

# Notes

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## Notation

- $N$  number of time series
- $T$  length of time series
- $y_t$   $N \times 1$  vector of observation at  $\mathbf{t}$
- $f_t$   $q \times 1$  factor at  $\mathbf{t}$
- $B$   $N \times q$  loading matrix

## Method

PCA:

$$\operatorname{argmin}_{\mathbf{f}_t \in \mathbb{R}^K} \sum_{t=1}^T (\mathbf{y}_t - \mathbf{B}\mathbf{f}_t)' (\mathbf{y}_t - \mathbf{B}\mathbf{f}_t) \quad (1)$$

WPCA:

$$\operatorname{argmin}_{\mathbf{f}_t \in \mathbb{R}^K} \sum_{t=1}^T (\mathbf{y}_t - \mathbf{B}\mathbf{f}_t)' \Sigma_u^{-1} (\mathbf{y}_t - \mathbf{B}\mathbf{f}_t) \quad (2)$$

Karlman Filter

## Experiment

Cholesky decomposition is not positive definite.

**Error in chol.default(denom) :  
the leading minor of order 71 is not positive definite**

## Reference

- Quefeng Li, Guang Cheng, Jianqing Fan & Yuyan Wang (2018) Embracing the Blessing of Dimensionality in Factor Models, *Journal of the American Statistical Association*, 113:521, 380-389, DOI: 10.1080/01621459.2016.1256815
- Bai, J., and Liao, Y. (2013), “Statistical Inferences Using Large Estimated Covariances for Panel Data and Factor Models,” *arXiv:1307.2662*. [380,381,382,383]