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# **Linearisation of multiple RF-power amplifiers with the presence of antenna crosstalk**

Based on measurement

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Master thesis  
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## AALBORG UNIVERSITY

### STUDENT REPORT

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**Title:**

Linearisation of multiple RF-power amplifiers with the presence of antenna crosstalk

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**Project Group:****Participant(s):**

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**Abstract:**

This project is aiming on linearisation on RF-power amplifiers with the presence of antenna cross-talk. The crosstalk plays an important role in driving the amplifiers in the linear region. A better understanding of this is given by the use of measurement. First Digital Pre Distortion (DPD) is applied to one amplifier and then several amplifiers with one antenna each. The measurement shows that the antennas introduces distortion and that it can be compensated for by treating the setup with antennas as one model when doing DPD.

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## AALBORG UNIVERSITET

### STUDENTERRAPPORT

#### Institut for Elektroniske Systemer

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**Titel:**

Linearisering af flere RF-power forstærkere med tilstædeværelse af crosstalk mellem antenner

**Tema:****Projektperiode:**

2019

**Projektgruppe:****Deltager(e):**

Karsten Schou Nielsen

**Abstract:**

Dette projekt sigter mod linearisering af RF-effektforstærkere med tilstædeværelse af crosstalk mellem antenner. Crosstalk spiller en vigtig rolle ved at drive forstærkere i den lineære region. En bedre forståelse af dette er givet ved hjælp af målinger. Først Digital Pre Distortion (DPD) anvendes til en forstærker og derefter flere forstærkere med en antennen hver. Måling viser, at antennerne introducerer forvrængning, og at det kan kompenseres ved at behandle opstætningen med antennen som en model, når der laves DPD.

**Vejleder(e):**

Ming Shen

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# **Todo list**



# Preface

This thesis project has been carried out within the Antennas, Propagation and Millimetre-Wave Systems (AMPS) at Aalborg University Denmark under supervision of associate professor Ming Shen. I am thankful for this valuable experience at the university and by the new knowledge I have acquired, as well as by the global atmosphere at AMPS. I hope that this work will be helpful for others in the same area in the future.

Aalborg University, May 31, 2019

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# Chapter 1

## Introduction

This master thesis is aiming at the linearization of Power amplifiers with the presence of cross talk in antenna arrays. The tasks includes the characterization of the cross talk and its impact on the system linearity and digital pre-distortion of Power Amplifiers (PA) under effects of antenna cross talks. The project is motivated by the quickly growing need from the mobile communication industry, where highly integrated beam-steerable arrays consisting of a large number of power amplifiers and antenna elements are considered as the solution for higher data rates desired in emerging applications such as self-driving cars, remote e-health etc. There will be use Digital Pre Distortion (DPD) techniques that can capture the total non-linearity of the whole array including the PAs and antenna elements. The special focus is to reduce the system complexity, while maintaining the linearisation performance. This project will be conducted in a way combining mainly measurements together with computation in MATLAB.

The report is divided into 5 sections where the first is this introduction. The second is some basic theory that gives the reader a basic understanding of the measurement that has been done in section 4. Section 3 describes how to mathematically describe a PA and how to linearise it with DPD, a description of crosstalk is also given together with a simple method to capture the non-linearity of the system. To test this model measurement has been provided in section 4 where measurement has been done at a single PA directly connected to a spectrum analyzer. Also two PAs with one antenna each, and four PAs with one antenna each has been measured with a receiver antenna at the spectrum analyzer. Section 5 presents measurement of the farfield and S-parameters of the used antennas to explain the results from section 4.

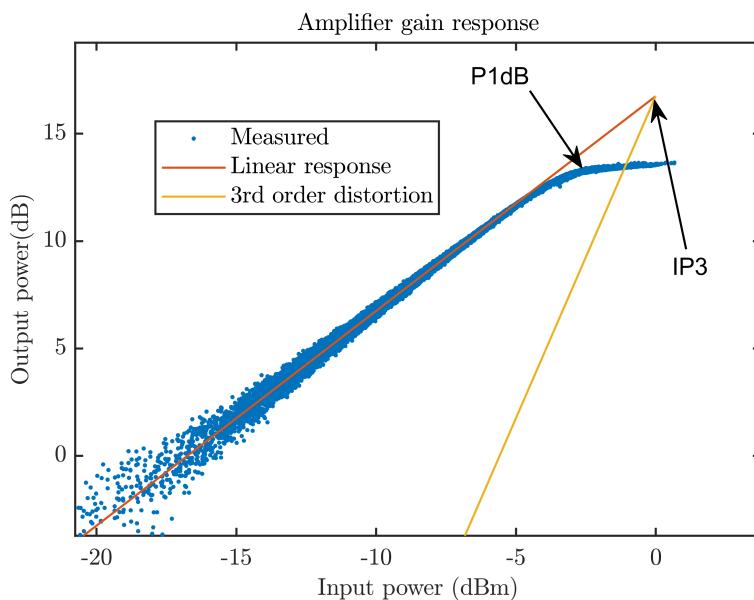


# Chapter 2

## Basic Theory

In this section, some basic theory is given to provide the reader with a basic understanding of the measurement that has been performed in section 4.

### 2.1 Non-linearity



**Figure 2.1:** Amplifier non-linearity

An ideal power amplifier has an linear response over all frequencies and input power. This is depicted in 2.1 as Linear response. Unfortunately this is not true and therefore a measurement of a power amplifier has been done. The measurement shows that the amplifier at some level can be assumed linear, but at a point the amplifier will

saturate due to the supply voltage and the gain will compress. The point where there is 1dB from the linear response to the real response is called the 1dB compression point (P1dB) which is also depicted in the figure. The non-linear gain response causes a distortion at the output which can be described by equation 2.1 [National Instruments, 2019]. If a input-signal using two tones is considered then there will be a difference and a sum of the frequencies presented at the output which is caused by the cubic term in equation 2.3.

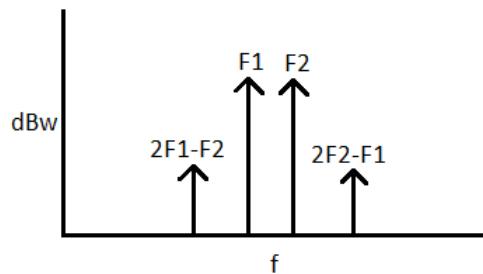
$$V_{out} = a_0 + a_1 V_{in} + a_2 V_{in}^2 + a_3 V_{in}^3 + a_4 V_{in}^4 + \dots \quad (2.1)$$

Where  $V_{out}$  is the output signal from the amplifier,  $a_1, a_2, a_3\dots$  is coefficients describing the ratio of the distortion and  $V_{in}$  is the input signal. If a single tone input is presented, then the output will consist of purely odd and even harmonic distortion.

$$V_{in} = \sin(\omega_1 t) + \sin(\omega_2 t) \quad (2.2)$$

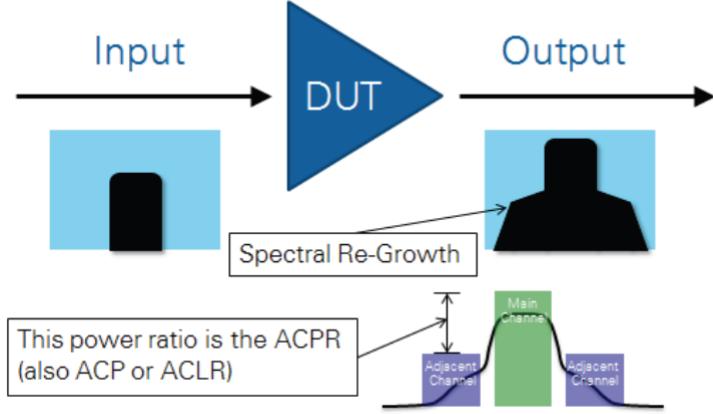
$$V_{out} = a_0 + a_1(\sin(\omega_1 t) + \sin(\omega_2 t)) + a_2(\sin(\omega_1 t) + \sin(\omega_2 t))^2 + a_3(\sin(\omega_1 t) + \sin(\omega_2 t))^3 + \dots \quad (2.3)$$

This is also called Two-Tone Third-Order Intermodulation Distortion and is also depicted in figure 2.1 as 3rd order distortion with a slope of 3:1. It can bee seen that when the output power increases then the 3rd order distortion increases 3 times. A measurement of this is called the third-order-intercept-point (IP3 or TOI). However, the intercept point it not directly measurable since the amplifier reaches compression way before. It can bee seen from figure 2.2 that the distorted component are spaced too close in frequency to be effectively filtered. This will cause distortion into nearby channels and is measured as Adjacent Chennel Power Ratio (ACPR).



**Figure 2.2:** Two-Tone Third-Order Intermodulation Distortion

### Distortion due to non-linearity

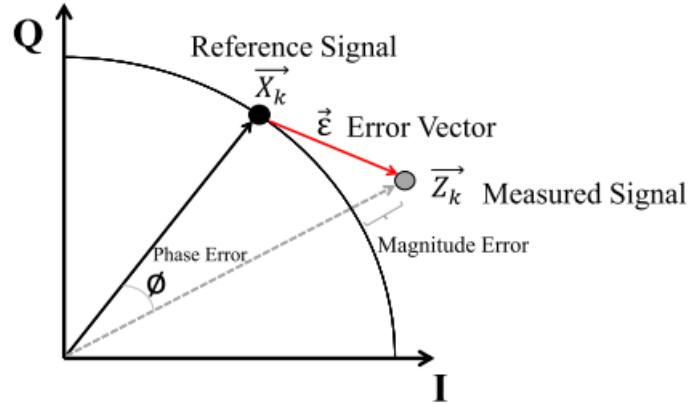


**Figure 2.3:** Graphical Depiction of ACPR in the frequency domain [National Instruments, 2019]

Due to the non-linearity of the PA described before, spectral regrowth will occur which will affect nearby channels. The Adjacent Channel Power Ratio (ACPR) is a measure of the power of the distortion components, caused by the non-linearity of the PA, that are leaked into the adjacent channel see figure 2.3. The formula for the ACPR is given by equation 2.4 and is used after a Fourier transform has been performed at the output signal of the PA.

$$ACPR = \frac{\int_{adjch} |Y(f)|^2 df}{\int_{mainch} |Y(f)|^2 df} \quad (2.4)$$

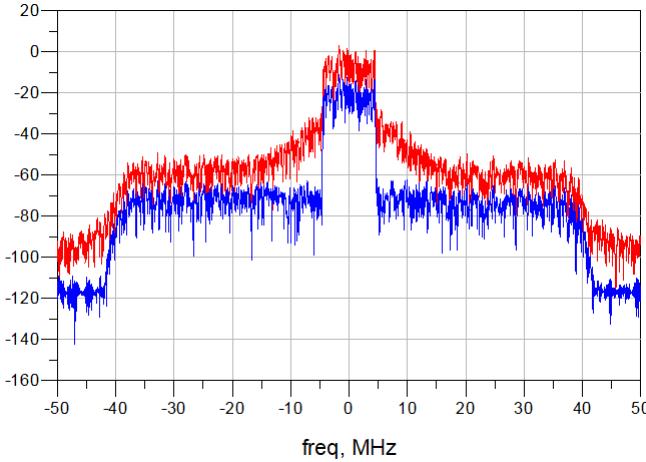
Where  $Y(f)$  is the Fourier transform of the signal, adjch is the adjacent-channel and mainch is the main-channel.



**Figure 2.4:** Graphical view of the EVM

Another measure of the error is the Error Vector Measurement (EVM) or Relative Constellation Error (RCE) which both is a measure of the error due to the constellations points in a IQ plot. If a signal is sent through an amplifier with a given IQ value, then the amplifier will distort those IQ values. The EVM and RCE is a measure of the power of the error vector divided by the power of the reference vector. [Ali Cheaito, et. al, 2016]

$$EVM = \frac{P_{error}}{P_{reference}} = \frac{E[|z(t) - x(t)|^2]}{E[|x(t)|^2]} \quad (2.5)$$



**Figure 2.5:** Destortion simulated in ADS, where blue is input-signal and red is output-signal. The simulation is made with a single amplifier connected to a  $50\Omega$  resistor. It is clearly that the output-signal is distorted. The ACPR becomes  $-45\text{dB}$  with a BW at  $10\text{MHz}$

## 2.2 AM/AM and AM/PM distortion

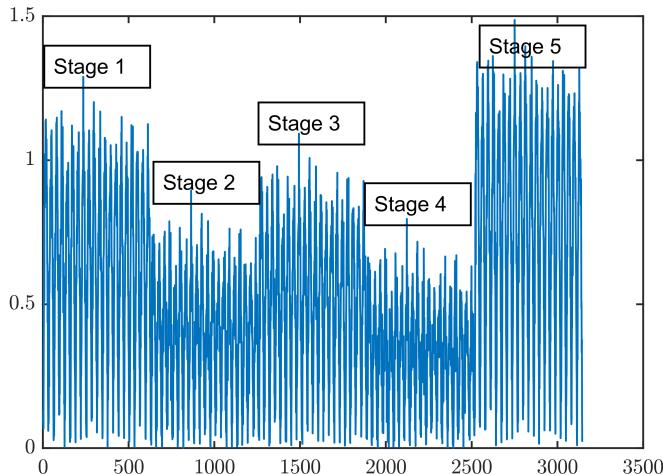
If the input signal to the PA is modelled as equation 2.6

$$x(t) = a(t)e^{j\phi(t)} \quad (2.6)$$

Where  $a(t)$  is the envelope of the signal and  $e^{j\phi(t)}$  is the phase of the input signal. Then the distorted output of the amplifier will be that of equation 2.6 where  $g(t)$  is the amplitude distortion and  $f(t)$  is the phase distortion also called Amplitude to Amplitude (AM/AM) and Amplitude to Phase (AM/PM) distortion. AM/AM distortion can be defined as the deviation from the constant gain when PA is operated in compression region. On the other hand, the increased phase change at compression region can be termed as AM/PM distortion. In presence of wideband signals having non constant amplitude, PA behaves as nonlinear system and exhibits two types of non-linearities which is static distortion and memory effects.

$$y(t) = g(a(t))e^{j\phi(t)+f(a(t))} \quad (2.7)$$

### Memory effects



**Figure 2.6:** Example of amplitude changes at the input of a PA

In modern communication systems, the input power to the PA may be adjusted corresponding to the needs by the network. This makes a sudden increase or decrease in the power as depicted in figure 2.6 which makes the PA work in the transient stage [Yan Guo, et.al, 2015] [Taijun Liu, et.al, 2007]. The transient stage is where the power suddenly increases or decreases to another mean power, whereas the steady state is when the PA operates under stable conditions where the mean power

is constant. When the PA is operated in steady state under a high mean power, the amplifier will begin to dissipate heat. This will cause the internal transistors to operate under a hot state where the characteristic of the transistors will change due to a colder state. If the mean power suddenly is decreased the amplifier will still be hot, but with time the amplifier will cool down and the characteristic will change. This can be called slow memory effects whereas fast memory effects is when the amplifier is driven in its steady state and the parasitics of the components distort the signal. Also antennas at the output of the amplifier has an important role specially if several antennas are connected to form an array. The electrical field will couple to each other and cause fields that will affect the memory effects in the system.

## 2.3 Efficiency

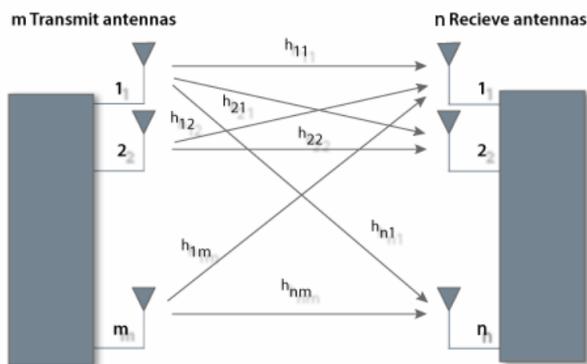
An important measure of an amplifier is its efficiency, specially when the amplifier is located in a battery powered application. The efficiency of a amplifier is given by equation 2.8

$$\eta = \frac{P_{out}}{P_{amplifier} + P_{out}} = \frac{P_{out}}{P_{DC}} \quad (2.8)$$

Where  $P_{out}$  is output power from the amplifier,  $P_{amplifier}$  is power dissipated in the amplifier and  $P_{DC}$  is the power DC consumption. A more common way to express the efficiency is in terms of power added efficiency (PAE) which is a measure of the difference of power between the output and the input signals versus the DC power consumption.

$$PAE = \frac{P_{out} - P_{in}}{P_{DC}} \quad (2.9)$$

## 2.4 Antenna Diversity and MIMO



**Figure 2.7:** Concept of MIMO [Silvus Technologies, 2019]

MIMO (Multiple Input Multiple Output) systems are systems with Multiple Element Antennas at both link ends. The antenna elements of a MIMO system can be used for four different purposes: beamforming, diversity, interference suppression, and spatial multiplexing which is transmission of several data streams in parallel that allows improvement of capacity.[Andreas F. Molisch, 2011] A MIMO system is modelled as in equation 2.10 and is also depicted in figure 2.7.

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n} \quad (2.10)$$

Where  $\mathbf{y}$  is the received vector,  $\mathbf{H}$  is the channel matrix,  $\mathbf{x}$  is the transmitted vector and  $\mathbf{n}$  is noise. The principle of MIMO is to ensure that the same information reaches the receiver on several statistically independent channels. In MIMO systems, several transmits paths is archived by use of several antennas, which gives a spatial separation if they are separated enough to give a correlation factor  $\rho$  that is below  $0.5 - 0.7$  [Andreas F. Molisch, 2011]. The formula for the envelope correlation factor between two antennas is given by equation 2.11. The formula assumes that the WSSUS (Wide-Sense Stationary Uncorrelated Scattering) model is valid, no LOS exists, the power delay profile has an exponential shape, the incident power is isotropically distributed in azimuth and only propagates in the horizontal plane, and an omnidirectional antenna is used.

$$\rho = \frac{J_0^2(k_0 v \tau)}{1 + (2\pi)^2 S_\tau^2 (f_2 - f_1)^2} \quad (2.11)$$

Where  $J_0$  is the Bessel function of the first kind and  $S_\tau$  is the delay-spread of the channels. If the correlation between two antennas is investigated for the same frequency, then the formula can be rewritten as equation 2.12 because  $f_2 - f_1 = 0$ .

$$\rho = J_0^2(2\pi d)^{-1} \quad (2.12)$$

Where  $d$  is the element spacing given in wavelengths. A plot of this can bee seen in figure 2.8.

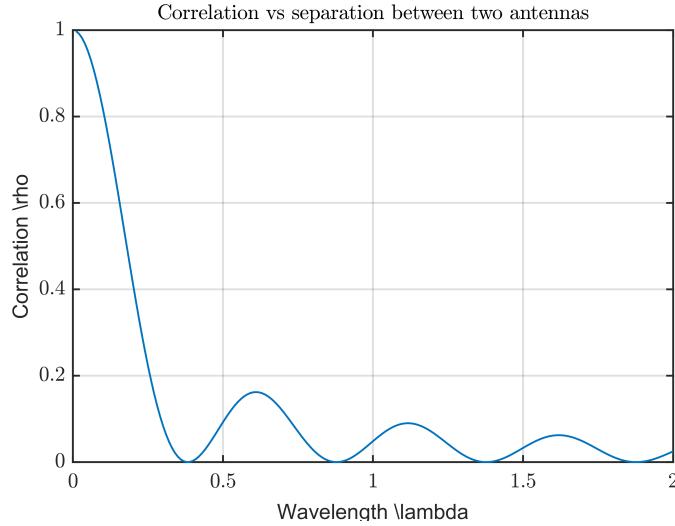


Figure 2.8: Correlation factor for two antennas versus distance

Another method to calculate the correlation factor is to use measured or simulated S-parameters as shown in equation 2.13 [Xuan Wang, et. al, 2011] where  $k$  is the propagation constant and  $d$  the distance in meters.

$$\rho = \frac{A + BJ_0(kd)}{B + AJ_0(kd)} \quad (2.13)$$

$$A = -2Re(S_{12}^*(1 - S_{11})) \quad (2.14)$$

$$B = |1 - S_{11}|^2 + |S_{12}|^2 \quad (2.15)$$

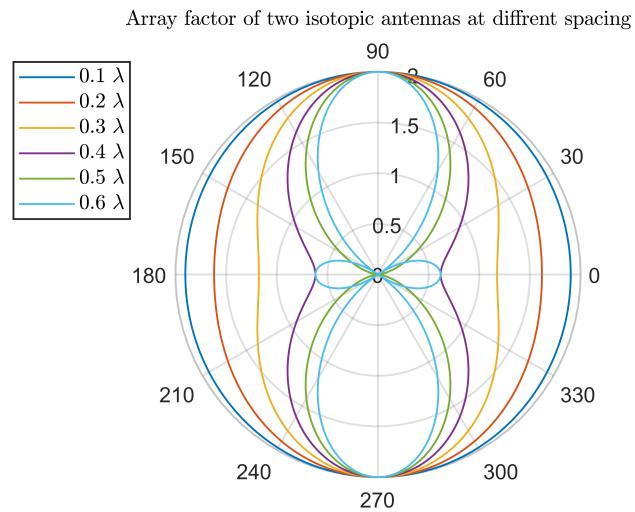
## 2.5 Array factor

When several antennas are spaced relatively close to each other it is called an antenna array. If the antennas are isotropic and are spaced with a quarter wavelength then the array will radiate twice the energy in the direction perpendicular to the array, thou the gain along the array will become zero. A mathematical expression of this is called the array factor (AF).

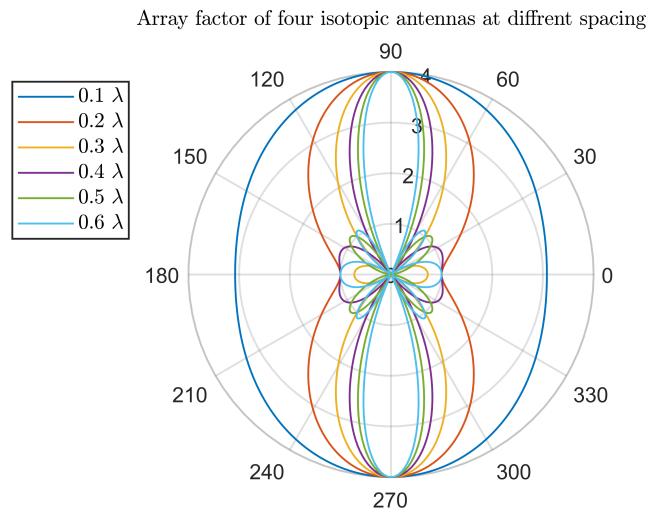
$$AF = \sum_{n=1}^N e^{(nJ2\pi d \cos(\alpha) + JB(n))} \quad (2.16)$$

Where  $N$  is number of antennas in the array,  $d$  is the distance between the antennas,  $\alpha$  is the azimuth angle from  $0..2\pi$  and  $B$  is the feeding phase of a single antenna. In figure 2.9 and 2.10 the array factor for 2 and 4 antennas spaced  $[0.1, 0.2, 0.3, 0.4, 0.5, 0.6]\lambda$  are plotted respectively. It is seen that the energy doubles

in the  $90^\circ$  for all distances in figure 2.9 while it becomes 4 times greater in figure 2.10.



**Figure 2.9:** Array factor of two antennas with different spacing



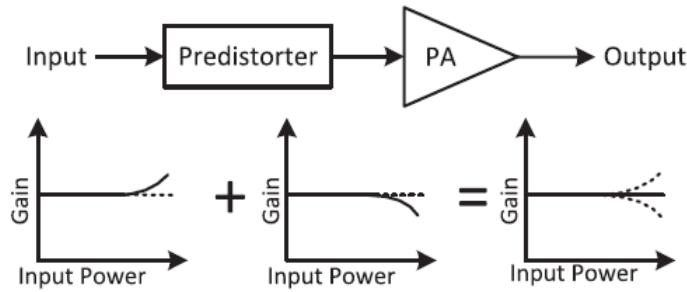
**Figure 2.10:** Array factor of four antennas with different spacing



# Chapter 3

## Amplifier modelling

### 3.1 Pre-distortion



**Figure 3.1:** Concept of predistortion [Yan Guo, et.al, 2015]

In figure 3.1 the concept of Digital Pre-Distortion (DPD) is depicted. DPD is a way to "distort" the incoming signal with the inverse transfer-function of the amplifier. For example the gain of the amplifier is ideally linear in the small-signal region and gets non-linear at higher signal levels. To overcome this, a block called the predistorter inverses this non-linear curve which is the exact inverse of the PA, then a linear amplification can be achieved at the final PA output. But to achieve this inverse of the PA all the non-linear effects have to be accounted for including memory effects.

### 3.2 DPD models

#### Weiner

A simple model to include memory effects is the Weiner model, which consists of a linear filter  $h(m)$  followed by  $a_k$  which is the polynomial coefficients of the non-linearity. The model is given by equation 3.1

$$y_{wiener}(n) = \sum_{k=1}^K a_k \left[ \sum_{m=0}^{M-1} h(m)x(n-m) \right]^k \quad (3.1)$$

It is seen that the output consists of the sum of the non-linear response multiplied with the sum of the input with the former input multiplied with a filter. The Weiner model is one of the simplest ways to combine memory effects with non-linearity but unfortunately it does not provide good results for modelling a power amplifier.

### Hammerstein

Another simple model is the Hammerstein model which is given by equation 3.2

$$y_{hammerstein}(n) = \sum_{m=0}^{M-1} g(m) \sum_{k=1}^K a_k x^k(n-m) \quad (3.2)$$

Which is formed by a non-linearity followed by a linear filter. It is seen that the output consist of the sum of the linear filter  $g(m)$  multiplied with the sum of the filter coefficients  $a_k$  multiplied with the input signal and the former input signal in the power of  $k$ . Yet this filter is simple it does also have it's limitations when it come to modelling of power amplifiers.

### Memory Polynomial

A more used and general model is the memory polynomial given in equation 3.3. The model is a deviation of the Hammerstein model which has proven effective for predistortion of actual power amplifiers under typical operations.

$$y_{mp}(n) = \sum_{k=0}^{K-1} \sum_{m=0}^{M-1} a_{km} x(n-m) |x(n-m)|^k \quad (3.3)$$

where  $a_{km}$  is the filter coefficients,  $x(n)$  is the input,  $M$  is the memory debt and  $k$  is the envelope order.

### Estimation of coefficients

A way to calculate the coefficients for a DPD algorithm is by use of the least-square-type algorithms. The reason for this is that the coefficients are linear weighting of non-linear signals. The easiest way to formulate such a problem is to first collect the coefficients into one  $J \times 1$  vector denoted  $\mathbf{w}$ , where  $J$  is the total number of coefficients. The input can then further be assembled in to a vector denoted  $\mathbf{X}$  which dimensions is  $N \times J$ . The model output can then be expressed by:

$$\hat{\mathbf{y}} = \mathbf{X}\mathbf{w} \quad (3.4)$$

where  $\hat{\mathbf{y}}$  is an  $N \times 1$  vector which is an estimate of the real output  $\mathbf{y}$ . The inverse of this model used for predistortion is then:

$$\hat{\mathbf{x}} = \mathbf{Y}\mathbf{w} \quad (3.5)$$

where the input now is being estimated from the output samples. It is then possible to use the least-squares solution to minimize the estimation error:

$$\mathbf{w} = (\mathbf{Y}^H \mathbf{Y})^{-1} \mathbf{Y}^H \mathbf{x} \quad (3.6)$$

where  $\mathbf{Y}$  is a  $J \times N$  matrix where  $N$  is number of samples. The equation can further be rewritten as:

$$\mathbf{Y}^H \mathbf{Y} \mathbf{w} = \mathbf{Y}^H \mathbf{x} \quad (3.7)$$

This equation can easily be solved by MATLAB using the "backslash" operator (\) by Cholesky decomposition and forward/backward substitution.

### Estimation in MATLAB

If an input and output signal is measured and imported into MATLAB and called  $\mathbf{x}$  and  $\mathbf{y}$  respectively, then a for-loop can do the  $\mathbf{Y}$  matrix. Next we need to remove M sampels from  $\mathbf{x}$  because of the time delay, then the substitution to find  $\mathbf{w}$  using the (\) operator can be done. The code is given below:

```
K = 5;%envelope order
M = 8;%memory debth

Y = [];% init matrix
for m = 1:M
    for k = 1:K
        Y(:, end+1) = (y(m: end-M+m).* abs(y(m: end-M+m)).^(k-1));
    end
end

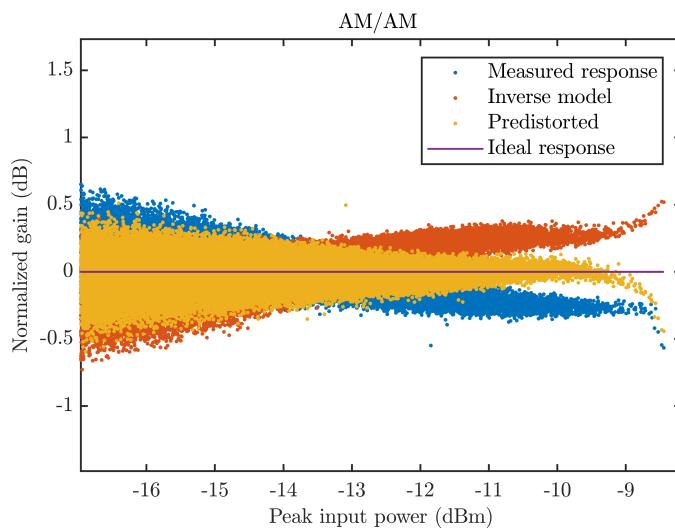
w = Y\y(M: end);%Do the regression
x_est = Y*w;%estimated input
error = mean(abs(x(M: end)-x_est))
```

Now equation 3.5 must be used to obtain the inverse model:

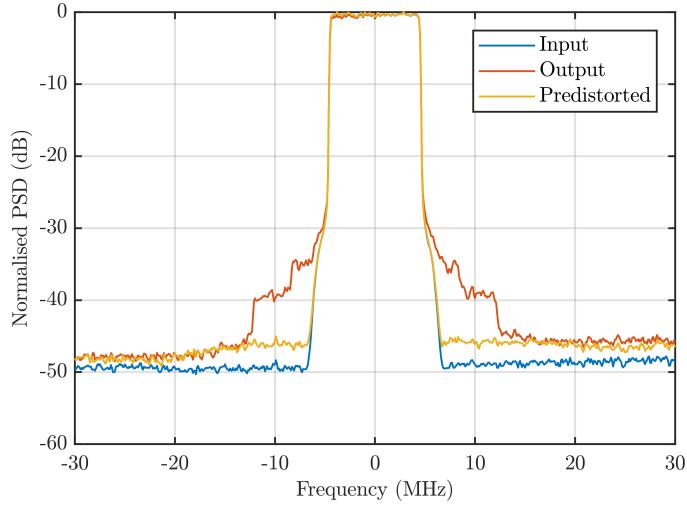
```
X = [];% init matrix
for m = 1:M
    for k = 1:K
        X(:, end+1) = (x(m: end-M+m).* abs(x(m: end-M+m)).^(k-1));
    end
end

x_inv = X*w;%inverse model
```

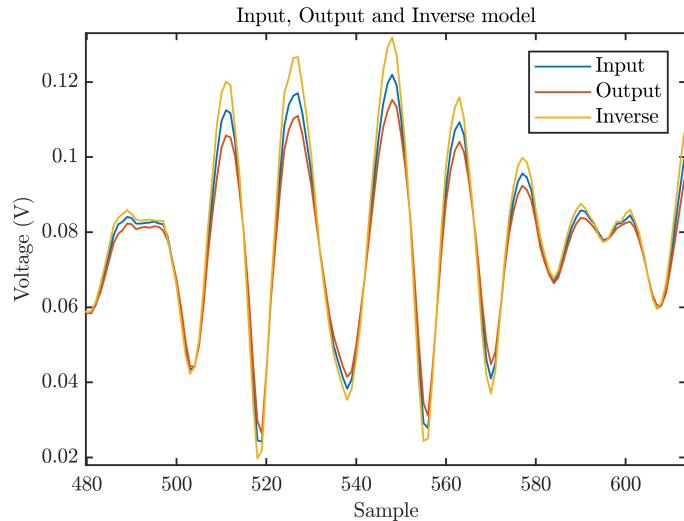
In figure 3.2 a AM/AM plot is depicted of measurements done at an amplifier. The plot shows how the output (blue) is driven in its non-linear region. Then the inverse model (red) inverses this non-linearity and when this signal is presented at the input of the amplifier, then the response will become close to linear (yellow). The reason that it still reaches some level of compression is because of the limit of the supply-voltage to the amplifier. A PSD of the same measurements is depicted in figure 3.3. From that it is easy to see how the pre-distorted signal lowers the distortion. From figure 3.4 a plot of the absolute value of the I and Q baseband values is depicted. It is clearly seen that the output is a non-linear response of the input and that the inverse model is compensating for the gain error.



**Figure 3.2:** AM/AM plot of measured response and inverse model



**Figure 3.3:** PSD of output measured at amplifier close to it's compression point and output at same power level but with predistortion.



**Figure 3.4:** Absolute value of baseband I and Q values

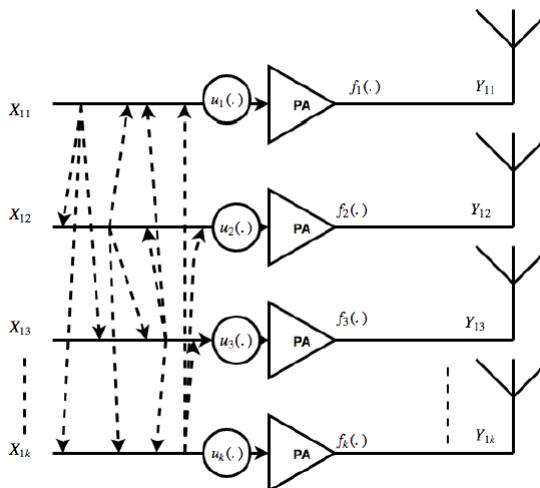
### 3.3 Crosstalk

Crosstalk is coupling from one branch to another branch. When only a signal is present on a single branch, no crosstalk would appear to this branch. On the other hand if a signal is presented at two branches then crosstalk would appear to both of them. There exist three types of crosstalk which is: Crosstalk before the PA's, see figure 3.5, Crosstalk after the PA's, see figure 3.6 and Crosstalk on the antennas and

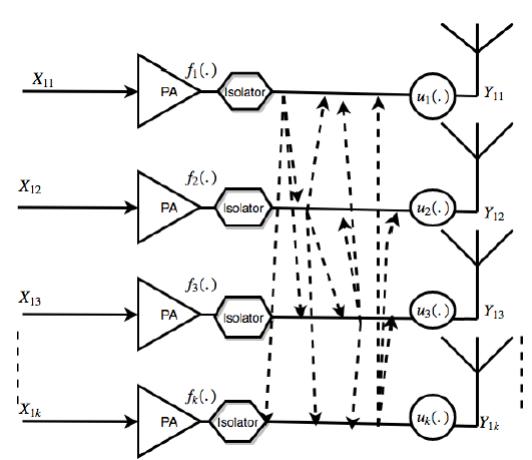
mishmash due to coupling. Crosstalk before the PA is also called nonlinear since it is amplified by the non linear PA. The nonlinear crosstalk and the PA nonlinear response should be jointly compensated by a predistorter to get a reliable system performance [Zahidul Islam Shahin, et. al, 2017] denoted  $\mu_k(\cdot)$ . The output from the branches would become that of equation 3.8.

$$Y_{1k} = fk(uk(X_{11}, X_{12}, X_{13}, X_{1k})) \quad (3.8)$$

Where X is the input signal, Y is the output and  $fk$  is the PA response.



**Figure 3.5:** Crosstalk before PA [Zahidul Islam Shahin, et. al, 2017]

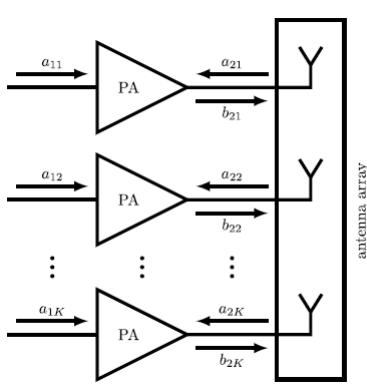


**Figure 3.6:** Crosstalk after PA [Zahidul Islam Shahin, et. al, 2017]

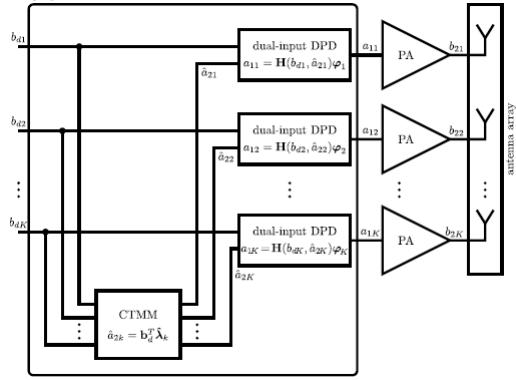
Crosstalk after the PA is called linear since it has an linear impact. In figure 3.6 the output of the amplifier is connected to an isolator, which makes the output unaffected by reflections. A linear model can therefore be used which is shown in equation 3.9.

$$Y_{1k} = \mu_k(f1(X_{11}), f2(X_{12}), f3(X_{13})..fk(X_{1k})) \quad (3.9)$$

When no isolators is presented the output will now be affected by the crosstalk or mutual-coupling between the antennas. A sketch of this is depicted in figure 3.7 where  $a_{1k}$  is the incoming signal to the amplifier,  $b_{2k}$  is the output from the amplifier and  $a_{2k}$  is the reflected signal form the antenna array at the k'th branch [Katharina Hausmair, et. al, 2017]. The relation between  $a_{2k}$  and the output signals  $b_{2k}$  is determined by the characteristics of the antenna arrays S-parameters. The system model of the multi-antenna transmitter can, therefore, be split in to a crosstalk and mismatch model (CTMM). This block can further be used together with a dual-input-DPD which holds the model for the PA, see figure 3.8.



**Figure 3.7:** Model of the antenna crosstalk [Katharina Hausmair, et. al, 2017]

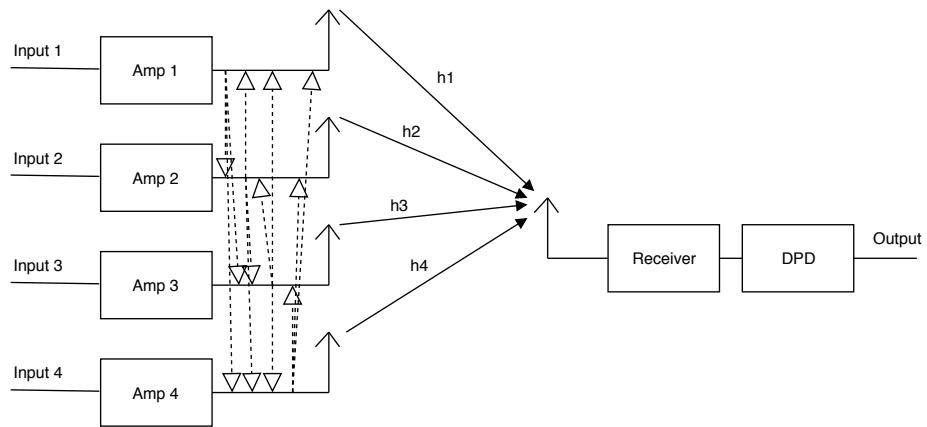


**Figure 3.8:** The predistortion method consists of two main blocks: one linear CTMM block for the whole transmitter and a dual-input DPD block in every transmit path. [Katharina Hausmair, et. al, 2017]

The CTMM describe the crosstalk and mishmash signals  $a_{2k}$  as a function of the PA output  $b_{2k}$ . A mathematical model of this is shown in equation 3.10.

$$a_{2k} = \sum_{i=1}^K \lambda_{ki} b_{2i} = \mathbf{b}_2^T \boldsymbol{\lambda}_k \quad (3.10)$$

Where  $\mathbf{b}_2 = [b_{21}, \dots, b_{2K}]^T$  are complex coefficients describing the input to the antenna and  $\boldsymbol{\lambda}_k = [\lambda_{k1}, \dots, \lambda_{kK}]^T$  are complex coefficients describing the reflection from the antenna, which also corresponds to S-parameters. The Dual-Input PA Model is then a function of the signals  $a_{1k}$  and  $a_{2k}$  which becomes a lengthy equation that is not further described here. The model can be found in [Katharina Hausmair, et. al, 2017]. Its has been found that the approach is capable of reducing the ACPR of a measurement setup using 4-Tx antennas from -36.3dB to -50.7dB which is nearly distortion free. The problem with the model is that the S-parameters for the antennas has to be known and that the method needs feedback from each amplifier. This is a large problem if several amplifiers are used since it will increase complexity in the layout and also if the S-parameters cannot be measured it introduces another problem. A solution to this problem can be to treat the amplifiers with antennas as one system and then do the DPD at the receiver side as depicted in figure 3.9. In order to make this configuration to work, the transmitter side has to send a pilot sequence to the receiver that is known for the receiver. Then the receiver can obtain the coefficients for the DPD algorithm and then do the estimation of the signal itself or it can transmit the DPD coefficients to the transmitter. The benefits with this approach is that also the channel is taken into account. Another problem that can be omitted with this approach is that when doing DPD in the conventional way, the amplifier has to act identical to the pre distorted signal that it did to the non-distorted which not always come true.



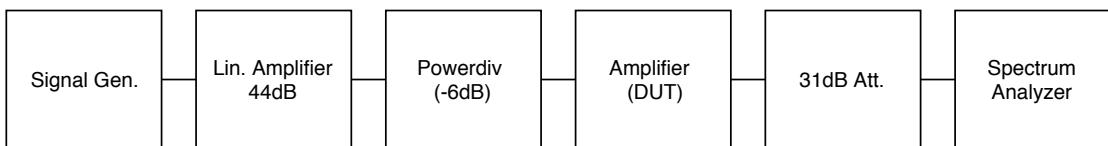
**Figure 3.9:** Estimation of the DPD coefficients at receiver side.

## Chapter 4

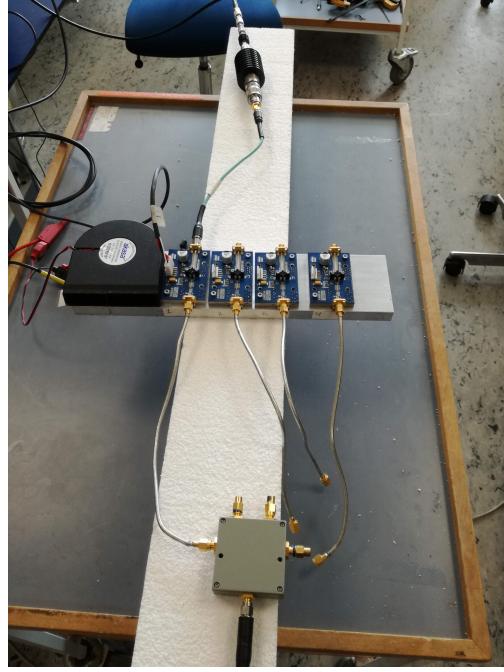
# Measurement

### 4.1 Amplifier

The amplifier used for measurements is a CGH400006P 6W RF Power GaN HEMT transistor mounted at a development board for this transistor type, driven in class AB. The Transistor has a specified mean gain at 13dB and a maximum output at 32dBm which gives a maximum input at 19dBm. This is a large amount of power to deliver for a signal generator so in order to protect the equipment an amplifier has been connected to the output. With cable loss taken into account the amplifier has a gain at 44dB. Futher after the amplifier a four port power divider has been connected to prepare the measurement setup to connect several amplifiers. A block diagram of the setup is depicted in figure 4.1. The output of the amplifier is connected to a 31dBm attenuator to ensure that the spectrum analyser is operated under safe conditions. The signal generator generates a input signal that is a 10MHz LTE signal with a baseband frequency at 3.5GHz.

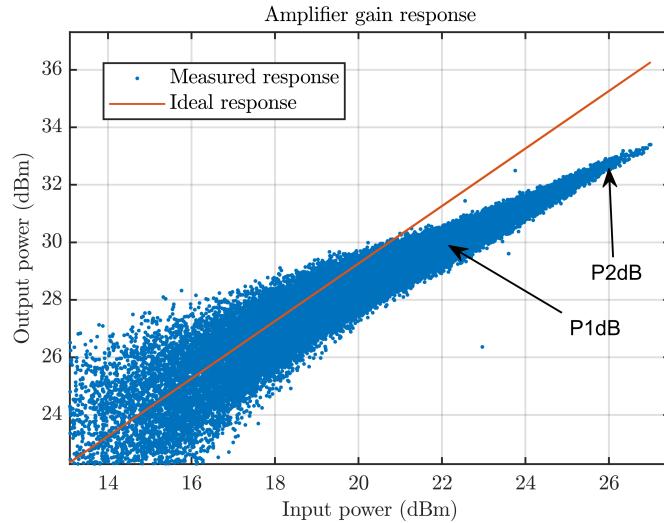


**Figure 4.1:** Measurement setup for measurement at only the amplifier



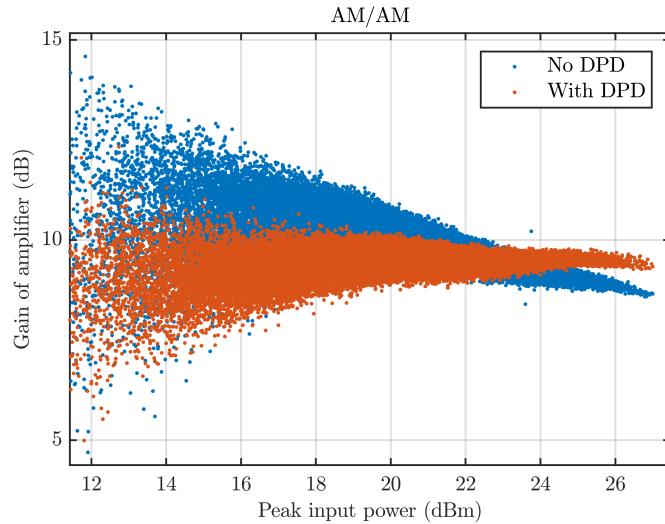
**Figure 4.2:** Picture of the measurement setup

In order to use DPD at the amplifier, it is important to drive the amplifier at its 1dB compression point or more. Therefore the first measurement that has to be done is to measure the gain response of the amplifier to find the input power level that satisfies this. The gate voltage for the amplifier is  $V_g = 2.798V$  and the drain current is  $I_d = 100mA$ . The result are depicted in figure 4.3.

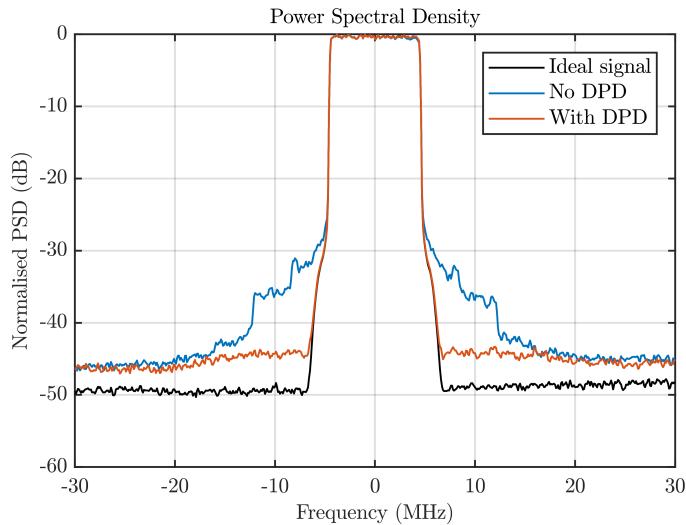


**Figure 4.3:** Measured gain response of the amplifier with a 10MHz LTE signal at 3.5GHz

It can be seen from figure 4.3 that the amplifier in this setup, has a gain about 10dB. The 1dB compression point is at 22dBm input power and 2dB compression is at 26dBm. It is therefore decided to continue with a power level that has a peak input power of 27dBm. The DPD algorithm has therefore been applied and the result can be seen in figure 4.4 and 4.5. It can be seen that the DPD works fine and that the distortion becomes lower with the DPD as expected. It can be seen from the AM/AM plot that the gain is lowered to 9dB with the DPD but that compression is avoided.

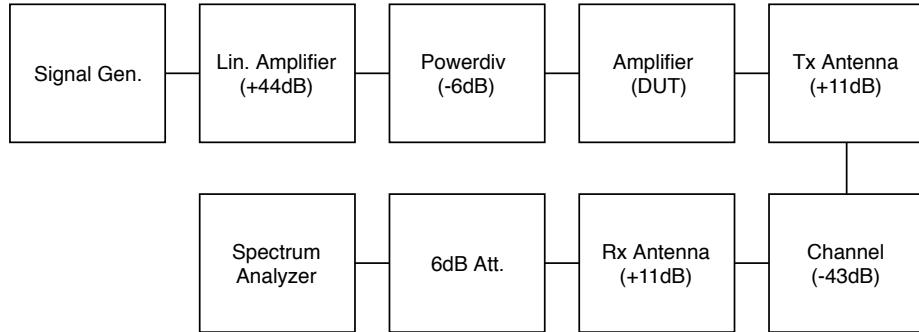


**Figure 4.4:** AM/AM response of the amplifier with and without DPD



**Figure 4.5:** Measured PSD with and without DPD

## 4.2 One amplifier one antenna

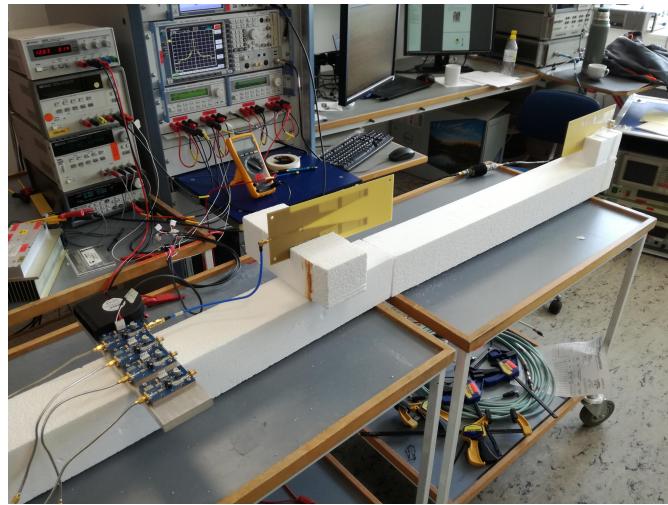


**Figure 4.6:** Measurement setup for measurement at one amplifier with one Tx and one Rx antenna

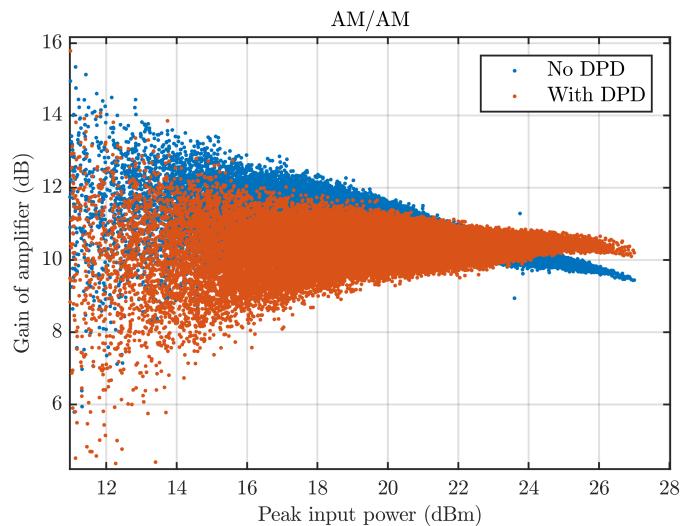
Since now it has been proven that the DPD works well for a single amplifier connected to a fixed load, it is necessary to see if there would be any changes when the amplifier is connected to a single Tx antenna. The measurement setup is depicted in figure 4.6. The output of the amplifier is connected to one Tx antenna with a gain at 11dB. The Rx antenna are spaced 1m apart which gives loss at 43dB in free space. The total loss can be calculated as:

$$L_{dB} = 20\log_{10}(d) + 20\log_{10}(f) + 20\log_{10}\left(\frac{4\pi}{c}\right) + G_t + G_r = 21.3dB \quad (4.1)$$

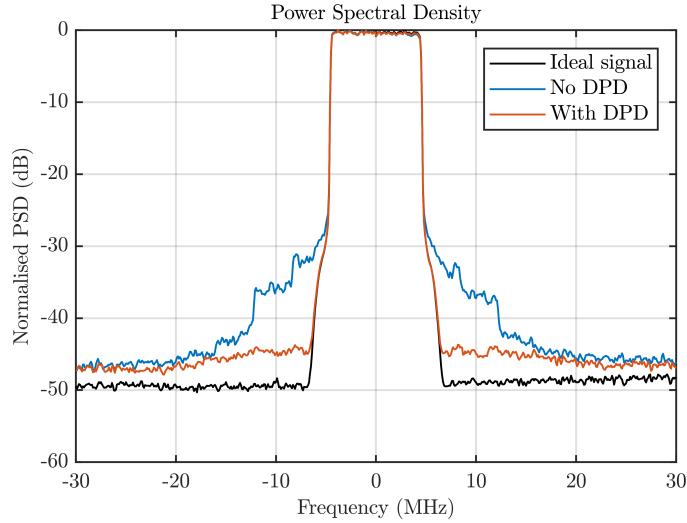
Where  $d$  is distance between the antennas,  $f$  is the center frequency,  $c = 3.0e8$  is the speed of light and  $G_t$   $G_r$  is the gain of the transmitting antenna and receiving antenna respectively [Constantine A. Balanis, 2005]. In order to compensate for the loss and to drive the spectrum analyser in the same power level as in the former measurement, the attenuator has been reduced to 6dB. It is seen from figure 4.8 that the gain now is close to 10dB which is caused by the compensation for the free space loss that is not correct but close. The distortion seen in figure 4.9 is lowered with DPD and therefore it can be concluded that the DPD still works with one antenna connected to the amplifier. The model used for DPD is the model for the amplifier only.



**Figure 4.7:** Picture of the measurement setup for one amplifier with one Tx and one Rx antenna

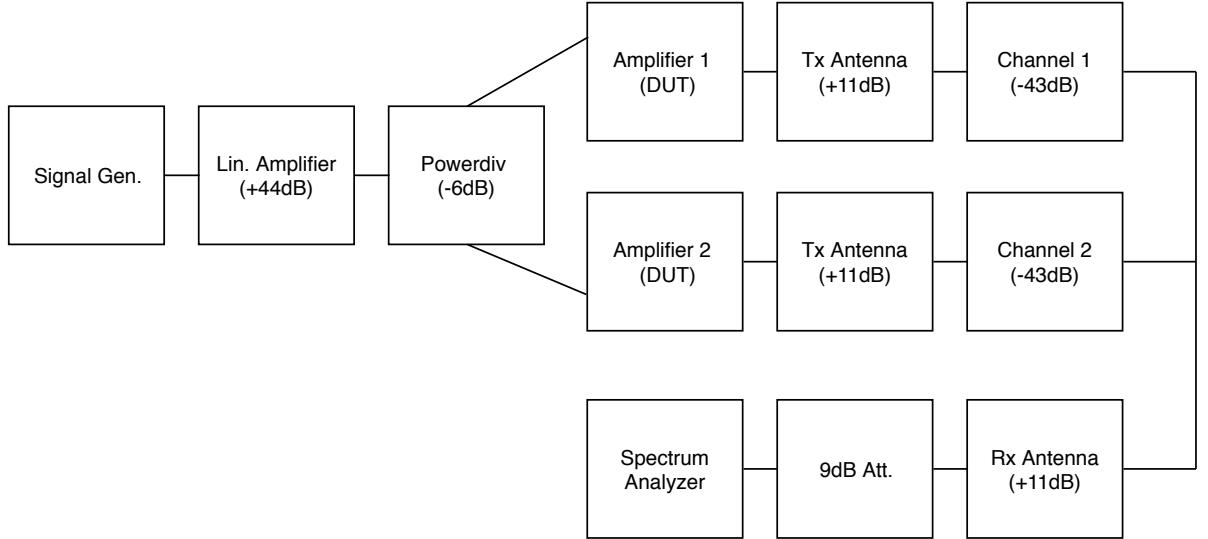


**Figure 4.8:** AM/AM response of the amplifier with and without DPD using one Tx antenna



**Figure 4.9:** Measured PSD with and without DPD using one Tx antenna

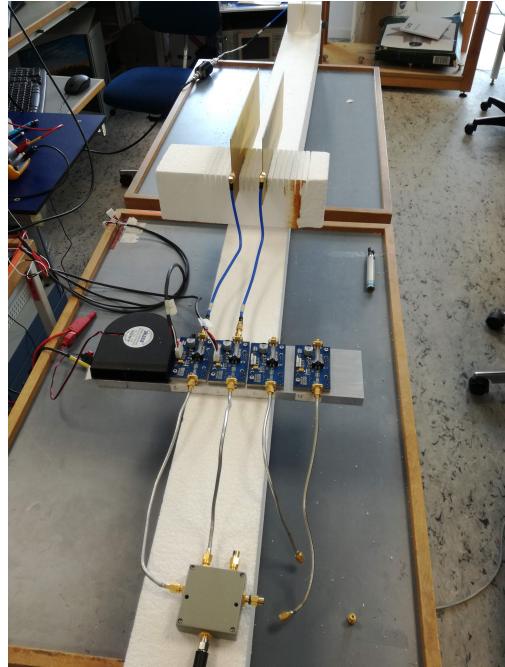
### 4.3 Two amplifiers two antennas



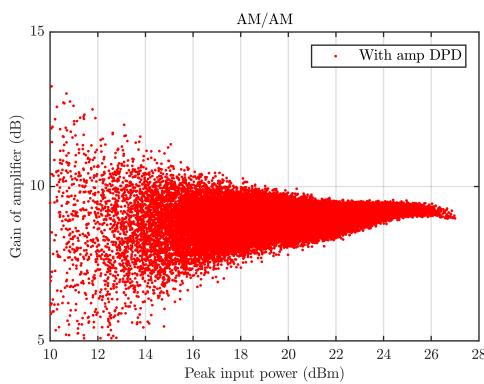
**Figure 4.10:** Measurement setup for measurement at two amplifiers with two Tx and one Rx antenna

In this section it is measured if it has an impact if two amplifiers are connected to an antenna each, spaced at different distances. The measurement setup is depicted in figure 4.10. Since the extra amplifier and antenna will introduce 3dB more power, 3dB is added to the attenuator to ensure the same power level at the input to the

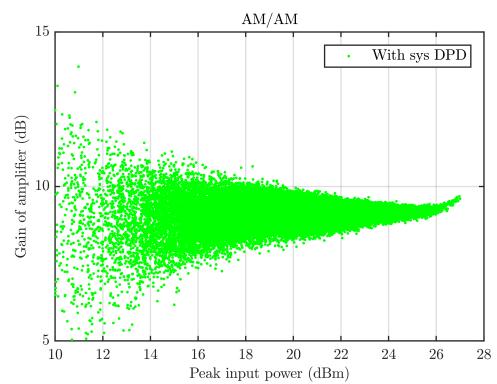
spectrum analyzer. The measurements has all been done at the same powerlevel but the distances of the antennas are varied from 0.1 wavelength to 0.6 in steps of 0.1. First a measurement of the system is done without DPD for all distances, where the measured signal is imported into MATLAB and an inverse signal is generated. This inverse signal is then uploaded to the signal generator and the new measurement is called "With sys DPD" for each distance. Then a measurement with the inverse signal in the former section is applied for each distance and the measured signal is then called "With amp DPD". The results can be seen from figure 4.12 to 4.19.



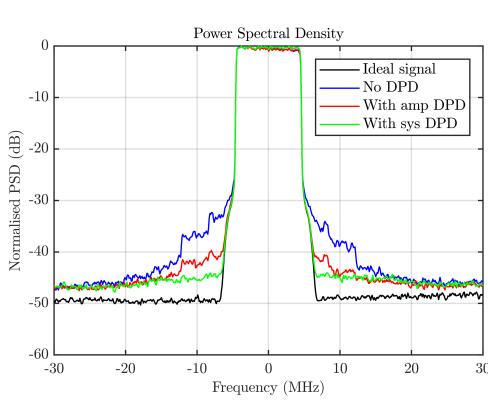
**Figure 4.11:** Picture of measurement setup using two Tx antennas



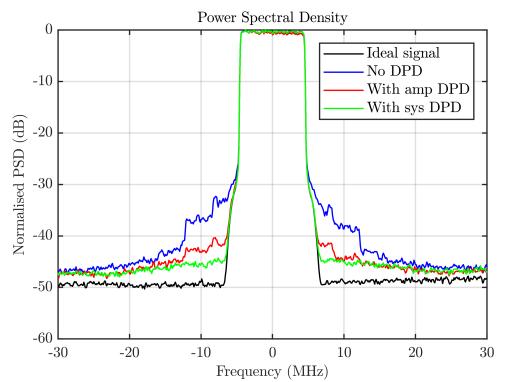
**Figure 4.12:** AM/AM distortion at  $d = 0.1\lambda$  with amplifier DPD



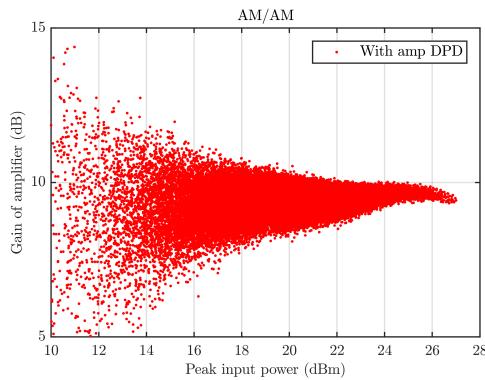
**Figure 4.13:** AM/AM distortion at  $d = 0.1\lambda$  with system DPD



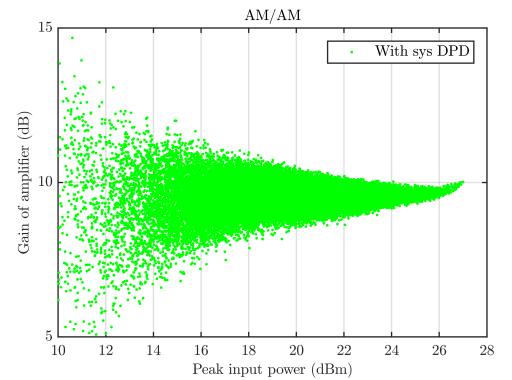
**Figure 4.14:** PSD of measurement at  $d = 0.1\lambda$



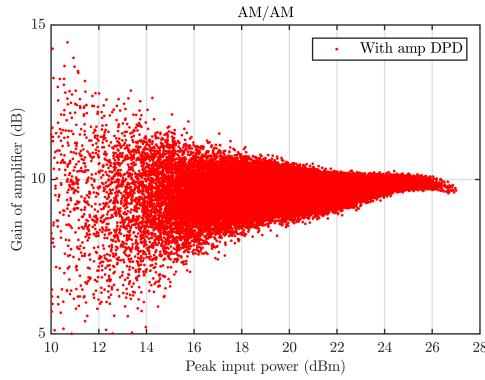
**Figure 4.15:** PSD of measurement at  $d = 0.2\lambda$



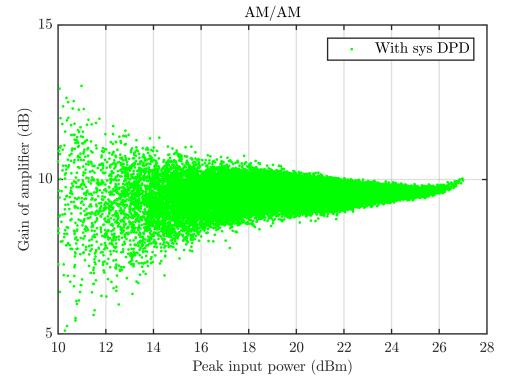
**Figure 4.16:** AM/AM distortion at  $d = 0.2\lambda$  with amplifier DPD



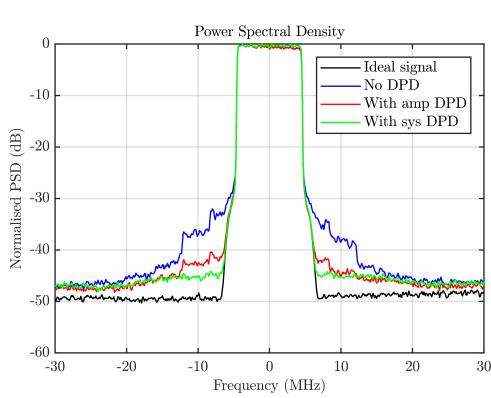
**Figure 4.17:** AM/AM distortion at  $d = 0.2\lambda$  with system DPD



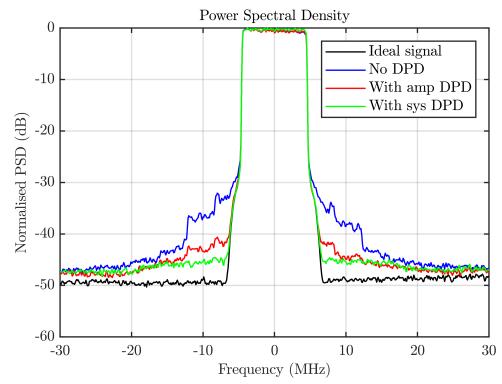
**Figure 4.18:** AM/AM distortion at  $d = 0.3\lambda$  with amplifier DPD



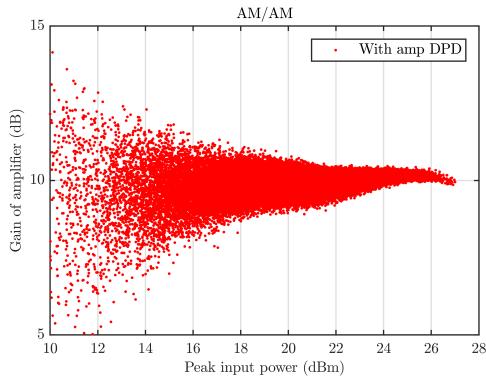
**Figure 4.19:** AM/AM distortion at  $d = 0.3\lambda$  with system DPD



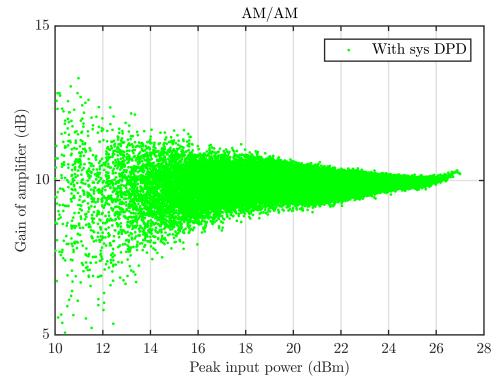
**Figure 4.20:** PSD of measurement at  $d = 0.3\lambda$



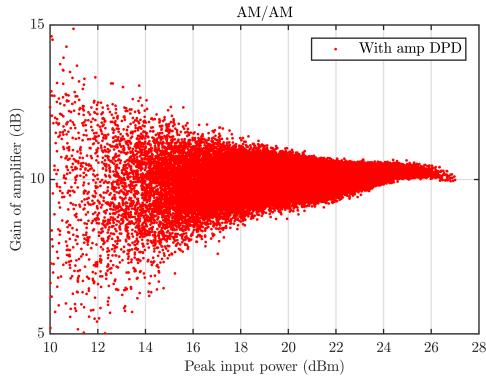
**Figure 4.21:** PSD of measurement at  $d = 0.4\lambda$



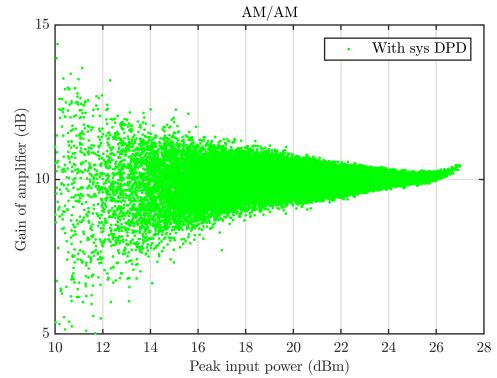
**Figure 4.22:** AM/AM distortion at  $d = 0.4\lambda$  with amplifier DPD



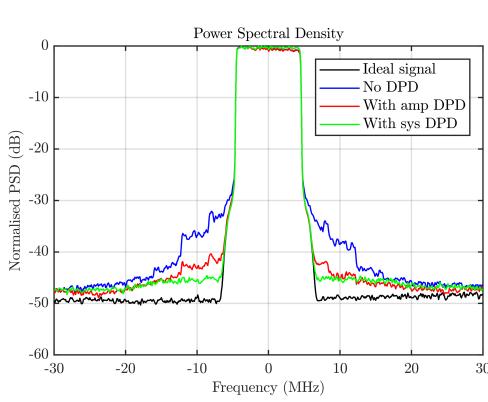
**Figure 4.23:** AM/AM distortion at  $d = 0.4\lambda$  with system DPD



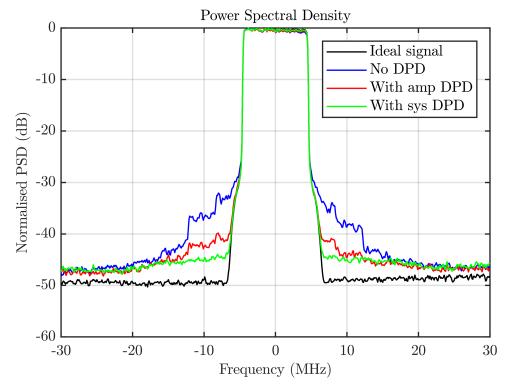
**Figure 4.24:** AM/AM distortion at  $d = 0.5\lambda$  with amplifier DPD



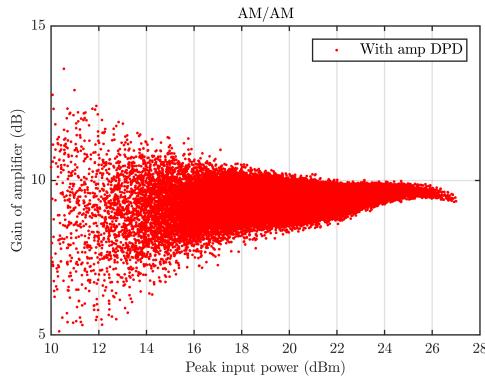
**Figure 4.25:** AM/AM distortion at  $d = 0.5\lambda$  with system DPD



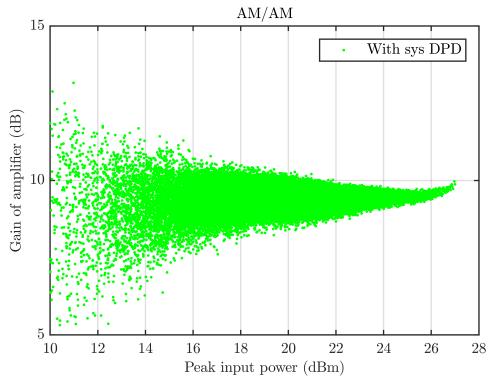
**Figure 4.26:** PSD of measurement at  $d = 0.5\lambda$



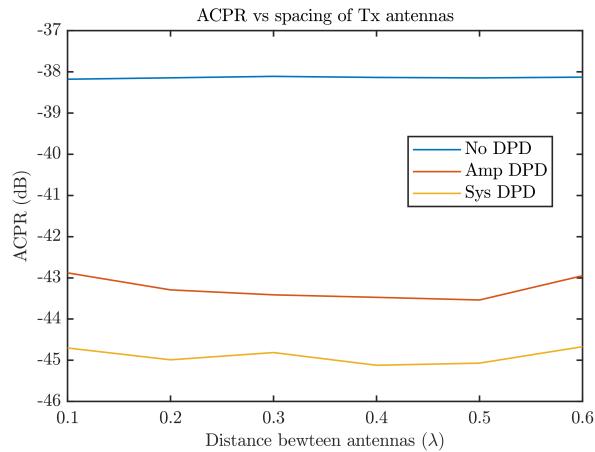
**Figure 4.27:** PSD of measurement at  $d = 0.6\lambda$



**Figure 4.28:** AM/AM distortion at  $d = 0.6\lambda$  with amplifier DPD



**Figure 4.29:** AM/AM distortion at  $d = 0.6\lambda$  with system DPD

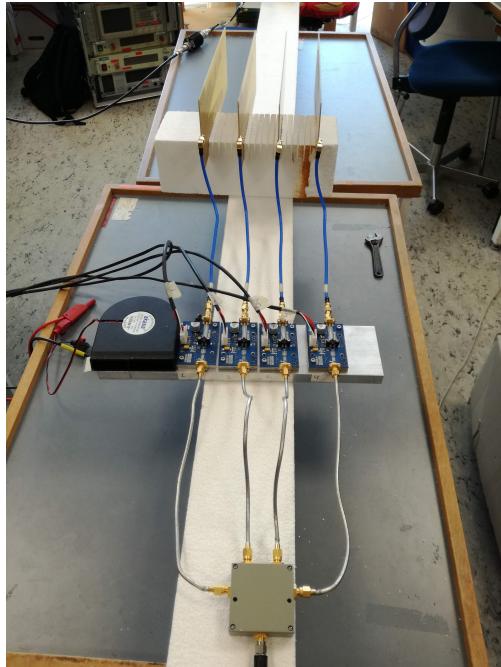


**Figure 4.30:** ACPR versus distance between antennas

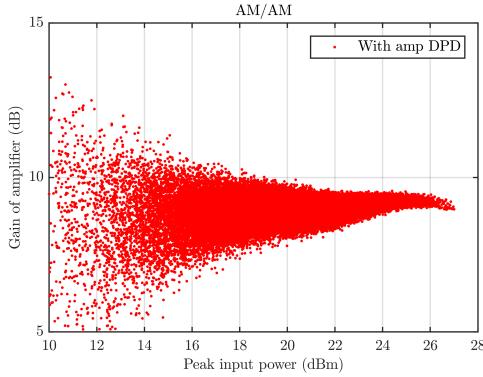
From the AM/AM plots it can be seen that when doing DPD with only the model for the amplifier taken into account, there are lots of non-linearity about 22-27dBm input. When treating the amplifiers with antennas as one model the AM/AM linearity is improved but it seems that the DPD algorithm tends to overcompensate at high power values. From the PSD plots it is seen that the ACPR is decreased when treating the setup as one model. This can also be seen in figure 4.30 where the ACPR is shown for the different distances. It is seen that the ACPR changes due to the distance between the antennas. This is caused by the gain difference in the antenna array, where the highest gain is at  $0.5\lambda$  which then has the lowest ACPR. The antenna measurement is presented in section 5.

#### 4.4 Four amplifiers four antennas

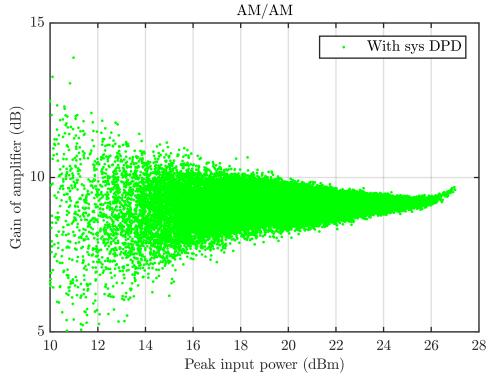
In this section measurement is done at four amplifiers and four antennas. The setup for the measurement is the same as in figure 4.6 but with four amplifier chains instead of two. The results are shown in figure 4.31 to 4.49.



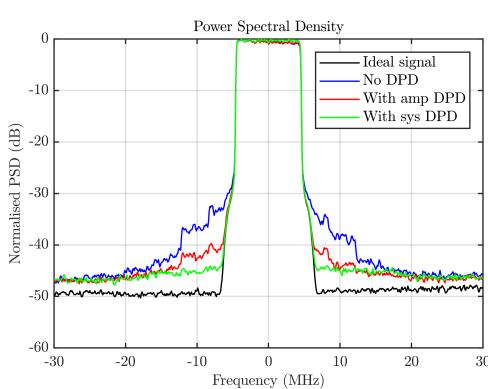
**Figure 4.31:** Picture of measurement setup using four Tx antennas



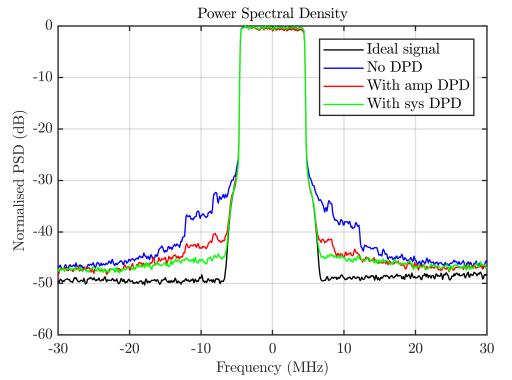
**Figure 4.32:** AM/AM distortion at  $d = 0.1\lambda$  with amplifier DPD



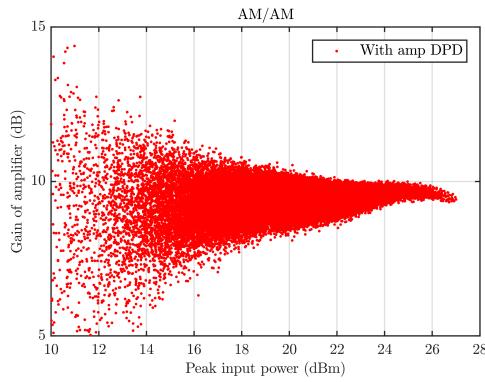
**Figure 4.33:** AM/AM distortion at  $d = 0.1\lambda$  with system DPD



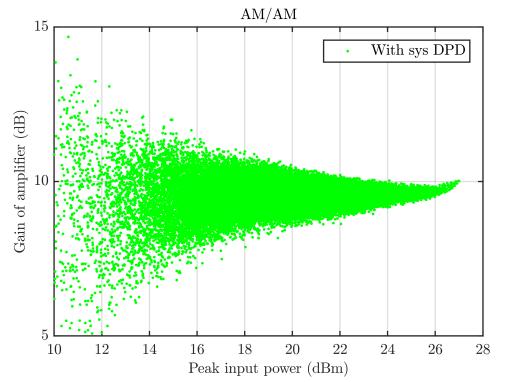
**Figure 4.34:** PSD of measurement at  $d = 0.1\lambda$



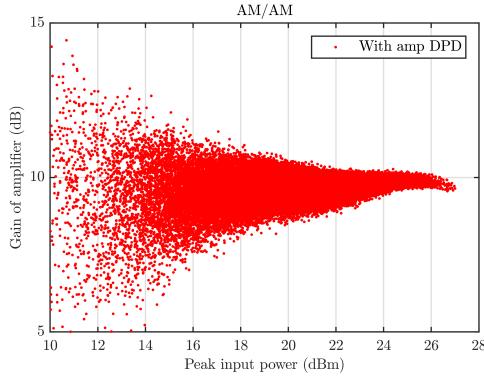
**Figure 4.35:** PSD of measurement at  $d = 0.2\lambda$



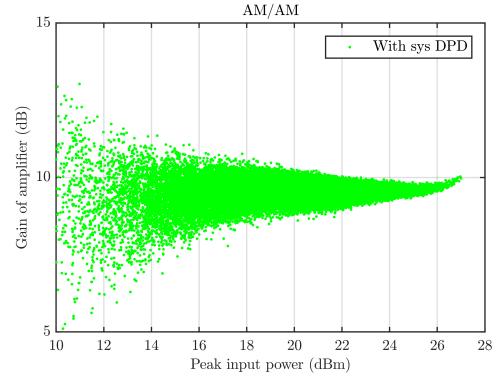
**Figure 4.36:** AM/AM distortion at  $d = 0.2\lambda$  with amplifier DPD



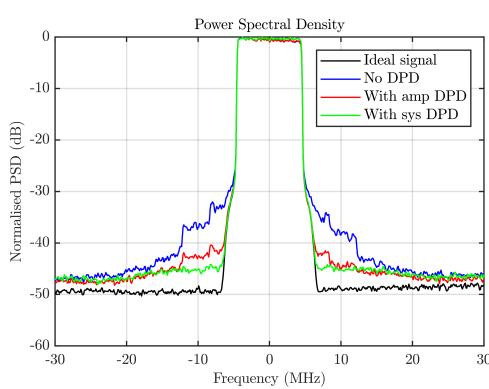
**Figure 4.37:** AM/AM distortion at  $d = 0.2\lambda$  with system DPD



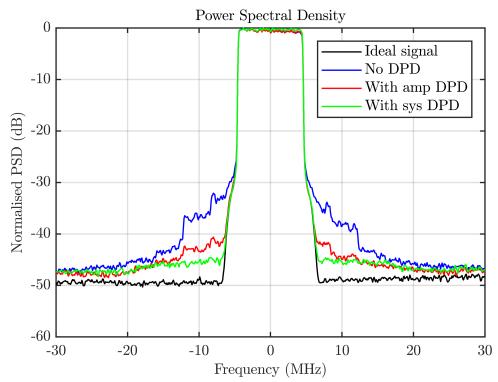
**Figure 4.38:** AM/AM distortion at  $d = 0.3\lambda$  with amplifier DPD



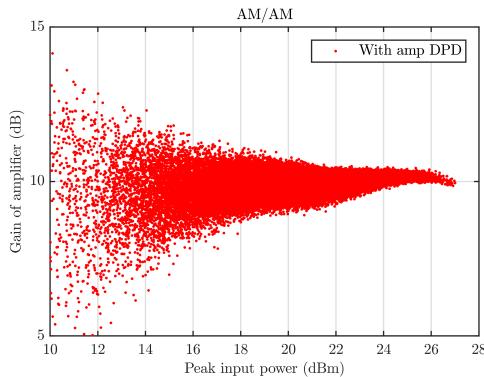
**Figure 4.39:** AM/AM distortion at  $d = 0.3\lambda$  with system DPD



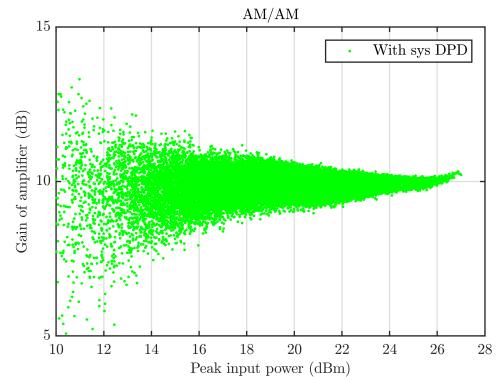
**Figure 4.40:** PSD of measurement at  $d = 0.3\lambda$



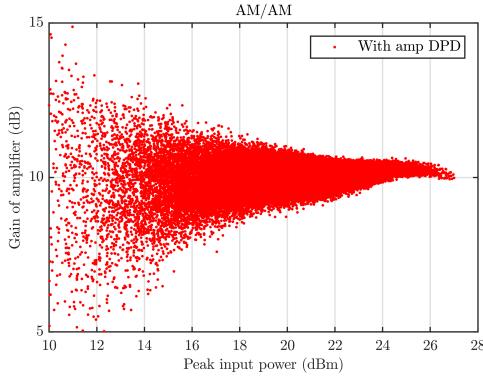
**Figure 4.41:** PSD of measurement at  $d = 0.4\lambda$



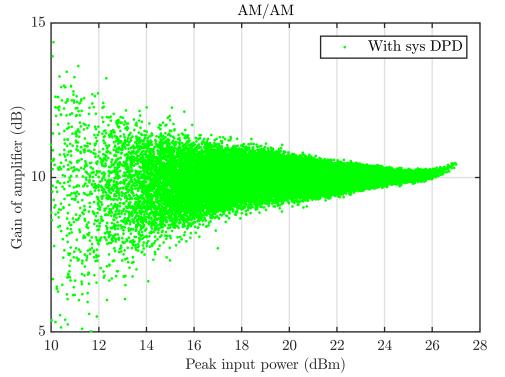
**Figure 4.42:** AM/AM distortion at  $d = 0.4\lambda$  with amplifier DPD



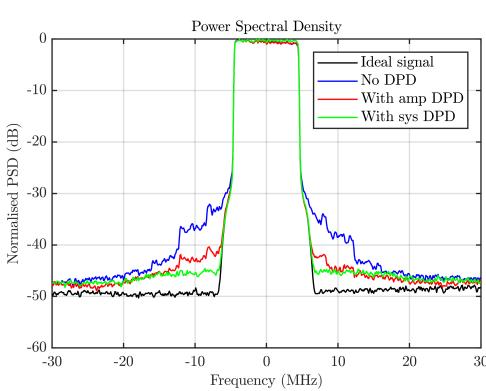
**Figure 4.43:** AM/AM distortion at  $d = 0.4\lambda$  with system DPD



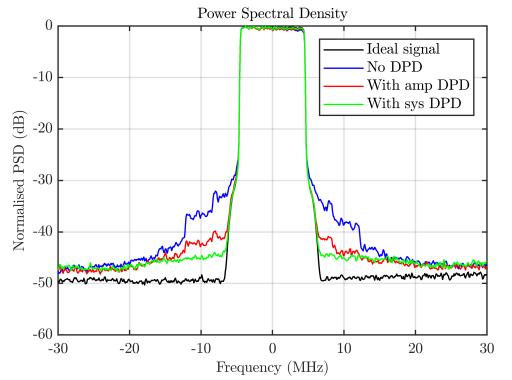
**Figure 4.44:** AM/AM distortion at  $d = 0.5\lambda$  with amplifier DPD



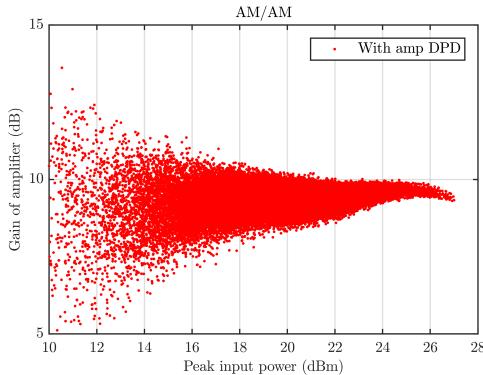
**Figure 4.45:** AM/AM distortion at  $d = 0.5\lambda$  with system DPD



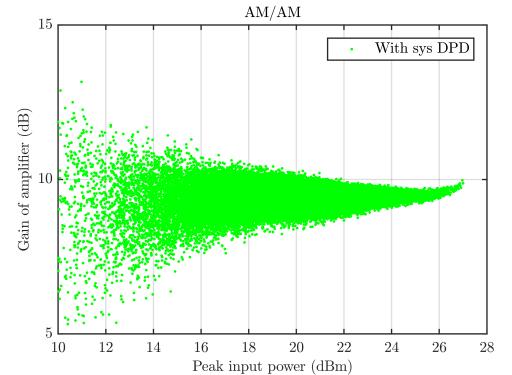
**Figure 4.46:** PSD of measurement at  $d = 0.5\lambda$



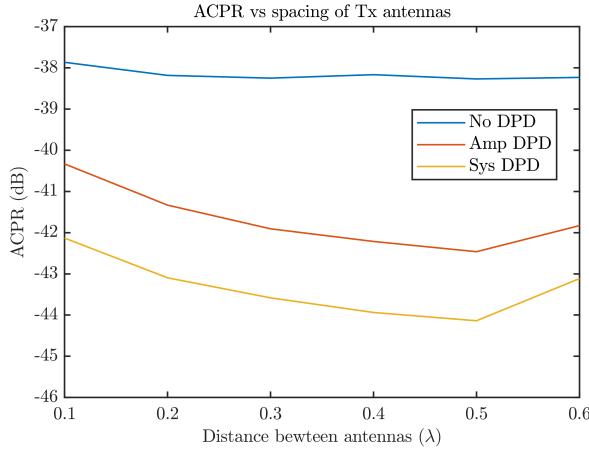
**Figure 4.47:** PSD of measurement at  $d = 0.6\lambda$



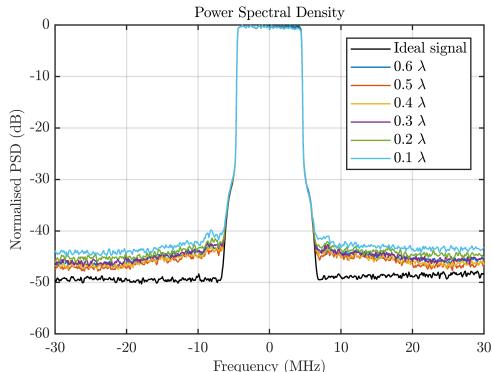
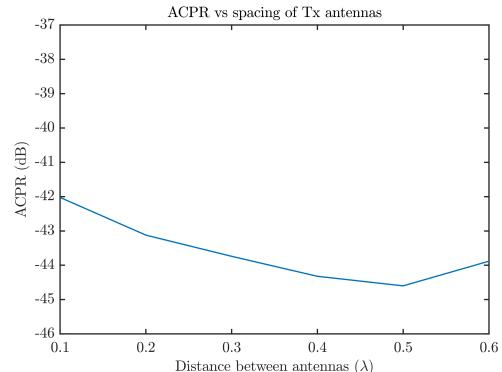
**Figure 4.48:** AM/AM distortion at  $d = 0.6\lambda$  with amplifier DPD



**Figure 4.49:** AM/AM distortion at  $d = 0.6\lambda$  with system DPD

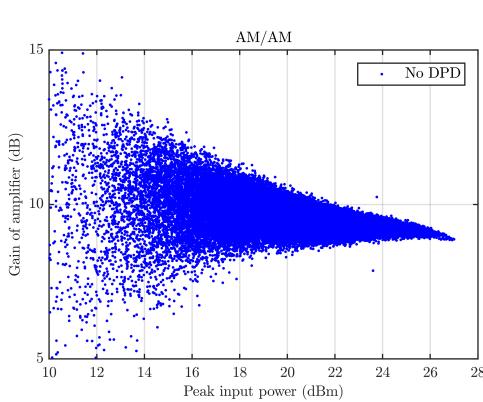
**Figure 4.50:** ACPR versus distance between antennas

It can be seen from figure 4.32 to 4.50 that it does not introduce other problems when introducing four amplifiers than using two. The DPD algorithm still tends to overcompensate at high power values but still maintains a low ACPR. The ACPR is depicted in figure 4.50 and shows like in the former section that the ACPR changes due to antenna gain. The lowest ACPR is found at  $0.5\lambda$  like in the case with two amplifiers. Since the ACPR seems to be a constant value if there is accounted for the antenna gain. A test has been made where the DPD model is obtained at  $0.5\lambda$  and used at the other distances also. This was expected to make a large difference in the distortion since the S-parameters of the antennas changes a lot. See section 5 for antenna measurement. But from figure 4.51 and 4.52 it can be seen that the ACPR becomes like the ACPR in figure 4.50.

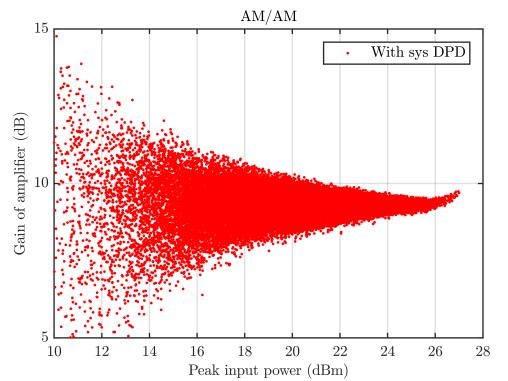
**Figure 4.51:** PSD of measurement where the DPD model is obtained at  $0.6\lambda$  but is also used at other distances**Figure 4.52:** ACPR of measurement where the DPD model is obtained at  $0.6\lambda$  but is also used at other distances

## 4.5 Two amplifiers different current

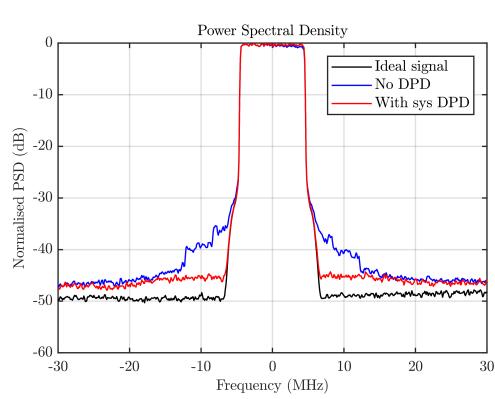
In the former measurement the drain current for each amplifier has been adjusted to 100mA by tuning the gate voltage, to ensure same working conditions for all four amplifiers. In this section is measured if it has any impact that the current is different. First all four amplifiers is connected to the same gate voltage and the current is measured in each amplifier. The two amplifiers with the largest difference is then used for these measurement. The results are shown in figure 4.54 to 4.61 which shows that when the gate voltage is adjusted the performance of the amplifiers changes. This is seen at the AM/AM plots where a difference clearly is seen. This is also why DPD with only considering one amplifier as a model not can be used for multiple amplifiers if the current is different. The results shows thou that if the amplifiers with antennas are treated as a hole, then the DPD algorithm works well and therefore a different bias current is not a huge problem when doing so.



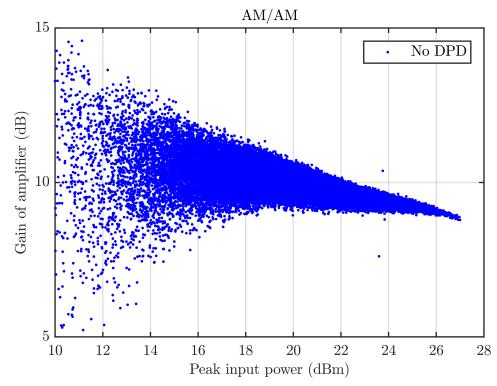
**Figure 4.53:** AM/AM distortion at 56mA in amplifier 1 and 100mA in amplifier 2 with gate voltages at 2.798V without DPD



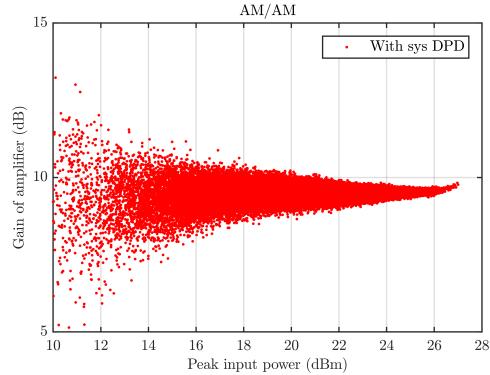
**Figure 4.54:** AM/AM distortion at 56mA in amplifier 1 and 100mA in amplifier 2 with gate voltages at 2.798V with DPD



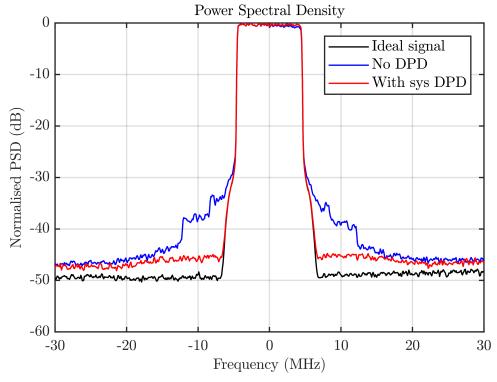
**Figure 4.55:** PSD at 56mA in amplifier 1 and 100mA in amplifier 2 with gate voltages at 2.798V



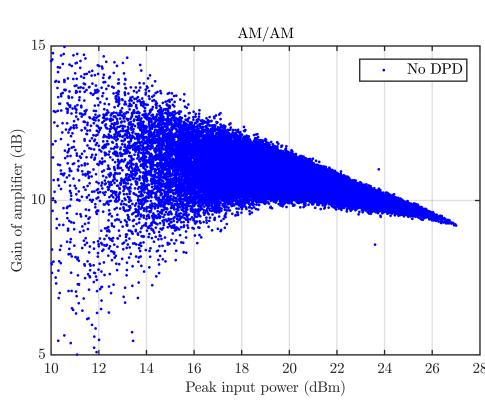
**Figure 4.56:** AM/AM distortion at 75mA in amplifier 1 and 112mA in amplifier 2 with gate voltages at 2.742V without DPD



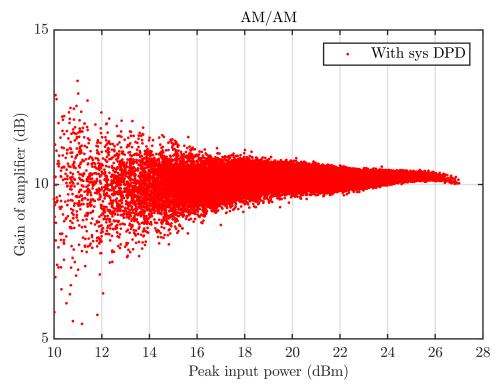
**Figure 4.57:** AM/AM distortion at 75mA in amplifier 1 and 112mA in amplifier 2 with gate voltages at 2.742V with DPD



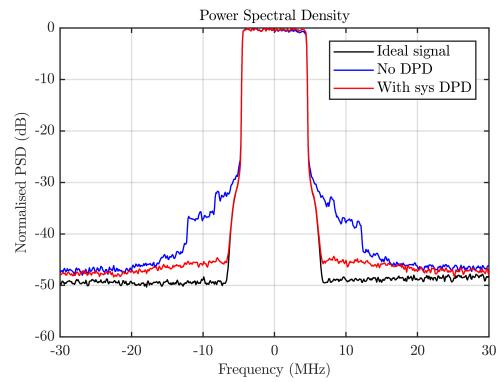
**Figure 4.58:** PSD at 75mA in amplifier 1 and 112mA in amplifier 2 with gate voltages at 2.742V



**Figure 4.59:** AM/AM distortion at 100mA in amplifier 1 and 136mA in amplifier 2 with gate voltages at 2.672V without DPD



**Figure 4.60:** AM/AM distortion at 100mA in amplifier 1 and 137mA in amplifier 2 with gate voltages at 2.672V with DPD



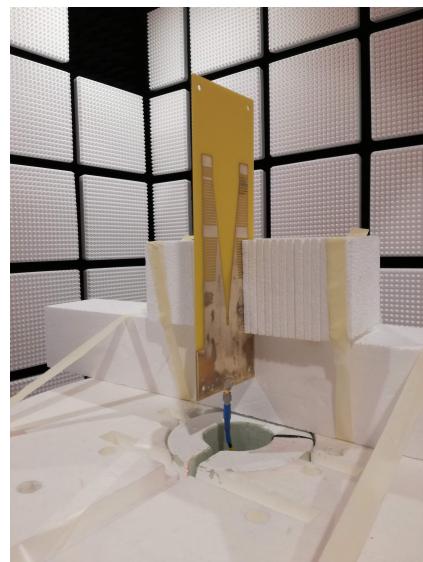
**Figure 4.61:** PSD at 100mA in amplifier 1 and 137mA in amplifier 2 with gate voltages at 2.672V

# Chapter 5

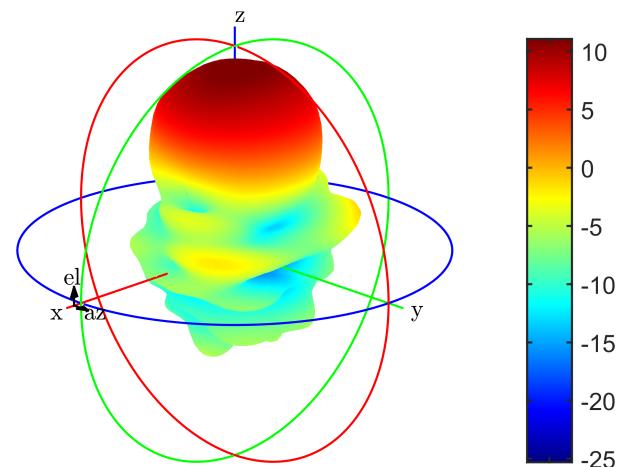
## Antenna measurement

### 5.1 Single antenna

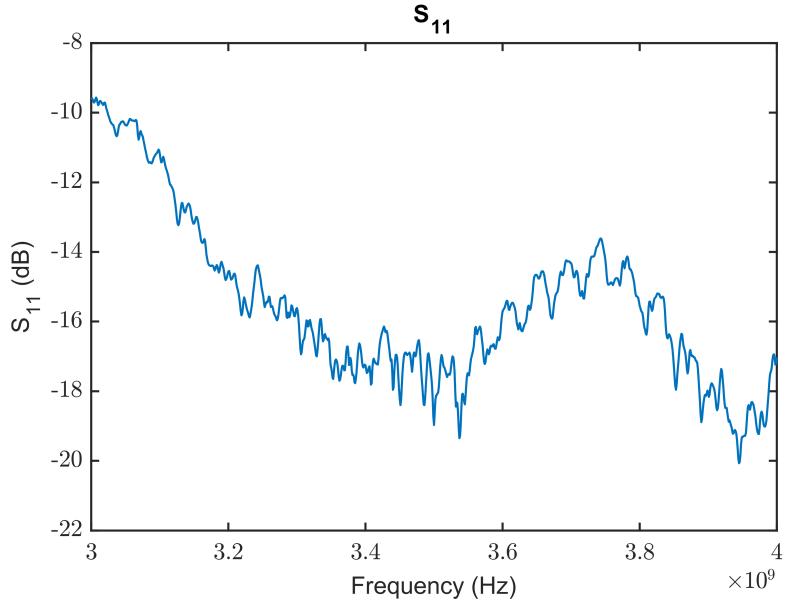
The first measurement done is the farfield of a single antenna only. The measurement of the farfield is done in an anechoic chamber to ensure that no reflections will affect the results. See figure 5.1 The antenna is mounted on a fixture made of flamingo and is connected directly to a cable that further is connected to a signal generator. The measurement shows in figure 5.2 that the antenna has a maximum gain at 11.1 dB and that the farfield can be assumed omnidirectional. The S-paramerets has also been measured but those are not done in an anechoic chamber, but at a setup that is depicted in figure 5.34 the reason is that it was not possible to do the measurement in an anechoic chamber because of the network analyzer who was fixed in an other room. The best would have been to first measure the S-parameters in the anechoic chamber and then measure the S-parameters in the setup where the mesaurement with the amplifiers has been done to see the differences when introducing reflections from the room. Since this has not been possible both due to time and equipment one should be aware of the eventually differences.



**Figure 5.1:** Measurement of a single antenna in an anechoic chamber



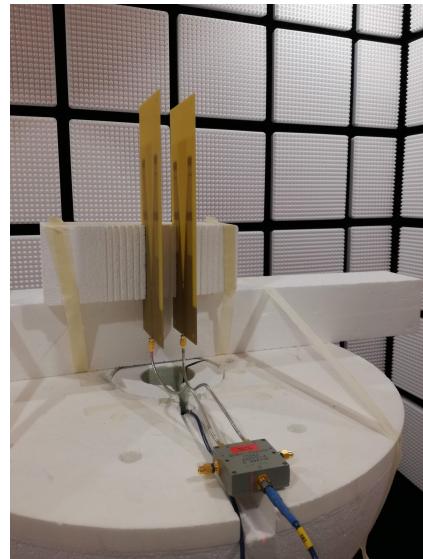
**Figure 5.2:** Measured farfield in dB. Maximum gain is 11.1dB



**Figure 5.3:** Measured S11 parameter of a single antenna

## 5.2 Two antennas

In this section measurement is done at two antennas that are spaced at different distances. This is to see how the farfield will change due to coupling of the array. In the theory the gain should become 3dB greater using two antennas than using one antenna, but for this measurement a power divider is used, which is a 4-port divider that introduces a loss at 6dB to every port. Therefore a decrease of 3dB is expected. The unused ports of the power divider is terminated to a  $50\Omega$  load. It is seen from figure 5.5 to 5.10 that the farfield flattens in the y direction and that the gain varies with the distances between the elements. The loss seems to be lower than expected since a loss at only 2.2dB is obtained at  $d = 0.5\lambda$ . The S-parameters is presented in figure 5.11 to 5.14. It is seen that as expected  $S_{11}$  and  $S_{22}$  are similar and that  $S_{12}$  and  $S_{21}$  also are similar. It is seen that the return-loss  $S_{11}$  and  $S_{22}$  changes a lot with the spacing of the antennas. The largest difference is seen from 0.1 to 0.3 wavelengths. This is also seen from the coupling  $S_{12}$  and  $S_{21}$  that at 0.1 and 0.2 wavelengths ther is a large amount of coupling.

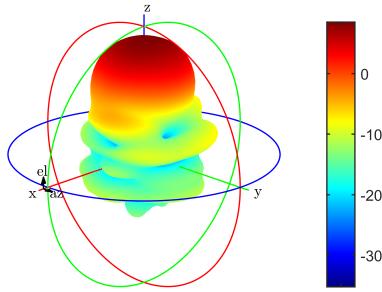


**Figure 5.4:** Measurement of two antennas with a powerdivider in an anechoic chamber. The distances between the antennas are varied for every measurement. The distance is  $0.5\lambda$  on the picture

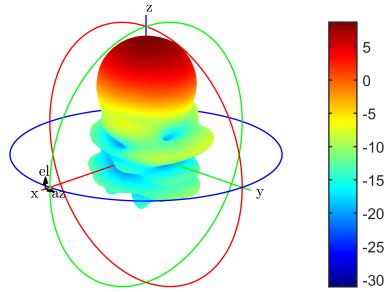


**Figure 5.5:** Farfield for  $d = 0.1\lambda$ . Maximum gain is 7.8dB

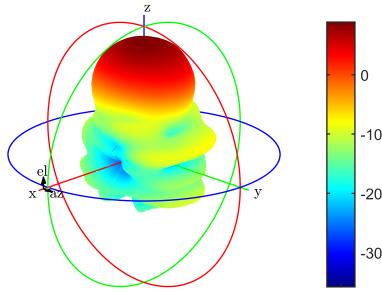
**Figure 5.6:** Farfield for  $d = 0.2\lambda$ . Maximum gain is 8.2dB



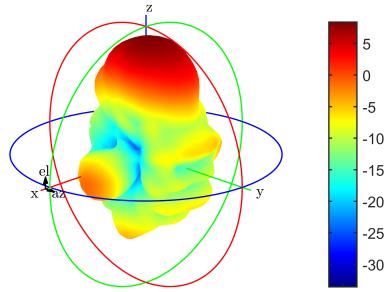
**Figure 5.7:** Farfield for  $d = 0.3\lambda$ . Maximum gain is 8.5dB



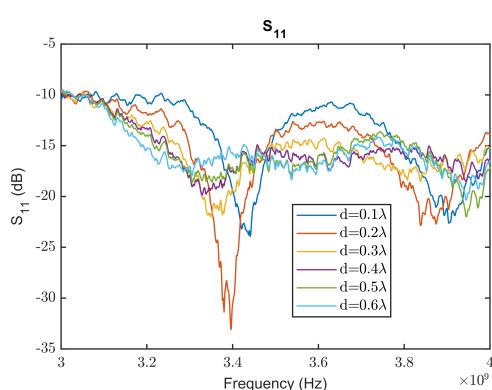
**Figure 5.8:** Farfield for  $d = 0.4\lambda$ . Maximum gain is 8.7dB



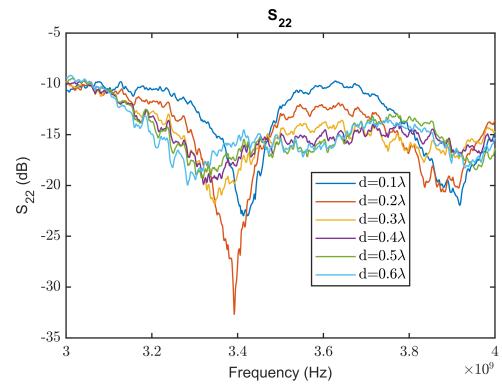
**Figure 5.9:** Farfield for  $d = 0.5\lambda$ . Maximum gain is 8.9dB



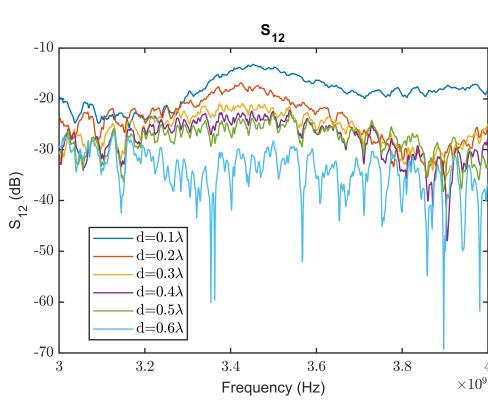
**Figure 5.10:** Farfield for  $d = 0.6\lambda$ . Maximum gain is 8.4dB



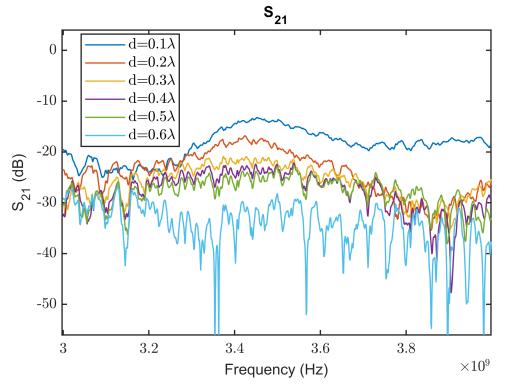
**Figure 5.11:** Measured  $S_{11}$  with two antennas



**Figure 5.12:** Measured  $S_{22}$  with two antennas



**Figure 5.13:** Measured  $S_{12}$  with two antennas



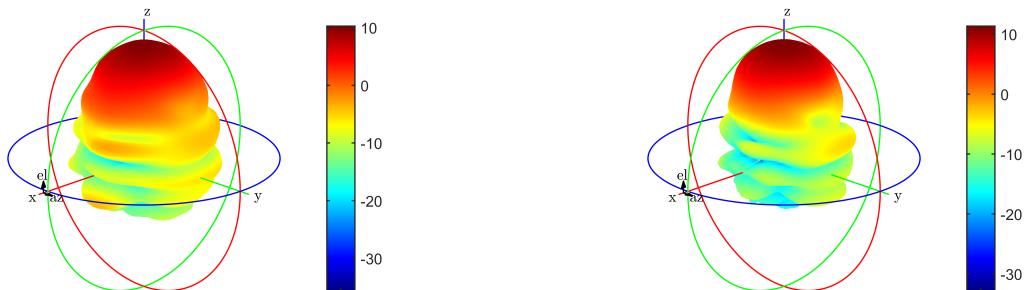
**Figure 5.14:** Measured  $S_{21}$  with two antennas

### 5.3 Four antennas

In this section four antennas is measured. The expected gain is the same as for one antenna because of the powerdivider. Like the case for the measurement done at two antennas the distances is also varied in these measurements. The unused antennas are terminated to  $50\Omega$ . It is seen that the farfield flattens even more at this configuration in the y axis. This is mainly caused by the geometry of the antennas. The gain is also higher then expected which can be seen from figure 5.16 to 5.21. The S-parameters are presented in figure 5.22 to 5.33. The S-parameters shows that  $S_{11}$  and  $S_{44}$  are similar and that  $S_{22}$  and  $S_{33}$  are similar thou variations is seen. This is mainly because that the distance between the antennas are not exactly the same ant that the antennas in them self have small variations. Like in the case with two antennas the coupling gets worse with a smaller distance ant the return loss also variates a lot.



**Figure 5.15:** Measurement of four antennas with a powerdivider in an anechoic chamber. The distances between the antennas are varied for every measurement. The distance is  $0.5\lambda$  on the picture



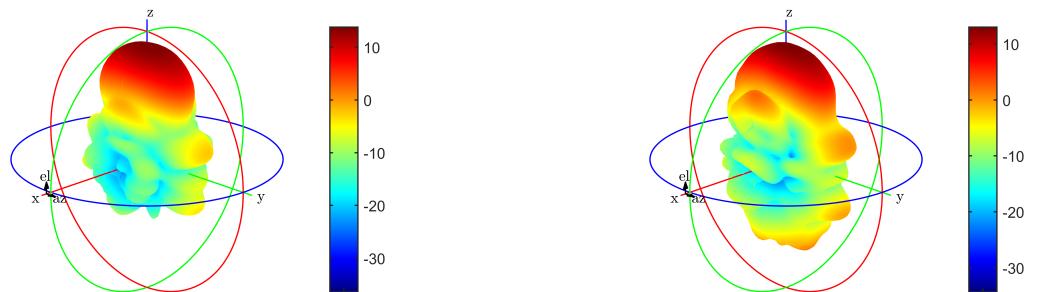
**Figure 5.16:** Farfield for  $d = 0.1\lambda$ . Maximum gain is 10.3dB

**Figure 5.17:** Farfield for  $d = 0.2\lambda$ . Maximum gain is 11.3dB



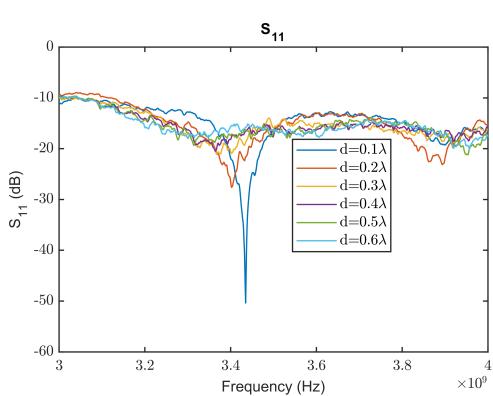
**Figure 5.18:** Farfield for  $d = 0.3\lambda$ . Maximum gain is 12.2dB

**Figure 5.19:** Farfield for  $d = 0.4\lambda$ . Maximum gain is 13.1dB

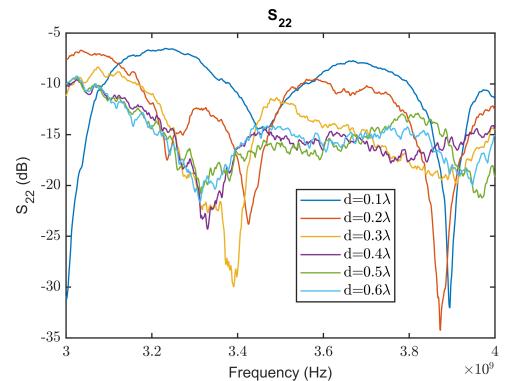


**Figure 5.20:** Farfield for  $d = 0.5\lambda$ . Maximum gain is 13.8dB

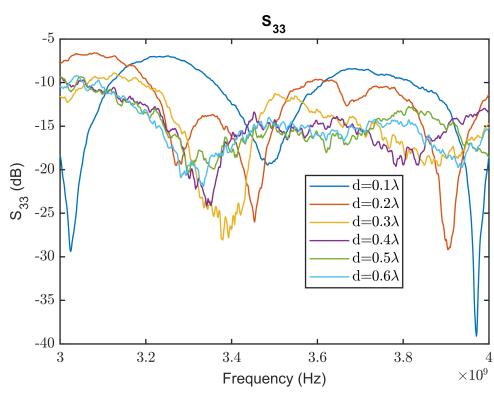
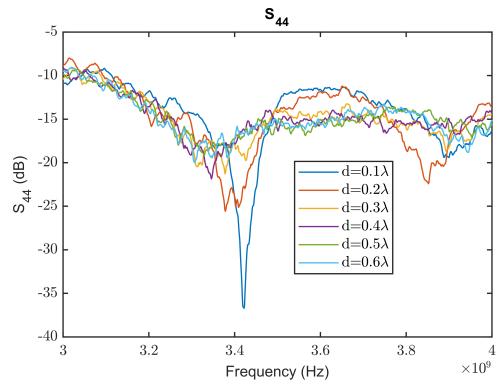
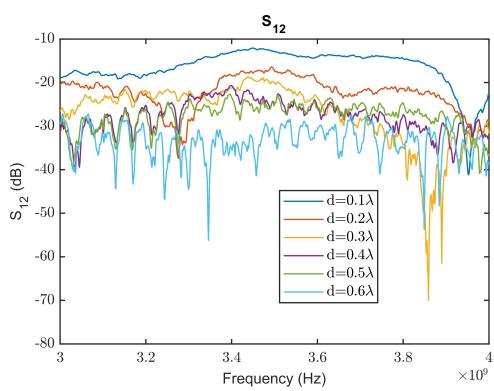
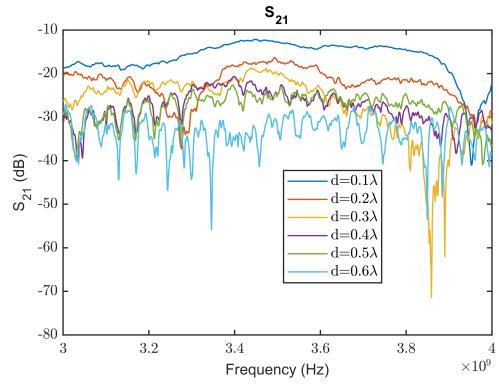
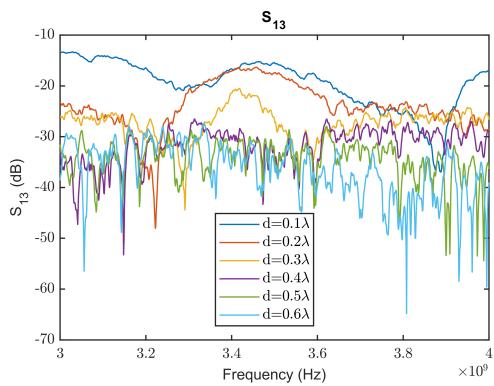
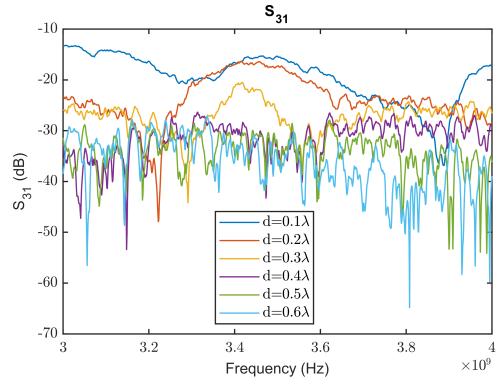
**Figure 5.21:** Farfield for  $d = 0.6\lambda$ . Maximum gain is 13.0dB

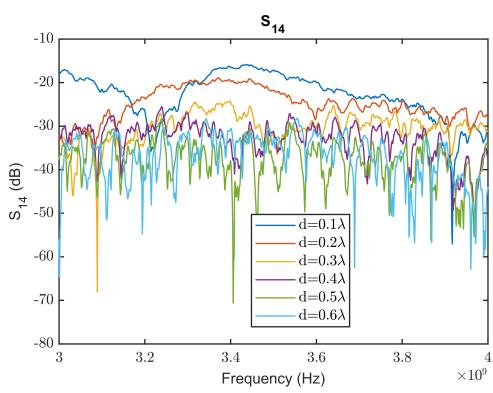


**Figure 5.22:** Measured  $S_{11}$  with four antennas

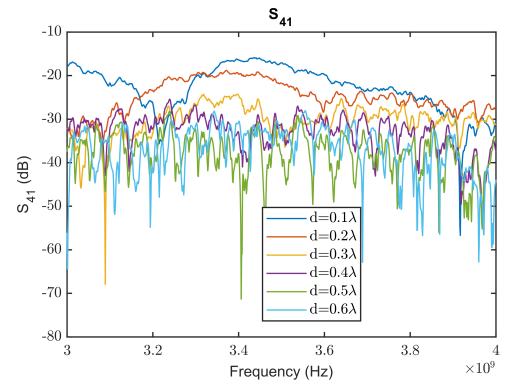


**Figure 5.23:** Measured  $S_{22}$  with four antennas

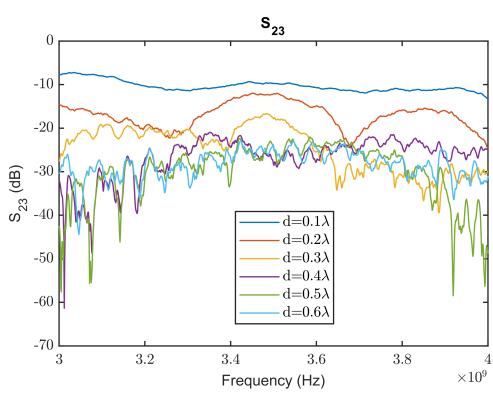
**Figure 5.24:** Measured  $S_{33}$  with four antennas**Figure 5.25:** Measured  $S_{44}$  with four antennas**Figure 5.26:** Measured  $S_{12}$  with four antennas**Figure 5.27:** Measured  $S_{21}$  with four antennas**Figure 5.28:** Measured  $S_{13}$  with four antennas**Figure 5.29:** Measured  $S_{31}$  with four antennas



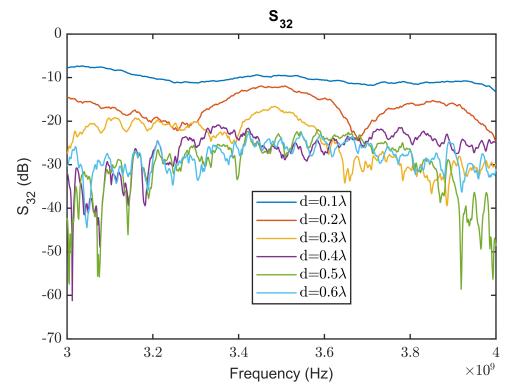
**Figure 5.30:** Measured  $S_{14}$  with four antennas



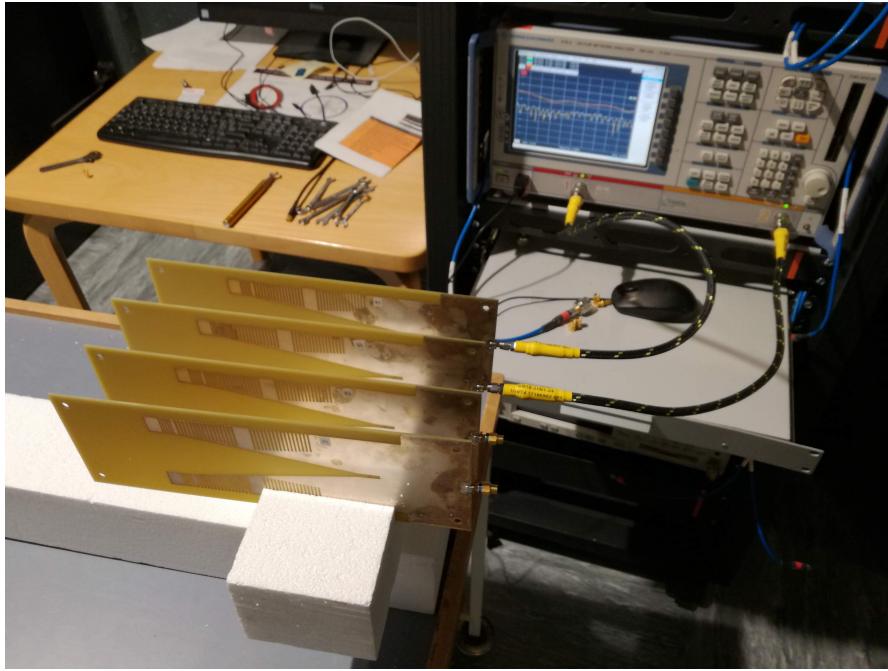
**Figure 5.31:** Measured  $S_{41}$  with four antennas



**Figure 5.32:** Measured  $S_{23}$  with four antennas



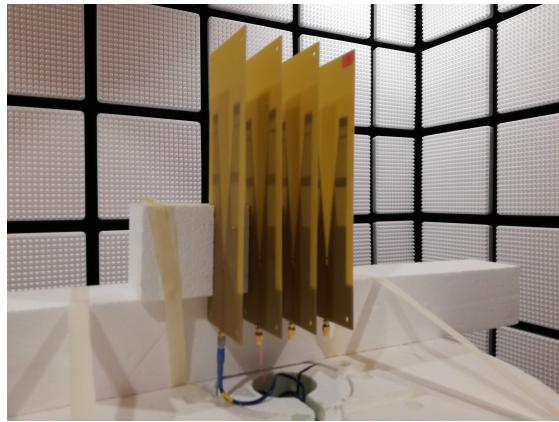
**Figure 5.33:** Measured  $S_{32}$  with four antennas



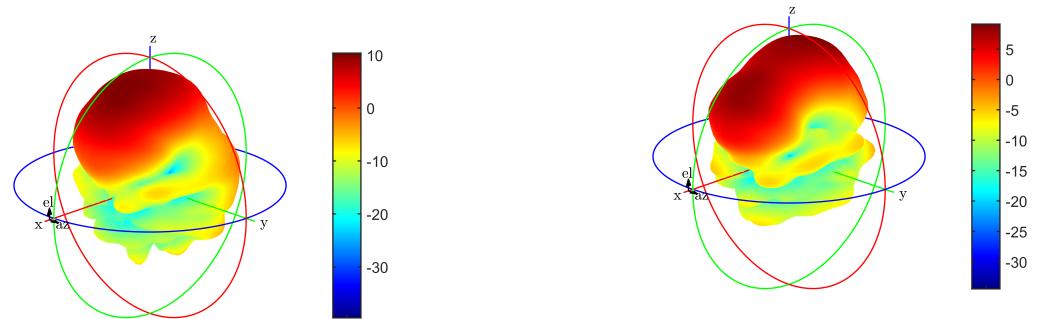
**Figure 5.34:** Measurement of S-parameters using four antennas. The measurement using one and two antennas has been done at the same way. The unused antennas are terminated to  $50\Omega$

## 5.4 Single element four antennas

In this section the farfield of a single element in a array with 4 antennas is measured. It is expected that the first and fourth element has a radiation pattern equal to each other and that second and the third is also equal to each other. It is seen to be somewhat true in figure 5.36 to 5.39 thou variations is seen.

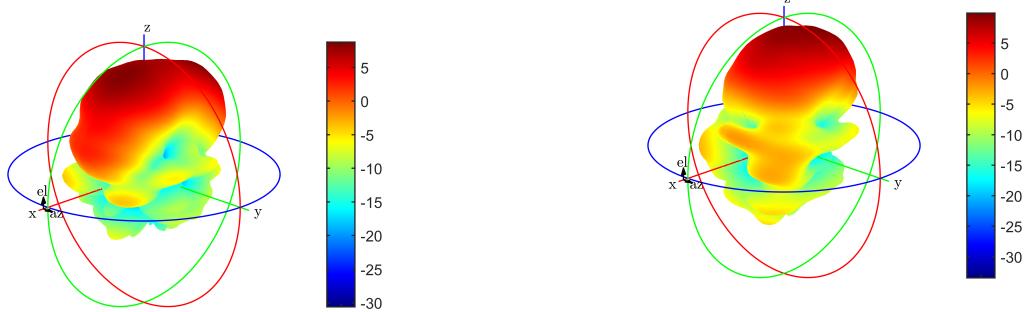


**Figure 5.35:** Measurement of a single antenna in a 4 element array. The unused antennas is terminated to  $50\Omega$ . For every measurement the cable is mounted on another antenna and the load is shifted.



**Figure 5.36:** Farfield first element in the four element array. Maximum gain is 10.4dB

**Figure 5.37:** Farfield second element in the four element array. Maximum gain is 9.1dB



**Figure 5.38:** Farfield third element in the four element array. Maximum gain is 8.8dB

**Figure 5.39:** Farfield fourth element in the four element array. Maximum gain is 9.9dB



# **Chapter 6**

## **Conclusion**

Work done....



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Yan Guo, et.al (2015). Power adaptive digital predistortion for wideband rf power amplifiers with dynamic power transmission. IEEE TRANSACTIONS ON MICROWAVE THEORY AND TECHNIQUES, VOL. 63, NO. 11, NOVEMBER 2015.

Zahidul Islam Shahin, et. al (2017). Efficient dpd coefficient extraction for compensating antenna crosstalk and mismatch effects in advanced antenna system. Department of Electrical and Information Technology LTH, Lund University SE-221 00 Lund, Sweden.



## Appendix A

### MATLAB code

Code to plot AM/AM distortion. powerLev is peak power level at signal generator, preGain is gain of pre-amplifier, Att is attenuation at spectrum analyzer.

```
powerLev = -11;
preGain = 44;
Att = 31;

input = 10*log10( abs(e0)./max( abs(e0) ))+preGain+powerLev;

for i=1:N
    figure;
    gain = 20*log10( abs(e(i,:))*10^(Att/20)./
    (abs(e0)*10^(preGain/20)))-(powerLev);
    plot(input ,gain -6 ,'.r');
    grid on
    title('AM/AM')
    xlabel('Peak input power (dBm)')
    ylabel('Gain of amplifier (dB)')
    legend('With sys DPD')
    ylim([-6 4])
    xlim([10 28])
end
```

Code to plot PSD

```
Fs=1e8;
Res = 100e3;
Nfft = Fs/Res;
[Psd_in,F_in] = pwelch(e0/sqrt(Fs),blackman(Nfft),
[],Nfft, Fs,'centered');

%setFigOptions
```

```

q = [200:800]; % plot only from 30MHz
figure;
plot(F_in(q)*1e-6, 10*log10(Psd_in(q)/max(Psd_in(q))), 'k')
hold on

for i = 1:N
    [Psd_out(:, i), F_out(:, i)] = pwelch(e(i, :) / sqrt(Fs),
        blackman(Nfft), [], Nfft, 'centered');
    plot(F_out(q, i)*1e-6, 10*log10(Psd_out(q, i) /
        max(Psd_out(q, i))))
end

grid on
xlabel('Frequency (MHz)');
ylabel('Normalised PSD (dB)');
legend('Ideal signal', '0.6 $\lambda$', '0.5 $\lambda$',
    '0.4 $\lambda$', '0.3 $\lambda$', '0.2 $\lambda$',
    '0.1 $\lambda$');
title('Power Spectral Density')

```

Code to plot ACPR

```

for i = 1:N
    A=10*log10(Psd_out(q, i)/max(Psd_out(q, i)));
    Index = F_in(q); x = find(Index == 0);
    IndexL = [x-150:x-60];
    IndexH = [x+60:x+150];
    Acpr_L=mean(A(IndexL));
    Acpr_H=mean(A(IndexH));

    ACPR(i) = (Acpr_L+Acpr_H)/2;
end

X = [0.6 0.5 0.4 0.3 0.2 0.1]';

figure(3)
plot(X,ACPR)
xlabel('Distance between antennas ($\lambda$)')
ylabel('ACPR (dB)')
title('ACPR vs spacing of Tx antennas')
ylim([-46 -37])

```

Code to plot antenna S-parameters

```

%% Load S-parameters for two ant
clear
clc
close all

filename = [ 'SPAR/0p1.s2p' ; 'SPAR/0p2.s2p' ; 'SPAR/0p3.s2p' ;
'SPAR/0p4.s2p' ; 'SPAR/0p5.s2p' ; 'SPAR/0p6.s2p' ] ;

for i = 1:6
file = fopen(filename(i,:));
Data = cell2mat(textscan(file ,'%f %f %f %f %f %f %
f %f %f %*[^\n]' , 'HeaderLines' ,5));
file = fclose(file);

f = Data(:,1);
S11 = Data(:,2)+1j*Data(:,3);
S11 = 10.^ (S11/10);

S21 = Data(:,4)+1j*Data(:,5);
S21 = 10.^ (S21/10);

S12 = Data(:,6)+1j*Data(:,7);
S12 = 10.^ (S12/10);

S22 = Data(:,8)+1j*Data(:,9);
S22 = 10.^ (S22/10);

plot(f,10*log10(abs(S22)))
hold on
end

title('S_{22}')
xlabel('Frequency (Hz)')
ylabel('S_{22} (dB)')

legend('d=0.1$\lambda$' , 'd=0.2$\lambda$' , 'd=0.3$\lambda$' ,
'd=0.4$\lambda$' , 'd=0.5$\lambda$' , 'd=0.6$\lambda$')

```

Code to plot antenna farfield

```

%% plot antenna farfield
clear
clc

```

```
close all

file1 = fopen( 'Data/4th_element_4_array.txt' );
Data1 = cell2mat( textscan( file1 ,'%f %f %f %f %f
%f %f %f %*[^\n]' , 'HeaderLines' , 2 ) );
file1 = fclose( file1 );

s = 121;
phi = Data1(72601:s:79860,2); %phi axis
theta = Data1(1:s,3); %theta axis

mag = zeros( length(phi) , length(theta) );
index = (72601:79860);
gaindB = Data1(index,8);

for i = 1:length(phi)
    mag(i,:) = gaindB((1+(s*(i-1)):(s*i)));
end
phi(end) = pi;

figure(1)
patternCustom(mag, theta*180/pi, phi*180/pi)

gain = max(gaindB)
```