

Description:

Implementation of random number generation techniques:

a. linear congruential

b. blum-blum shub generator

The linear congruential method produces a sequence of integers X_1, X_2, X_3, \dots between **zero** and **m-1** according to the following recursive relationship:

$$X_{i+1} \equiv (aX_i + c) \bmod m, \quad i = 0, 1, 2, \dots$$

- The initial value X_0 is called the seed;
- a is called the constant multiplier;
- c is the increment
- m is the modulus

The selection of **a**, **c**, **m** and **X_0** drastically affects the statistical properties such as mean and variance, and the cycle length.

Example: $m=123$, $a=5$, $c=2$, seed $X_0=73$

$$\begin{aligned} X_1 &= (5 \times 73 + 2) \bmod 123 \\ &= 367 \bmod 123 \\ &= 121 \end{aligned}$$

$$\begin{aligned} X_2 &= (5 \times 121 + 2) \bmod 123 \\ &= 607 \bmod 123 \\ &= 115 \end{aligned}$$

$$\begin{aligned} X_3 &= (5 \times 115 + 2) \bmod 123 \\ &= 577 \bmod 123 \\ &= 85 \end{aligned}$$

.....

If we want to generate random bit

$$X_0 = 73 \equiv 1 \bmod 2 \Rightarrow 1$$

$$X_1 = 121 \equiv 1 \bmod 2 \Rightarrow 1$$

$$X_2 = 115 \equiv 1 \bmod 2 \Rightarrow 1$$

$$X_3 = 85 \equiv 1 \bmod 2 \Rightarrow 1$$

$$X_4 = 58 \equiv 0 \bmod 2 \Rightarrow 0$$

....

We get random 0 and 1....

Instructions:

Take the input from the file i.e. m , a , c , X_0 and the range in which a random number is to be generated, and print the random numbers

The Blum Blum Shub (BBS) method is as pseudorandom number generator and was created by Lenore Blum, Manuel Blum and Michael Shub in 1968. It uses the form of:

$$X_i = (X_{i-1})^2 \bmod n$$

where X_0 is a random seed. The value of **n** is equal to pq and where p and q are prime numbers. These values of p and q are both congruent to 3 mod 4 ($p=q=3 \pmod{4}$). What does that mean? Well when I take the values of p or q and divide them by 4, I will get a remainder of 3.

So, $p=7$ is possible (as 7 divided by 4 is 1 remainder 3), and $p=11$ is also possible (as 11 divided by 4 is 2 remainder 3). A value of 13 is not possible as it will be 3 remainder 1

$n=p \cdot q=77$

$X_1=(5)^2 \bmod 77$

$X_2=(25)^2 \bmod 77$

$X_3=(9)^2 \bmod 77$

$X_4=(4)^2 \bmod 77$

In this case we are using $p=7$ and $q=11$, and then a seed of $X_0=5$, and the random sequence is **25, 9, 4 and 16**

Instruction: Read the input from the file i.e. p , q , X_0 and the range in which a random number is to be generated, and print the random numbers

Implementation of random number generation techniques:

a. linear congruential

➤ [methodology followed](#)

```
#include <iostream>
#include <bits/stdc++.h>
#include <fstream>
using namespace std;

int main()
{
    ifstream fin;
    fin.open("input.txt");

    string s1;
    string s2;
    string s3;
    string s4;
    string s5;

    getline(fin, s1);
    getline(fin, s2);
    getline(fin, s3);
    getline(fin, s4);
    getline(fin, s5);

    long long int m = stoi(s1);
    long long int a = stoi(s2);
    long long int c = stoi(s3);
    long long int x0 = stoi(s4);
    long long int n = stoi(s5);
```

```

vector<int> x;
x.push_back(x0);

for (int i = 1; i <= n; i++)
{
    x.push_back((a * x[i - 1] + c) % m);
}

for (int i = 0; i <= n; i++)
{
    cout << "X" << i << " : " << x[i] << "\n";
}





string binary;
for (int i = 0; i <= n; i++)
{
    binary.push_back(x[i] % 2 + '0');
}

cout << binary << "\n";
fin.close();

return 0;
}

```

INPUT:

 ras.cpp	 output.txt PRACTICAL6	 main.cpp practical7
practical8 > linear congruential >  input.txt		
1	123	
2	5	
3	2	
4	73	
5	5	

b. blum-blum shub generator

➤ methodology followed

```
#include <iostream>
#include <bits/stdc++.h>
#include <fstream>
using namespace std;

int main()
{
    ifstream fin;
    fin.open("input2.txt");

    string s1;
    string s2;
    string s3;
    string s4;

    getline(fin, s1);
    getline(fin, s2);
    getline(fin, s3);
    getline(fin, s4);

    long long int p = stoi(s1);
    long long int q = stoi(s2);
    long long int x0 = stoi(s3);
    long long int nx = stoi(s4);

    long long int n = p * q;

    vector<long long int> x;
    x.push_back(x0);

    for (int i = 1; i <= nx; i++)
    {
        x.push_back((x[i - 1] * x[i - 1]) % n);
    }

    for (int i = 0; i <= nx; i++)
    {
        cout << "X" << i << " : " << x[i] << "\n";
    }

    string binary;
    for (int i = 0; i <= nx; i++)
```

```
{  
    binary.push_back(x[i] % 2 + '0');  
}  
  
cout << binary << "\n";  
fin.close();  
return 0;  
}  
  
// range = x%(max-min)+ min +1;
```

INPUT:

ras.cpp	output.txt PRACTICAL6	main.cpp practical7
practical8 > blum-blum shub generator > input2.txt		
1	7	
2	11	
3	5	
4	6	