

Example Sentences in FOL

Example 1

- Every child loves Santa.
- Everyone who loves Santa loves any reindeer.
- Rudolph is a reindeer, and Rudolph has a red nose.
- Anything which has a red nose is weird or is a clown.
- No reindeer is a clown.
- Scrooge does not love anything which is weird.
- Scrooge is not a child.

Example 2

- Anyone who buys carrots by the bushel owns either a rabbit or a grocery store.
- Every dog chases some rabbit.
- Mary buys carrots by the bushel.
- Anyone who owns a rabbit hates anything that chases any rabbit.
- John owns a dog.
- Someone who hates something owned by another person will not date that person.
- If Mary does not own a grocery store, she will not date John.

- Every child loves Santa.

$$\forall x (CHILD(x) \rightarrow LOVES(x, Santa))$$

- Everyone who loves Santa loves any reindeer.

$$\forall x (LOVES(x, Santa) \rightarrow \forall y (REINDEER(y) \rightarrow LOVES(x, y)))$$

- Rudolph is a reindeer, and Rudolph has a red nose.

REINDEER(Rudolph) \wedge REDNOSE(Rudolph)

- Anything which has a red nose is weird or is a clown.

$$\forall x (REDNOSE(x) \rightarrow WEIRD(x) \vee CLOWN(x))$$

- No reindeer is a clown.

$$\neg \exists x (REINDEER(x) \wedge CLOWN(x))$$

- Scrooge does not love anything which is weird.

$$\forall x (WEIRD(x) \rightarrow \neg LOVES(Scrooge, x))$$

- Scrooge is not a child.
 - *CHILD(Scrooge)*

Example 2

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- Mary buys carrots by the bushel.
- Anyone who owns a rabbit hates anything that chases any rabbit.
- John owns a dog.
- Someone who hates something owned by another person will not date that person.
- If Mary does not own a grocery store, she will not date John.

- Anyone who buys carrots by the bushel owns either a rabbit or a grocery store.

$$\forall x (BUY(x) \rightarrow \exists y (OWNS(x,y) \wedge (RABBIT(y) \vee GROCERY(y))))$$

- Every dog chases some rabbit.

$$\forall x (DOG(x) \rightarrow \exists y (RABBIT(y) \wedge CHASE(x,y)))$$

- Mary buys carrots by the bushel.

$$BUY(Mary)$$

- Anyone who owns a rabbit hates anything that chases any rabbit.

$$\forall x \forall y (OWNS(x,y) \wedge RABBIT(y) \rightarrow \forall z \forall w (RABBIT(w) \wedge CHASE(z,w) \rightarrow HATES(x,z)))$$

- John owns a dog.

$$\exists x (DOG(x) \wedge OWNS(John,x))$$

- Someone who hates something owned by another person will not date that person.

$$\forall x \forall y \forall z (OWNS(y,z) \wedge HATES(x,z) \rightarrow \neg DATE(x,y))$$

- (Conclusion) If Mary does not own a grocery store, she will not date John.

$$((\neg \exists x (GROCERY(x) \wedge OWN(Mary,x))) \rightarrow \neg DATE(Mary,John))$$

Example 3

- a. Some dragon is sleeping
- b. No dragon is sleeping
- c. Every dragon is sleeping
- d. Not every dragon is sleeping

a. Some dragon is sleeping

$$\exists x (D(x) \wedge S(x))$$

b. No dragon is sleeping

$$\neg \exists x (D(x) \wedge S(x))$$

c. Every dragon is sleeping

$$\forall x (D(x) \rightarrow S(x))$$

d. Not every dragon is sleeping

$$\neg \forall x (D(x) \rightarrow S(x))$$

Example 4

- a. Some dragon is sleeping or twitching
- b. No dragon is sleeping or twitching
- c. Every dragon is sleeping or twitching
- d. Not every dragon is sleeping or twitching

a. Some dragon is sleeping or twitching

$$\exists x [D(x) \wedge (S(x) \vee T(x))]$$

b. No dragon is sleeping or twitching

$$\neg \exists x [D(x) \wedge (S(x) \vee T(x))]$$

c. Every dragon is sleeping or twitching

$$\forall x [D(x) \rightarrow (S(x) \vee T(x))]$$

d. Not every dragon is sleeping or twitching

$$\neg \forall x [D(x) \rightarrow (S(x) \vee T(x))]$$

Example 5

Paul and Fred left home but Mary did not

Let L = left home, p = Paul, f = Fred, m = Mary

Translate into FOL

Paul left home $L(p)$

Fred left home $L(f)$

Mary left home $L(m)$

Mary didn't leave home $\neg L(m)$

Paul and Fred left home $(L(p) \wedge L(f))$

Paul and Fred left home but Mary did not $((L(p) \wedge L(f)) \wedge \neg L(m))$