

# **Knowledge Representation**

**(Examples of Resolution)**

# 1. Solve the example by using the concept of Resolution

- (a) Marcus was a man.
- (b) Marcus was a Roman.
- (c) All men are people.
- (d) Caesar was a ruler.
- (e) All Romans were either loyal to Caesar or hated him (or both).
- (f) Everyone is loyal to someone.
- (g) People only try to assassinate rulers they are not loyal to.
- (h) Marcus tried to assassinate Caesar.

**Prove: hate(Marcus, Caesar)**

# Convert to First Order Logic

- (a) Marcus was a man.
- (b) Marcus was a Roman.
- (c) All men are people.
- (d) Caesar was a ruler.
- (e) All Romans were either loyal to Caesar or hated him (or both).
- (f) Everyone is loyal to someone.
- (g) People only try to assassinate rulers they are not loyal to.
- (h) **Marcus tried to assassinate Caesar.**

- (a)  $\text{man}(\text{marcus})$
- (b)  $\text{roman}(\text{marcus})$
- (c)  $\forall X. \text{man}(X) \rightarrow \text{person}(X)$
- (d)  $\text{ruler}(\text{caesar})$
- (e)  $\forall X. \text{roman}(x) \rightarrow \text{loyal}(X, \text{caesar}) \vee \text{hate}(X, \text{caesar})$
- (f)  $\forall X \exists Y. \text{loyal}(X, Y)$
- (g)  $\forall X \forall Y. \text{person}(X) \wedge \text{ruler}(Y) \rightarrow \text{tryassasin}(X, Y) \rightarrow \neg \text{loyal}(X, Y)$
- (h)  $\text{tryassasin}(\text{marcus}, \text{caesar})$

Negate!

$\neg \text{hate}(X, \text{caesar})$

# Convert to Clausal Form

- (a)  $\text{man}(\text{marcus})$
- (b)  $\text{roman}(\text{marcus})$
- (c)  $\forall X. \text{man}(X) \rightarrow \text{person}(X)$   
 $(\neg \text{man}(X), \text{person}(X))$
- (d)  $\text{ruler}(\text{caesar})$
- (e)  $\forall X. \text{roman}(X) \rightarrow \text{loyal}(X, \text{caesar}) \vee \text{hate}(X, \text{caesar})$   
 $(\neg \text{roman}(X), \text{loyal}(X, \text{caesar}), \text{hate}(X, \text{caesar}))$
- (f)  $\forall X \exists Y. \text{loyal}(X, Y)$   
 $(\text{loyal}(X, f(X)))$
- (g)  $\forall X \forall Y. \text{person}(X) \wedge \text{ruler}(Y) \wedge \text{tryassasin}(X, Y) \rightarrow \neg \text{loyal}(X, Y)$   
 $(\neg \text{person}(X), \neg \text{ruler}(Y), \neg \text{tryassasin}(X, Y), \neg \text{loyal}(X, Y))$
- (h)  $\text{tryassasin}(\text{marcus}, \text{caesar})$

Negate!

$\neg \text{hate}(X, \text{caesar})$

$\neg \text{man}(x) \vee \text{person}(x)$

$\text{man}(\text{marcus}) \quad x/\text{marcus}$

$\text{person}(\text{marcus})$

$\neg \text{person}(\text{marcus}) \vee \neg \text{ruler}(y)$

$\vee \neg \text{tyrannical}(\text{marcus}, y)$

$\vee \neg \text{loyal}(\text{marcus}, y)$

$\neg \text{ruler}(y) \vee \neg \text{tyrannical}(\text{marcus}, y) \vee \neg \text{loyal}(\text{marcus}, y)$

$y/\text{caesar}$   
 $\text{ruler}(\text{caesar})$

$\text{tyrannical}(\text{marcus}, \text{caesar}) \vee \neg \text{tyrannical}(\text{marcus}, \text{caesar}) \vee \neg \text{loyal}(\text{marcus}, y)$

$\neg \text{loyal}(\text{marcus}, \text{caesar})$

$\text{loyal}(\text{marcus}, \text{caesar})$

2. Solve the example by using the concept of Resolution

1. **Gita likes all kinds of food.**
  2. **Mango and chapatti are food.**
  3. **Gita eats almond and is still alive.**
  4. **Anything eaten by anyone and is still alive is food.**
- **Goal:** Gita likes almond.



1.  $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{Gita}, x)$
2.  $\text{food}(\text{Mango}), \text{food}(\text{chapati})$
3.  $\forall x \forall y: \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
4.  $\text{eats}(\text{Gita}, \text{almonds}) \wedge \text{alive}(\text{Gita})$
5.  $\forall x: \neg \text{killed}(x) \rightarrow \text{alive}(x)$
6.  $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$

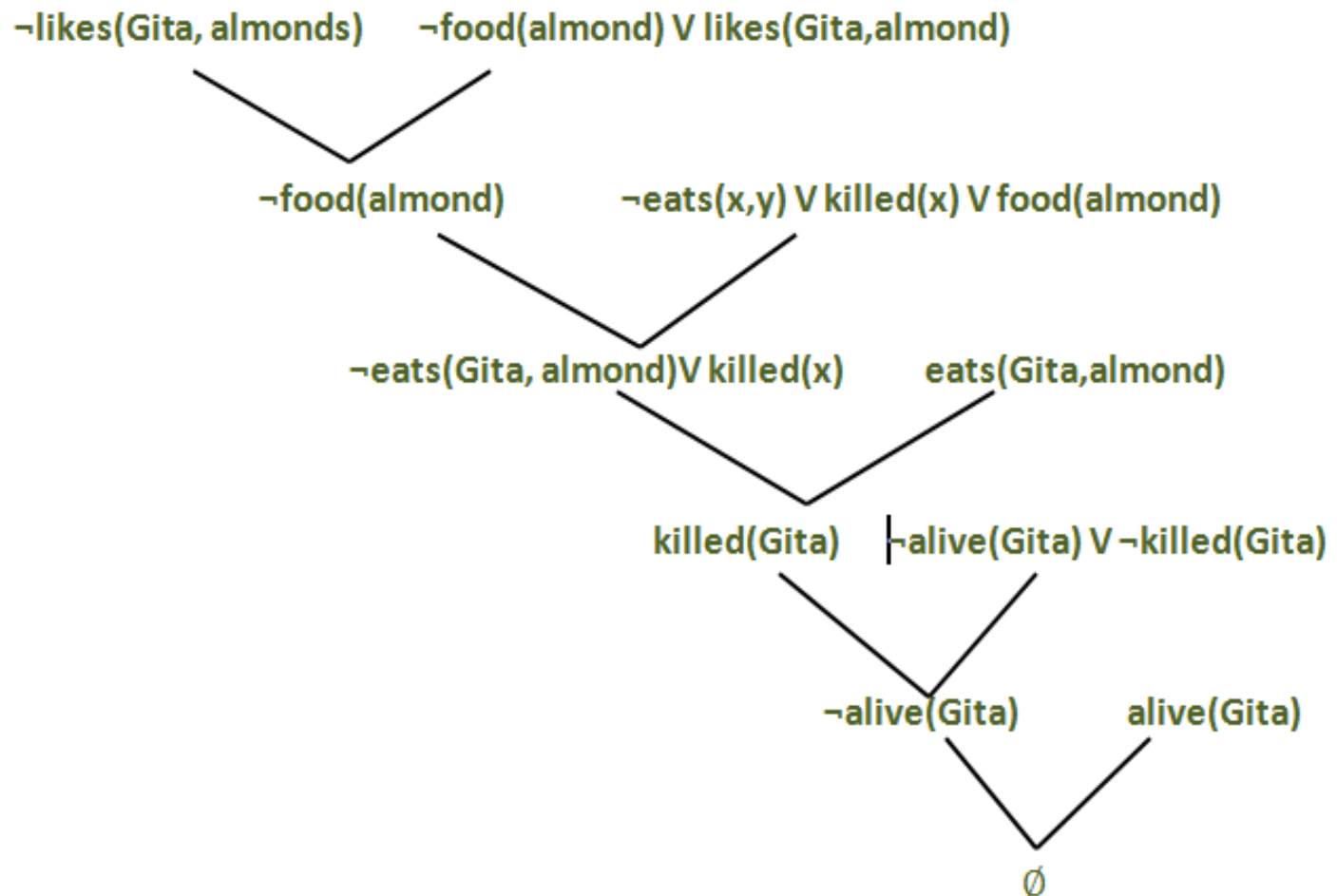
**Goal:**  $\text{likes}(\text{Gita}, \text{almond})$

**Negated goal:**  $\neg \text{likes}(\text{Gita}, \text{almond})$

**Now, rewrite in CNF form:**

1.  $\neg \text{food}(x) \vee \text{likes}(\text{Gita}, x)$
2.  $\text{food}(\text{Mango}), \text{food}(\text{chapati})$
3.  $\neg \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y)$
4.  $\text{eats}(\text{Gita}, \text{almonds}), \text{alive}(\text{Gita})$
5.  $\text{killed}(x) \vee \text{alive}(x)$
6.  $\neg \text{alive}(x) \vee \neg \text{killed}(x)$

Finally, construct the resolution graph:





3. Solve the example by using the concept of Resolution

**All oversmart persons are stupid. Children of oversmart persons are naughty. Ram is children of Hari. Hari is oversmart. Show that Ram is naughty.**

## Axioms in FOPL

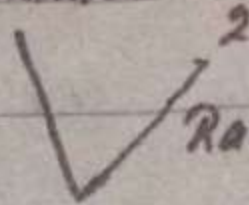
1.  $\forall x : \text{Oversmart}(x) \rightarrow \text{Stupid}(x)$
2.  $\forall x : \forall y : \text{Oversmart}(x) \wedge \text{child-of}(y, x) \rightarrow \text{Naughty}(y)$
3.  $\text{child-of}(\text{Ram}, \text{Hari})$
4.  $\text{Oversmart}(\text{Hari})$

## Clause Form

1.  $\neg \text{Oversmart}(x) \vee \text{Stupid}(x)$
2.  $\neg \text{Oversmart}(x) \vee \neg \text{child-of}(y, x) \vee \text{Naughty}(y)$
3.  $\text{child-of}(\text{Ram}, \text{Hari})$
4.  $\text{Oversmart}(\text{Hari})$

## Resolution

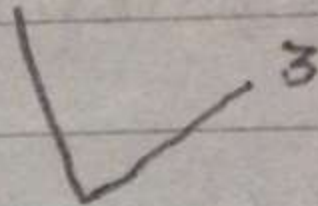
1 Naughty (Ram)



2

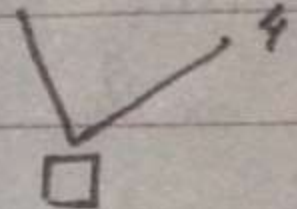
Ram/y<sub>2</sub>, Hari/n<sub>2</sub>

3 Oversmart (Hari) child-of (Ram, Hari)



3

4 Oversmart (Hari)



4

# Example

Assume the following facts:

- i. “Steve only likes easy courses.
- ii. Science courses are hard.
- iii. All the courses in Humanities Department are easy.
- iv. HM101 is a course in Humanities”.

Convert the above statements into appropriate wffs so that the resolution can be performed to answer the question. “ what course would steve like?”

First we will convert it into FOPL (First order predicate logic)

i. "Steve only likes easy courses.

$\forall x: \text{easy}(x) \rightarrow \text{likes}(\text{steve}, x)$

ii. Science courses are hard.

$\forall x: \text{science}(x) \rightarrow \sim \text{easy}(x)$

iii. All the courses in Humanities Department are easy.

$\forall x: \text{humanities}(x) \rightarrow \text{easy}(x)$

iv. HM101 is a course in Humanities".

$\text{humanities}(\text{HM101})$

The conclusion is encoded as  $\text{likes}(\text{steve}, x)$ .

- First we put our premises in the clause form and the negation of conclusion to our set of clauses (we use numbers in parentheses to number the clauses):

(1)  $\sim \text{easy}(x) \vee \text{likes}(\text{steve}, x)$

(2)  $\sim \text{science}(x) \vee \sim \text{easy}(x)$

(3)  $\sim \text{humanities}(x) \vee \text{easy}(x)$

(4)  $\text{humanities}(\text{HM101})$

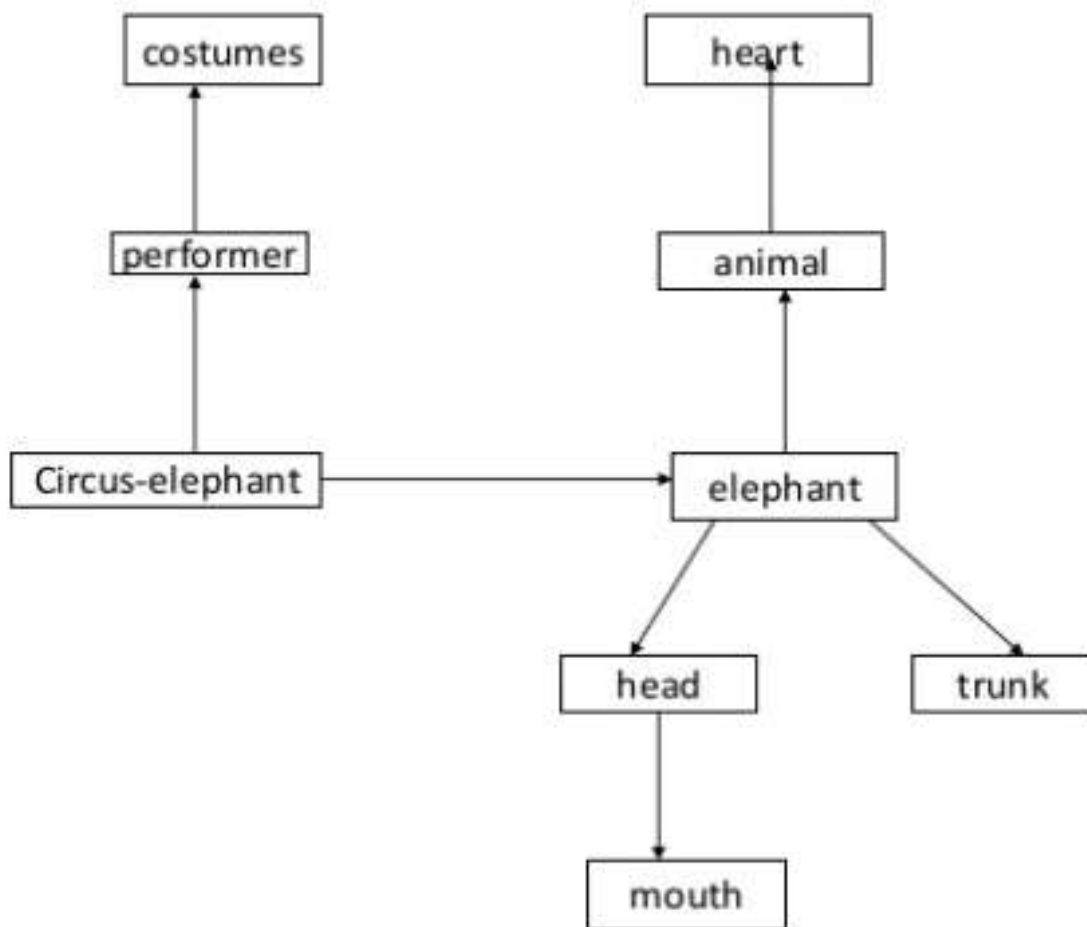
(5)  $\sim \text{likes}(\text{steve}, x)$

St	Clauses	Note
1	$\sim \text{easy}(x) \vee \text{likes}(\text{steve}, x)$	P
2	$\sim \text{science}(x) \vee \sim \text{easy}(x)$	P
3	$\sim \text{humanities}(x) \vee \text{easy}(x)$	P
4	$\text{humanities}(\text{HM101})$	P
5	$\sim \text{likes}(\text{steve}, x)$	P
6	$\sim \text{easy}(x)$	1 & 5
7	$\sim \text{humanities}(x)$	3 & 6
8	NIL	4 & 7, x=HM101

## Represent following information in Semantic net

- (is\_a circus-elephant elephant)
- (has elephant head)
- (has elephant trunk)
- (has head mouth)
- (is\_a elephant animal)
- (has animal heart)
- (is\_a circus-elephant performer)
- (has performer costumes)





# Solve By using Resolution, Forward Chaining and Backward Chaining

1. India is a Team
2. Australia is a Team
3. Match between India and Australia
4. India scores 350 runs and Australia scores 350 runs, India lost by 5 wickets and Australia lost by 7 wickets
5. The team which scored the maximum runs wins
6. If the scores are then the team which lost minimum wickets wins the match

**Prove by resolution that:**

India wins the match

## Step-1: Conversion of Facts into FOL

1.  $\text{Team}(\text{India})$
2.  $\text{Team}(\text{Australia})$
3.  $\text{Team}(\text{India}) \wedge \text{Team}(\text{Australia}) \rightarrow \text{Match}(\text{India}, \text{Australia})$
4.  $\text{Score}(\text{India}, \text{runs}(350)) \wedge \text{Score}(\text{Australia}, \text{runs}(350)) \wedge \text{lost}(\text{India}, \text{wickets}(5)) \wedge \text{lost}(\text{Australia}, \text{wickets}(7))$
5.  $\forall x : \text{Team}(x) \wedge \text{Score}(x, \text{max}(\text{runs})) \rightarrow \text{wins}(x, \text{match})$
6.  $\forall x, \forall y : \text{Team}(x) \wedge \text{Team}(y) \wedge \text{Score}(x, y, \text{equal}(\text{runs})) \wedge \text{lost}(x, \text{min}(\text{wickets})) \rightarrow \text{wins}(x, \text{match})$

### added predicates

7.  $\text{Score}(\text{India}, \text{runs}(350)) \wedge \text{Score}(\text{Australia}, \text{runs}(350)) \rightarrow \text{Score}(\text{India}, \text{Australia}, \text{equal}(\text{runs}))$
8.  $\text{lost}(\text{India}, \text{wickets}(5)) \wedge \text{lost}(\text{Australia}, \text{wickets}(7)) \rightarrow \text{lost}(\text{India}, \text{min}(\text{wickets}))$

### To Prove

$\text{wins}(\text{India}, \text{match})$

## Step-2: Conversion of FOL into CNF

### 2.1 Eliminate all implication ( $\rightarrow$ ) and rewrite

1.  $\text{Team}(\text{India})$
2.  $\text{Team}(\text{Australia})$
3.  $\neg (\text{Team}(\text{India}) \wedge \text{Team}(\text{Australia})) \vee \text{Match}(\text{India}, \text{Australia})$
4.  $\text{Score}(\text{India}, \text{runs}(350)) \wedge \text{Score}(\text{Australia}, \text{runs}(350)) \wedge \text{lost}(\text{India}, \text{wickets}(5)) \wedge \text{lost}(\text{Australia}, \text{wickets}(7))$
5.  $\forall x : \neg (\text{Team}(x) \wedge \text{Score}(x, \text{max}(\text{runs}))) \vee \text{wins}(x, \text{match})$
6.  $\forall x, \forall y : \neg (\text{Team}(x) \wedge \text{Team}(y) \wedge \text{Score}(x, y, \text{equal}(\text{runs})) \wedge \text{lost}(x, \text{min}(\text{wickets}))) \vee \text{wins}(x, \text{match})$

$$P \rightarrow Q = \neg P \vee Q$$

### added predicates

7.  $\neg (\text{Score}(\text{India}, \text{runs}(350)) \wedge \text{Score}(\text{Australia}, \text{runs}(350))) \vee \text{Score}(\text{India}, \text{Australia}, \text{equal}(\text{runs}))$
8.  $\neg (\text{lost}(\text{India}, \text{wickets}(5)) \wedge \text{lost}(\text{Australia}, \text{wickets}(7))) \vee \text{lost}(\text{India}, \text{min}(\text{wickets}))$

### To prove

$\text{wins}(\text{India}, \text{match})$

## Forward Chaining



## Backward Chaining

