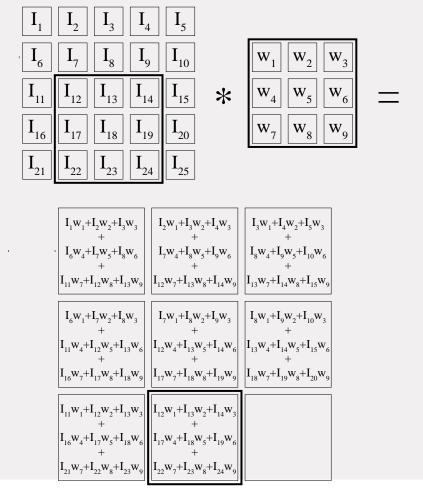




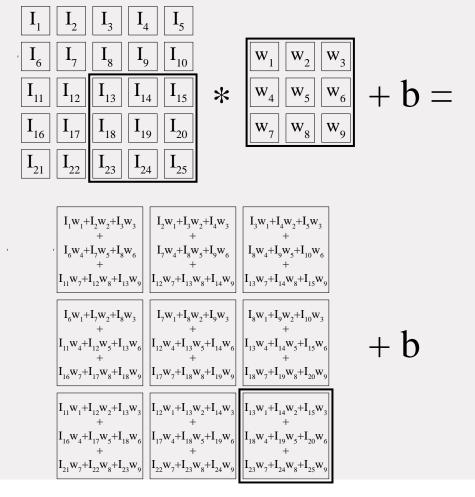






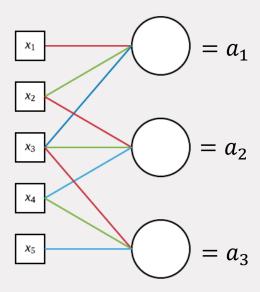






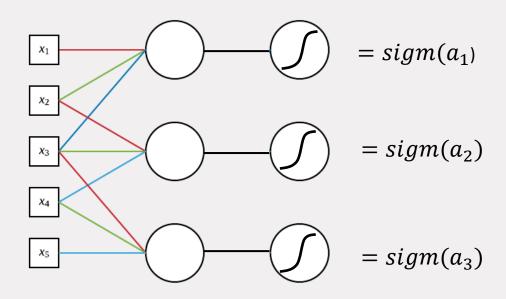


Convolutions + non-linearity



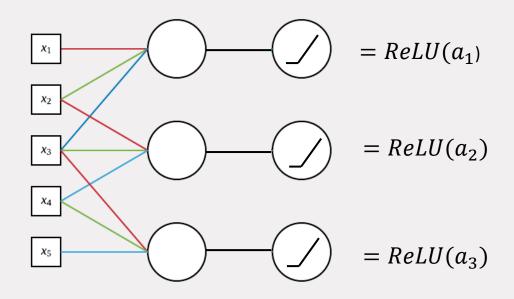


Convolutions + non-linearity (sigmoid)



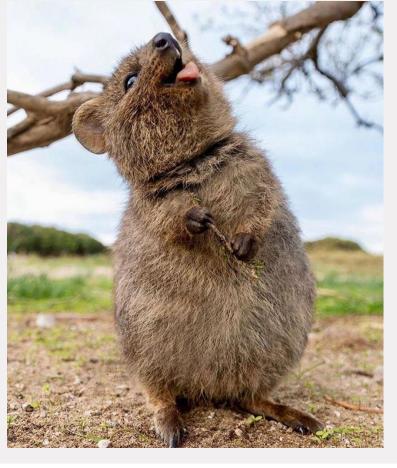


Convolutions + non-linearity (ReLU)





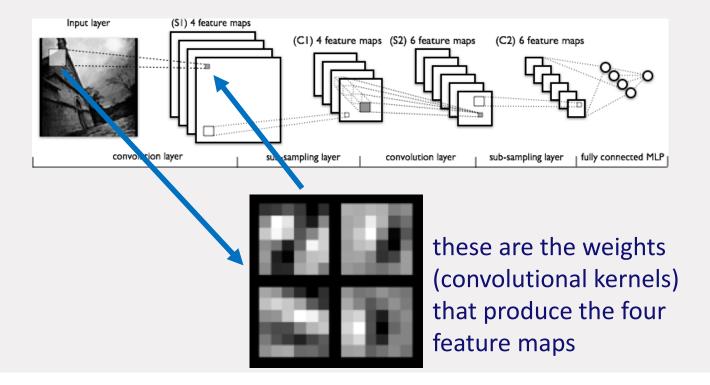
Break!



Quokka (Australia) https://imgur.com/r/aww/GqJi0il



Convolutional kernels



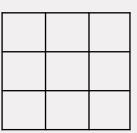


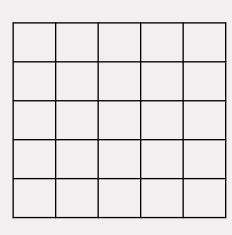
Kernel size

1 x 1

3 x 3

5 x 5

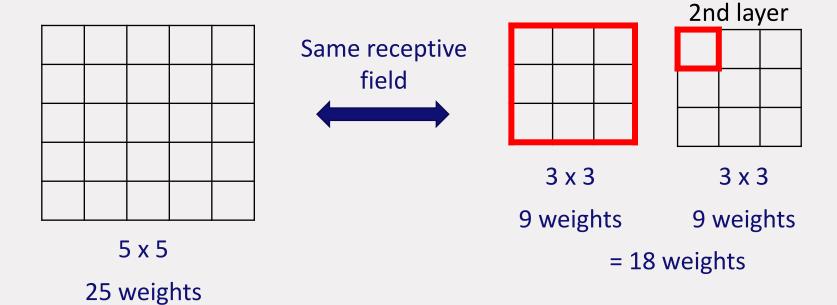




- More weights → more information
- More computations / memory
- Receptive field

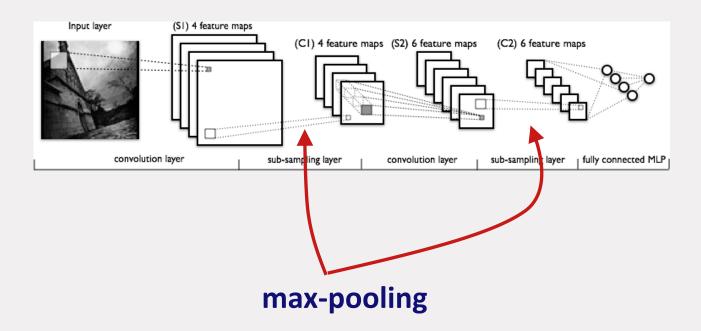


Receptive field





Max-pooling

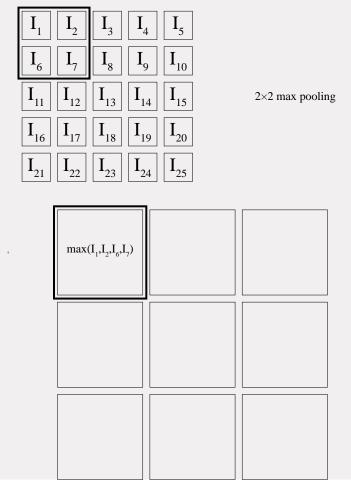




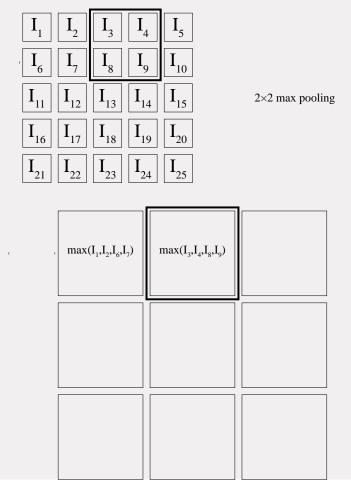
Max-pooling

- Reduce size of feature space
- Maximum of features
- Typical kernel size = 2 x 2

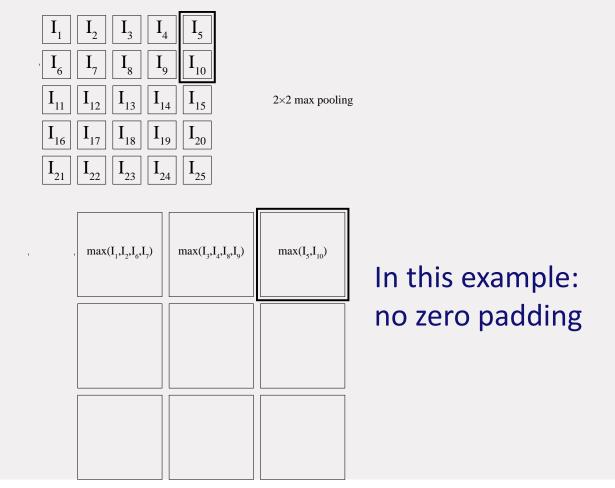




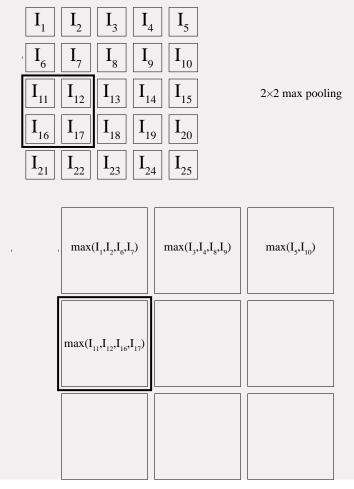




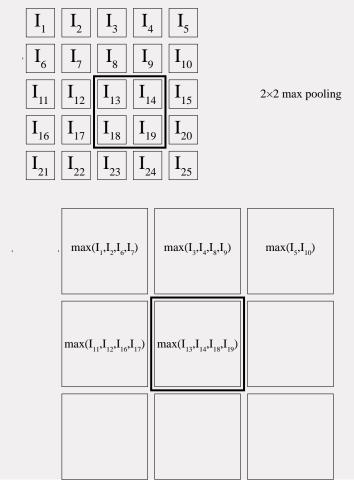




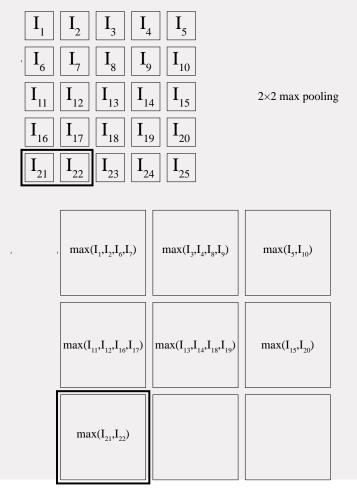




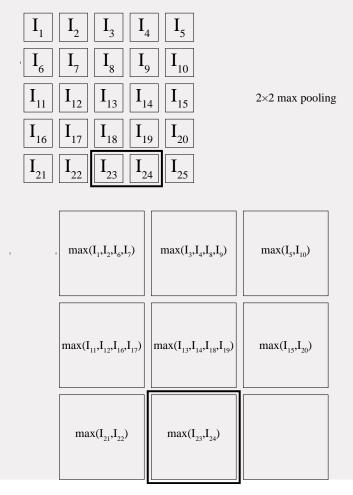




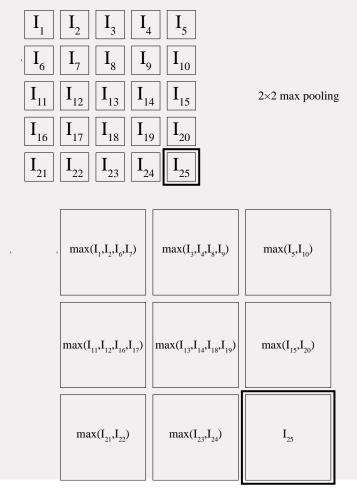














Benefits of max-pooling

- "Quickly" reduces the number size of the feature maps
- Introduces translation invariance (slightly translated version of the input image will result in the same output)

Alternative: Average Pooling



Let try it out!

http://scs.ryerson.ca/~aharley/vis/conv/flat.html

An Interactive Node-Link Visualization of Convolutional Neural Networks

Adam W. $Harley^{(\boxtimes)}$

Department of Computer Science, Ryerson University, Toronto, ON M5B 2K3, Canada aharley@scs.ryerson.ca



Training of Convolutional Neural Networks

- Similar to training of 'fully connected' neural networks
- Choose some (random) initial values for network weights
- Optimize networks weights with respect to a loss function that describes difference between network output and label/annotation
- Update networks weights iteratively

Through a process is called 'backpropagation'. A good explanation can be found here: https://www.youtube.com/watch?v=i940vYb6noo (5:10 - 28:00, not exam material)

Keep track of model performance on train & validation set



Summary

- Concept of convolutions in a neural network
- Why can we use a convolutional approach for (medical) images
- Convolutions enable development of deep (and large) neural networks
- Max-pooling layer in a convolutional neural network
- Kernel size
- Receptive field



