

# **Astronomy Variant Question Set**

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# The Night Sky

## Question 1: Stellar Triangulation

Two observatories at latitude  $40^{\circ}\text{N}$  measure the position of an asteroid simultaneously. Their longitudes differ by  $6.0^{\circ}$ , giving a baseline of 667 km. The asteroids apparent positions differ by  $48''$ . Assuming the baseline is perpendicular to the line of sight, compute the asteroids distance in km.

## Question 2: Parallax Distance and Absolute Magnitude

A nearby star has apparent magnitude  $m = 7.6$  and parallax  $p = 0.042''$ .

1. Compute its distance in parsecs.
2. Determine its absolute magnitude  $M$ .

## **Question 3: Magnitude and Flux Ratio**

Two variable stars A and B lie in the same cluster at distance 1.8 kpc. Star A brightens from  $m = 12.0$  to  $m = 11.2$ . Star B dims from  $m = 10.5$  to  $m = 11.0$ . Compute the ratio of the new flux of star A to the new flux of star B.

## **Question 4: Constellation Visibility at Given Latitude**

An observer at latitude  $+52^\circ$  wishes to know whether a star of declination  $-18^\circ$  is ever visible.

1. Determine whether the star rises above the horizon.
2. If it does, compute its maximum altitude when crossing the meridian.

## **Question 5: Solar Altitude on a Solstice**

At latitude  $+35^\circ$ , compute the Sun's maximum altitude:

1. on the summer solstice,
2. on the winter solstice.

Assume Earth's axial tilt is  $23.5^\circ$ .

## **Question 6: RADec and Meridian Crossing Time**

A star has coordinates  $\text{RA} = 05^{\text{h}}18^{\text{m}}$ ,  $\text{Dec} = +22^\circ$ . On February 10, the Sun's RA is approximately  $21^{\text{h}}$ . Estimate the local sidereal time at midnight and determine the clock time when the star crosses the meridian.

## Question 7: Atmospheric Refraction Shift

A star at true altitude  $12^\circ$  experiences atmospheric refraction approximated by  $r = \frac{1.02^\circ}{\tan(h+10.3^\circ)/(h+5.11^\circ))}$  where  $h$  is the true altitude in degrees and  $r$  is in arcminutes. Compute the apparent altitude of the star.

## Question 8: Sidereal vs Solar Day Timing

A star rises at 22:16 local time on March 1. Assuming the sidereal day is 23h 56m, determine the rise time of the same star on March 15.

## Question 9: Lunar Synodic/Sidereal Relation

The Earth's orbital period is  $P_{\text{year}} = 365.25$  days. Using the relation

$$\frac{1}{P_{\text{sid}}} - \frac{1}{P_{\text{syn}}} = \frac{1}{P_{\text{year}}},$$

an astronomer measures the synodic period of a moon around a distant exoplanet to be  $P_{\text{syn}} = 34.7$  hr. Compute the moon's sidereal period in hours.

## Question 10: Eclipse Geometry and Angular Sizes

A moon of radius 1800 km orbits its planet at distance  $4.9 \times 10^5$  km. Its star has radius  $6.2 \times 10^5$  km and lies  $1.4 \times 10^8$  km from the planet.

1. Compute the angular sizes of the star and moon as seen from the planet.
2. Determine whether a total or annular eclipse occurs when the moon passes directly in front of the star.

## Question 11: Planetary Synodic Period and Opposition

A newly discovered asteroid has sidereal period 4.21 years.

1. Compute its synodic period with respect to Earth.
2. Determine how many days elapse between successive oppositions.

## Question 12: Meteoroid Impact Rate Estimate

A meteoroid stream has spatial density  $4.0 \times 10^{-8} \text{ m}^{-3}$ . Earth sweeps through the stream at  $v = 29.8 \text{ km/s}$  over a cross-sectional area  $\pi R_{\oplus}^2$  with  $R_{\oplus} = 6370 \text{ km}$ . Estimate the number of meteoroids entering Earth's atmosphere per second during the peak of the shower.

# The Solar System

## **Question 1: Orbital Geometry and Inferior Conjunction**

A newly discovered inner planet has a synodic period of 142 days as seen from Earth. Assuming circular, coplanar orbits and  $P_E = 365.25$  days, determine

1. the planets sidereal period,
2. its orbital radius in AU.

## **Question 2: Keplerian Mass Determination in Binary Motion**

A small moon orbits a dwarf planet in a circular orbit of radius 880 km with period  $P = 11.3$  hr. Determine

1. the mass of the dwarf planet,
2. the escape velocity from its surface if its radius is  $R = 420$  km.

## Question 3: Atmospheric Scale Height on a Terrestrial World

A rocky planet has surface gravity  $g = 6.1 \text{ m s}^{-2}$  and atmospheric temperature  $T = 295 \text{ K}$ . Its atmosphere is dominated by nitrogen ( $m = 4.65 \times 10^{-26} \text{ kg}$ ). Calculate

1. the scale height  $H$ ,
2. the pressure at altitude  $z = 42 \text{ km}$  if the surface pressure is  $P_0 = 0.89 \text{ bar}$ .

## Question 4: Solar Insolation and Equilibrium Temperature

A planet orbits a Sun-like star at 2.35 AU and has Bond albedo  $A = 0.27$ . Assuming blackbody equilibrium with uniform heat redistribution, compute the planets equilibrium temperature.

## Question 5: Rotation and Oblateness of a Giant Planet

A gas giant of radius  $R = 6.4 \times 10^7$  m rotates once every  $P = 8.1$  hr. Assume hydrostatic balance and use the approximation

$$f \approx \frac{3R^3}{2GMP^2}$$

for the flattening  $f = (R_{\text{eq}} - R_{\text{pol}})/R_{\text{eq}}$ . If the planet's mass is  $M = 1.9 \times 10^{27}$  kg, compute its flattening.

## Question 6: Surface Cratering and Age Estimation

A region on an icy moon shows 185 craters larger than 5 km across per million square kilometers. If the external impact flux for bodies of that size is  $F = 7.5 \times 10^{-15}$  km $^{-2}$ yr $^{-1}$ , estimate the surface age of the region.

## Question 7: Ring Particle Orbit and Resonances

A ring particle orbits a giant planet at radius  $1.42 \times 10^5$  km with period  $P_r = 0.62$  days. A nearby moon has orbital radius  $2.31 \times 10^5$  km and period  $P_m = 1.82$  days. Determine whether the ring location corresponds to a  $2 : 1$  or  $3 : 1$  mean-motion resonance with the moon.

## Question 8: Meteoroid Ablation and Energy Deposition

A stony meteoroid of mass  $m = 180$  kg enters an atmosphere at  $v = 17.5$  km s $^{-1}$ . Assuming 85% of its kinetic energy is deposited as thermal energy in the air, compute

1. the total deposited energy in joules,
2. the equivalent energy in tons of TNT (1 ton TNT =  $4.184 \times 10^9$  J).

## Question 9: Cometary Outgassing and Non-Gravitational Acceleration

A comet nucleus of mass  $M = 3.4 \times 10^{12}$  kg experiences a measured non-gravitational acceleration

$$a_{\text{ng}} = 2.6 \times 10^{-7} \text{ m s}^{-2}.$$

If the gas outflow speed is  $u = 620 \text{ m s}^{-1}$ , estimate the required mass-loss rate  $\dot{M}$  assuming thrust  $T = \dot{M}u = Ma_{\text{ng}}$ .

## Question 10: Protoplanetary Disk and Accretion Timescale

At 3 AU in a young disk, the solid surface density is  $\Sigma_s = 5.2 \text{ kg m}^{-2}$ . Planetesimals of radius  $r = 7.0 \text{ km}$  and density  $1400 \text{ kg m}^{-3}$  grow by sweeping up material with gravitational focusing factor  $F_g = 18$ . If the orbital period is  $P = 5.2$  years, estimate the mass-doubling timescale for an individual planetesimal.