

Aim:

Write a C program to implement Kruskal's algorithm for finding the Minimum Cost Spanning Tree (MCST) and the total minimum cost of travel for a given undirected graph. The graph will be represented by an adjacency matrix.

Input Format:

- The first input should be an integer, representing the number of vertices in the graph.
- The next input should be an adjacency matrix representing the weighted graph.
- If there is no edge between two vertices, the weight should be given as 9999 (representing infinity).

Output Format:

- The program should print the edges selected in the Minimum Spanning Tree (MST) along with their weights.

Note:

- Refer to the visible test cases to strictly match the input and output layout.

Source Code:

minCostFinding.c

```
#include <stdio.h>
#include <stdlib.h>
#include <limits.h>
#define INF 9999

typedef struct{
int u,v, cost;
}Edge;

int find(int parent[], int i) {
    while(parent[i] != i)
        i = parent[i];
    return i;
}

void union1(int parent[], int rank[], int i, int j) {
    int root1 = find(parent,i);
    int root2 = find(parent,j);

    if(rank[root1] < rank[root2])
        parent[root1] = root2;
    else if (rank[root1] > rank[root2])
        parent[root2] = root1;
    else{
        parent[root2] = root1;
        rank[root1]++;
    }
}

int compare(const void *a, const void *b){
```

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Edge *e1 = (Edge*)a;
Edge *e2 = (Edge*)b;
if(e1 -> cost != e2 -> cost)
    return e1 -> cost - e2 -> cost;
if(e1 -> u != e2 -> u)
    return e1 -> u - e2 -> u;

return e1 -> v - e2 -> v;
}

void kruskalMST(int **cost, int V) {
    Edge edges[V*V];
    int edgeCount = 0;

    for(int i = 0; i < V; i++){
        for(int j = i; j < V; j++){
            {
                if(cost[i][j] != INF)
                {
                    edges[edgeCount].u = i;
                    edges[edgeCount].v = j;
                    edges[edgeCount].cost = cost[i][j];
                    edgeCount++;
                }
            }
        }
    }

    qsort(edges, edgeCount, sizeof(Edge), compare);

    int *parent = (int*)malloc(V*sizeof(int));
    int *rank = (int*)calloc(V, sizeof(int));

    for(int i = 0 ; i < V; i++){
        parent[i] = i;
    }

    int numEdges = 0, minCost = 0;

    for(int i = 0; i < edgeCount && numEdges < V - 1 ; i++){
        {
            int u = edges[i].u;
            int v = edges[i].v;
            int costEdge = edges[i].cost;

            int set_u = find(parent, u);
            int set_v = find(parent, v);

            if(set_u != set_v){
                printf("Edge %d:(%d, %d) cost:%d\n", numEdges, u, v, costEdge);
                union1(parent, rank, set_u, set_v);
                minCost += costEdge;
                numEdges ++;
            }
        }
    }
    printf("Minimum cost= %d\n", minCost);
}

```

```

    free(parent);
    free(rank);
}

int main() {
    int V;
    printf("No of vertices: ");
    scanf("%d", &V);

    int **cost = (int **)malloc(V * sizeof(int *));
    for (int i = 0; i < V; i++)
        cost[i] = (int *)malloc(V * sizeof(int));

    printf("Adjacency matrix:\n");
    for (int i = 0; i < V; i++)
        for (int j = 0; j < V; j++)
            scanf("%d", &cost[i][j]);

    kruskalMST(cost, V);

    for (int i = 0; i < V; i++)
        free(cost[i]);
    free(cost);

    return 0;
}

```

Execution Results - All test cases have succeeded!

Test Case - 1
User Output
No of vertices: 5
Adjacency matrix: 9999 2 9999 9999 5
2 9999 3 9999 9999
9999 3 9999 4 9999
9999 9999 4 9999 9999
5 9999 9999 9999 9999
Edge 0:(0, 1) cost:2
Edge 1:(1, 2) cost:3
Edge 2:(2, 3) cost:4
Edge 3:(0, 4) cost:5
Minimum cost= 14

Test Case - 2
User Output
No of vertices: 4
Adjacency matrix: 9999 3 6 3
3 9999 5 2
6 5 9999 4
3 2 4 9999
Edge 0:(1, 3) cost:2

Edge 1:(0, 1) cost:3
Edge 2:(2, 3) cost:4
Minimum cost= 9