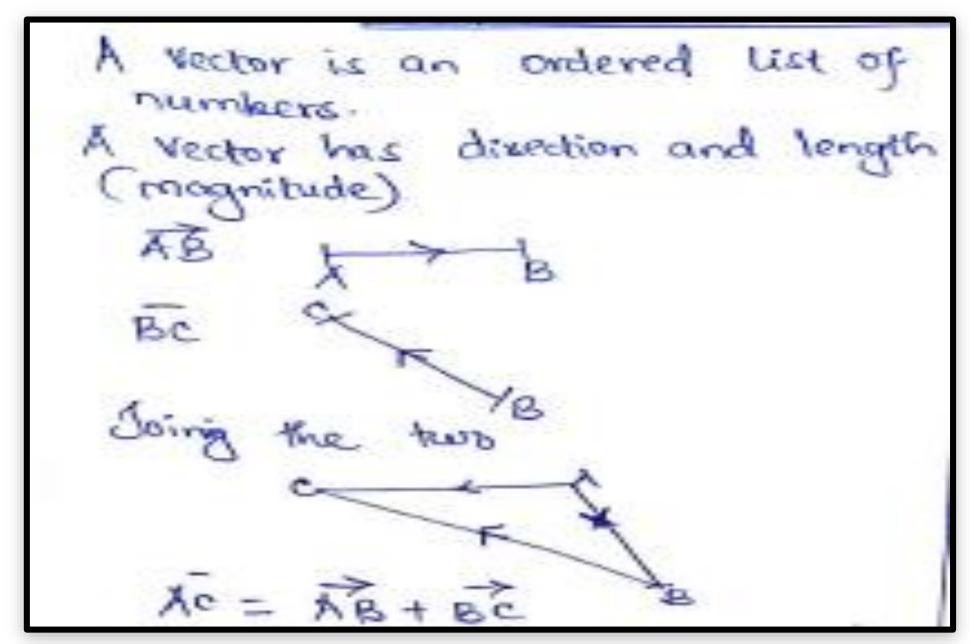
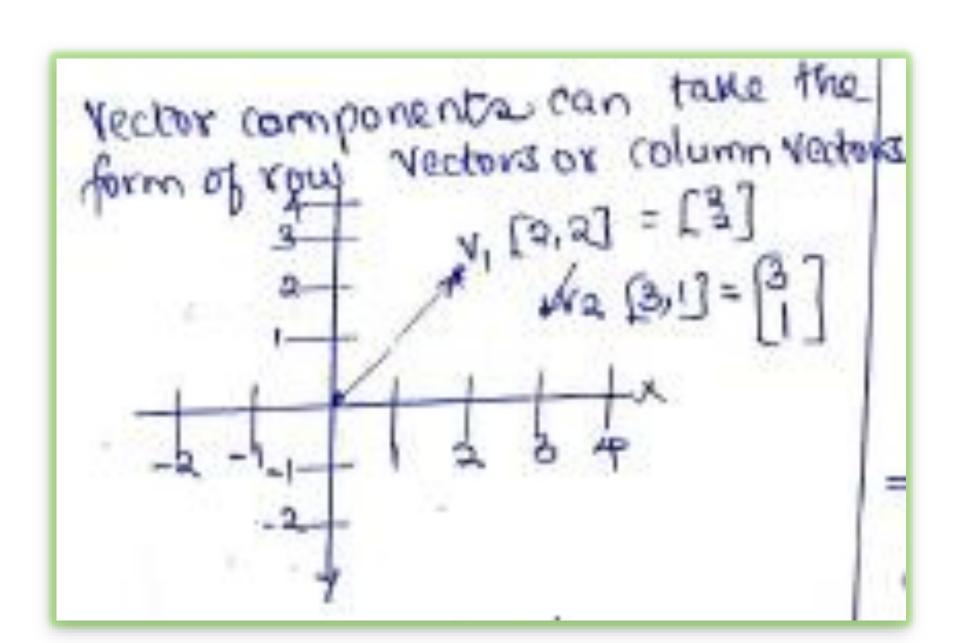
Vectors and Vector Spaces

mgichuki@jkuat.ac.ke

Introduction





A scalar quantity has magnitude only.

Speed is a scalar - 40 m/s

Velocity is a vector - 40 m/s North

Force is a vector 300 Heatons exerted cast

Suppose Vector V has initial point of (-4,1) and Terminal point B(8,6)

Vector 4 has initial patc(1,-15)

and terminal points b (3,9)

a) Determine if the two vectors

are equivalent.

V= 1B u= CD

$$V = (8-4), (6-1) = (18, 5)$$

 $U = (90/5)(3-1), (9-15) = (10, 24)$
 $U = (90/5)(3-1), (9-15) = (10, 24)$
 $V = (10, 24)$
 V

Position Vector at point (0,0) Unit Vector ||un = 1 Any vector with a magnitude $\frac{\eta_{A} \eta_{A}}{\Lambda} = \Lambda = \frac{\lambda}{\Lambda} \cdot \|\Lambda\|_{A}$

Position and Unit Vectors

Question

Find the unit vector in the same direction of
$$V = (4, -3)$$
 $U = \frac{V}{|V|} = \frac{(4, -3)}{\sqrt{4^2 + (-3)^2}} = \frac{4, -3}{5} = \frac{4}{5}$

Unit vector of vector $V = (\frac{2}{5}, \frac{3}{5})$

Proof: Is the magnitude = 1?

 $\int \frac{1}{3^2 + (\frac{3}{5})^2} = \int \frac{1}{25} \frac{1}{25} = \int \frac{1}{25} \frac{1}{25} = 1$

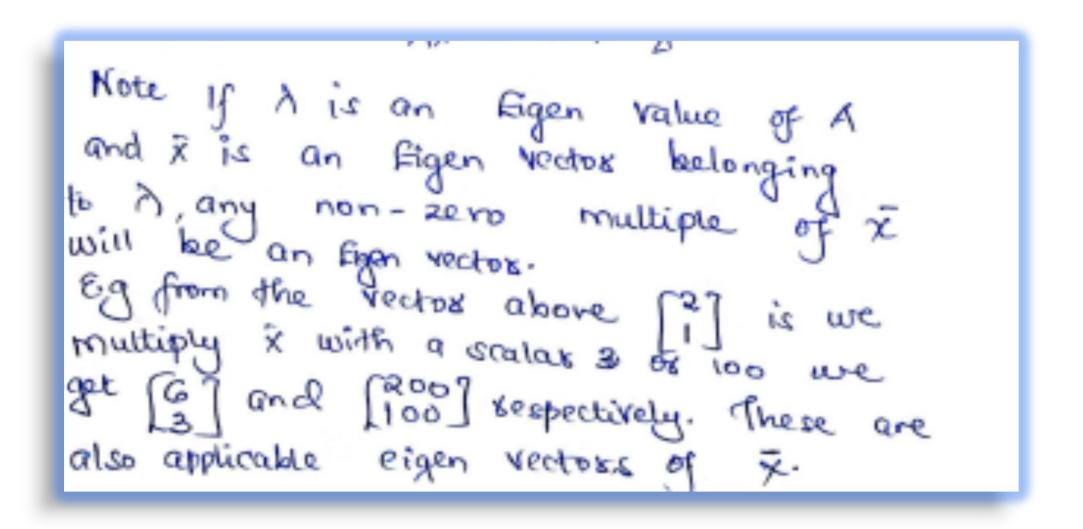
Eigen Vectors and Eigen Values

```
Eigen Vectors and Eigen Values defined:
 Let 1 be an nxn matrix.

A scalar 2 is called an Eigen Value
 of A if there's a non-zero Vector
 \bar{x} such that A\bar{x} = \lambda \bar{x}.
The Vector x is called an Rigen Vector
of A corresponding to Figen value 2.
Example:
Show that \bar{x} = [i] is an figen vector
of \Lambda = \begin{bmatrix} 3 & 2 \\ 3 & -2 \end{bmatrix} corresponding to \lambda = 4
Solution
Recall: A\bar{x} = \lambda \bar{x}
       3-2 1 = 4 []
      3.2+(-2).1)= [8]
```

$$v_{\lambda=4}^{\overrightarrow{}}
ightarrow \{2,1\}$$
 $v_{\lambda=-3}^{\overrightarrow{}}
ightarrow \{-1,3\}$

Scalars or Multiplies apply (e.g. vector 4,2, vector 6,3, Vector 200,100)



Finding Eigen Values and Eigen Vectors

```
The steps of computing Eigen Values and Eigen vectors
To solve the eigenvalues hi and the corresponding
Eigen vectors is of an nxn matrix X, we follow the following steps: eigif X = [3-1]
    i) Multiply the nxn Identity matrix by the
         Scalar y
                   ZI = Z[0] = [0 2]
   ii) Subtact the Identity matrix multiple from A A - \lambda I = \begin{bmatrix} 7 & 3 \\ 3 & - \end{bmatrix} - \begin{bmatrix} \lambda & 0 \\ 0 & \lambda \end{bmatrix} = \begin{bmatrix} 7 - \lambda & 3 \\ 3 & - 1 - \lambda \end{bmatrix}
  (i) Find the determinant of the toutrix from step (ii) det [7-2 3-7] = (7-2)(-2-1) - (3)(3)
                                  = -47-7+2+7 - 9 Factors 2 and 8,2
Solve the values of > that satisfy the equation det(A->)=0
```

(4) Colve for the corresponding vectors for each of The state of the To colve Bx = 0 [-13-9] [XI] = [0] 3RITR2 = New RZ 3][0] => -X, +3XR = D Suppose X2= 1 3(1)=X1=3 Vector =

- 3R2+R1 = New R1 [0 0][0] = 3x1+xe=0 suppose X1 = 1 Xa = -3(1) =-3 AGGLOR = Chack: (7 37 [3] = -2[3]=[6]

Example Two

$$v_{\lambda=2}^{\rightharpoonup} \rightarrow \{0,1\}$$

 $v_{\lambda=1}^{\rightharpoonup} \rightarrow \{1,0\}$

Example Three

b)
$$A = \begin{bmatrix} 0 & -1 \\ 0 & 0 \end{bmatrix}$$

$$A\hat{x} = A\hat{x}$$

$$AI = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} A = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & -1 \\ 0 & 1 \end{bmatrix}$$
Determinant of $A = AI$

$$A = \begin{bmatrix} -1 & -1 \\ 0 & 1 \end{bmatrix}$$
Eigen values ± 1

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} -1$$

$$v_{\lambda=-1}^{\rightharpoonup}
ightarrow \{1,1\}$$

 $v_{\lambda=1}^{\rightharpoonup}
ightarrow \{-1,1\}$

Real life applications of Eigen values and Eigen vectors

https://www.youtube.com/watch?v=R13Cwgmpuxc

Questions & Comments