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Assignment 1

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ICSE 2018 QUESTION 9 (C)

(c) The following figure represents a solid consisting of a right circular cylinder with a hemisphere at one end and a cone at the other. Their common radius is 7 cm. The height of the cylinder and cone are each of 4 cm. Find the volume of the solid.



Solution:

The various parameters considered in this problem are listed in Table (I)

Symbol	Formula/Value	Description
r	7cm	common radius
h	4cm	height of cone and cylinder
V1	$\frac{1}{3}\pi r^2 h$	Volume of cone
V2	$\pi r^2 h$	Volume of cylinder
V3	$\frac{1}{3}\pi r^3$	Volume of hemisphere
V	?	Volume of the figure

TABLE I

From the given information, the volume of the figure is equal to the sum of the volume of the cone, cylinder and hemisphere. Thus,

$$\begin{split} V &= V1 + V2 + V3 \\ \Longrightarrow V &= \frac{1}{3}\pi r^2 h + \pi r^2 h + \frac{2}{3}\pi r^3 \end{split}$$

$$\therefore V = \frac{2}{3}\pi r^2 (2h + r)$$

By substituting h and r,

Volume of the figure

$$= \frac{2}{3}49(8+7)\pi$$
$$= 490\pi$$
$$\approx 1539.38cm^3$$