

#1A Fuzzy and or and not operation

```
import numpy as np
```

```
# Fuzzy values (between 0 and 1)
```

```
A = np.array([0.1, 0.4, 0.7])
```

```
B = np.array([0.2, 0.5, 0.9])
```

```
# Fuzzy AND = min(A, B)
```

```
fuzzy_and = np.minimum(A, B)
```

```
# Fuzzy OR = max(A, B)
```

```
fuzzy_or = np.maximum(A, B)
```

```
# Fuzzy NOT = 1 - A
```

```
fuzzy_not = 1 - A
```

```
print("A =", A)
```

```
print("B =", B)
```

```
print("Fuzzy AND =", fuzzy_and)
```

```
print("Fuzzy OR =", fuzzy_or)
```

```
print("Fuzzy NOT (of A) =", fuzzy_not)
```

```
#1B plot triangular and trapezoidal membership
```

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
x = np.linspace(0, 10, 100)
```

```
# Triangular membership function
```

```
def triangular(x, a, b, c):
```

```
    return np.maximum(np.minimum((x - a) / (b - a), (c - x) / (c - b)), 0)
```

```
# Trapezoidal membership function
```

```
def trapezoidal(x, a, b, c, d):
```

```
    return np.maximum(np.minimum(np.minimum((x - a) / (b - a), 1), (d - x) / (d - c)), 0)
```

```
# Compute membership values
```

```
tri = triangular(x, 2, 5, 8)
```

```
trap = trapezoidal(x, 2, 4, 6, 8)
```

```
# Plotting
```

```
plt.plot(x, tri, label='Triangular')
```

```
plt.plot(x, trap, label='Trapezoidal')
```

```
plt.title('Membership Functions')
```

```
plt.xlabel('x')
```

```
plt.ylabel('Membership')
```

```
plt.legend()
```

```
plt.grid(True)
```

```
plt.show()
```

```
#2A simple fuzzy inference system (fis)

import numpy as np
import skfuzzy as fuzz
from skfuzzy import control as ctrl

temperature = ctrl.Antecedent(np.arange(0, 41, 1), 'temperature')
heater = ctrl.Consequent(np.arange(0, 101, 1), 'heater')

temperature['cold'] = fuzz.trimf(temperature.universe, [0, 0, 20])
temperature['warm'] = fuzz.trimf(temperature.universe, [15, 25, 35])
temperature['hot'] = fuzz.trimf(temperature.universe, [30, 40, 40])

heater['low'] = fuzz.trimf(heater.universe, [0, 0, 50])
heater['medium'] = fuzz.trimf(heater.universe, [25, 50, 75])
heater['high'] = fuzz.trimf(heater.universe, [50, 100, 100])

rule1 = ctrl.Rule(temperature['cold'], heater['high'])
rule2 = ctrl.Rule(temperature['warm'], heater['medium'])
rule3 = ctrl.Rule(temperature['hot'], heater['low'])

heater_ctrl = ctrl.ControlSystem([rule1, rule2, rule3])
heater_sim = ctrl.ControlSystemSimulation(heater_ctrl)

heater_sim.input['temperature'] = 100
heater_sim.compute()

print("Temperature: 100°C")
print("Heater Output:", heater_sim.output['heater'])
```

#3A McCulloch-Pitts neuron for AND gate

# Inputs and expected output

inputs = [(0, 0), (0, 1), (1, 0), (1, 1)]

# Weights and threshold for AND gate

weights = [1, 1]

threshold = 2

print("AND Gate using McCulloch-Pitts Neuron:")

for x1, x2 in inputs:

# Weighted sum

net\_input = x1 \* weights[0] + x2 \* weights[1]

# Activation function (step function)

output = 1 if net\_input >= threshold else 0

print(f"Input: ({x1}, {x2}) → Output: {output}")

#3B McCulloch-Pitts Neuron for OR Gate

# Inputs and expected output

inputs = [(0, 0), (0, 1), (1, 0), (1, 1)]

# Weights and threshold for OR gate

weights = [1, 1]

threshold = 1

print("OR Gate using McCulloch-Pitts Neuron:")

for x1, x2 in inputs:

# Weighted sum

net\_input = x1 \* weights[0] + x2 \* weights[1]

# Activation function (step function)

output = 1 if net\_input >= threshold else 0

print(f"Input: ({x1}, {x2}) → Output: {output}")

# 5(A) Adaline Implementation

import numpy as np

# Step 1: Generate synthetic linearly separable data

```
X = np.array([[1, 1],
              [2, 1],
              [1, 2],
              [2, 2],
              [3, 1],
              [3, 2],
              [3, 4],
              [4, 3],
              [4, 4]])
```

y = np.array([-1, -1, -1, -1, 1, 1, 1, 1, 1]) # Binary class labels

# Step 2: Add bias term to input

X\_bias = np.c\_[np.ones((X.shape[0], 1)), X] # Add bias as first column

# Step 3: Adaline Training Function

def adaline\_train(X, y, lr=0.01, epochs=20):

weights = np.zeros(X.shape[1])

for epoch in range(epochs):

output = np.dot(X, weights)

error = y - output

weights += lr \* X.T.dot(error)

return weights

# Step 4: Train the model

weights = adaline\_train(X\_bias, y)

# Step 5: Prediction

```
def predict(X, weights):  
    X_bias = np.c_[np.ones((X.shape[0], 1)), X]  
    return np.where(np.dot(X_bias, weights) >= 0, 1, -1)
```

# Step 6: Test the model

```
X_test = np.array([[1, 1], [4, 4], [2.5, 2.5]])  
predictions = predict(X_test, weights)  
print("Predictions:", predictions)
```

# 5(B) Adaline Error vs Epoch Graph

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

# Step 1: Generate simple dataset

```
X = np.array([[1], [2], [3], [4], [5]])
```

```
y = np.array([-1, -1, 1, 1, 1])
```

# Step 2: Add bias term

```
X_bias = np.c_[np.ones((X.shape[0], 1)), X]
```

# Step 3: Adaline with error tracking

```
def adaline_train_error(X, y, lr=0.01, epochs=20):
```

```
    weights = np.zeros(X.shape[1])
```

```
    errors = []
```

```
    for epoch in range(epochs):
```

```
        output = np.dot(X, weights)
```

```
        error = y - output
```

```
        weights += lr * X.T.dot(error)
```

```
        mse = (error**2).mean()
```

```
        errors.append(mse)
```

```
    return weights, errors
```

# Step 4: Train model and collect errors

```
weights, errors = adaline_train_error(X_bias, y)
```

# Step 5: Plot error vs epochs

```
plt.plot(range(1, len(errors)+1), errors, marker='o')
```

```
plt.xlabel('Epochs')
```

```
plt.ylabel('Mean Squared Error')
```

```
plt.title('Adaline - Error vs Epoch')
```

```
plt.grid(True)
```

```
plt.show()
```



#6.A

#XOR Problem with Backpropagation

import numpy as np

# Activation and its derivative

def sigmoid(x): return 1 / (1 + np.exp(-x))

def sigmoid\_derivative(x): return x \* (1 - x)

# Input/Output data

X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])

y = np.array([[0], [1], [1], [0]])

np.random.seed(1)

# Initialize weights and biases

w\_h = np.random.random((2, 4)) - 1 # Weights, hidden layer

bh = np.random.random((1, 4)) - 1 # Bias, hidden layer

w\_o = np.random.random((4, 1)) - 1 # Weights, output layer

bo = np.random.random((1, 1)) - 1 # Bias, output layer

lr = 0.1 # Learning rate

epochs = 10000

print("Training on XOR problem...")

for i in range(epochs):

# Forward propagation

h\_in = np.dot(X, w\_h) + bh

h\_out = sigmoid(h\_in)

o\_in = np.dot(h\_out, w\_o) + bo

o\_out = sigmoid(o\_in)

```
# Backpropagation

err_out = y - o_out
err_out = err_out * sigmoid_derivative(o_out)
err_h = err_out.dot(w_o.T) * sigmoid_derivative(h_out)

# Update weights and biases

w_h += X.T.dot(err_h) * lr
w_o += h_out.T.dot(err_out) * lr
bh += np.sum(err_h, axis=0, keepdims=True) * lr
bo += np.sum(err_out, axis=0, keepdims=True) * lr

print("Training complete.")
print("Final predictions:\n", o_out)
```

#P.7 (A)

#Implement GA to maximize  $f(x) = x^2$

```
import random
```

```
# Objective function
```

```
def fitness(x):
```

```
    return x**2
```

```
# Create initial population
```

```
def create_population(size, lower, upper):
```

```
    return [random.randint(lower, upper) for _ in range(size)]
```

```
# Selection (tournament style)
```

```
def select(population):
```

```
    a, b = random.sample(population, 2)
```

```
    return a if fitness(a) > fitness(b) else b
```

```
# Crossover (average of parents)
```

```
def crossover(parent1, parent2):
```

```
    return (parent1 + parent2) // 2
```

```
# Mutation (small random change)
```

```
def mutate(x, lower, upper, mutation_rate=0.1):
```

```
    if random.random() < mutation_rate:
```

```
        return random.randint(lower, upper)
```

```
    return x
```

```
# GA main loop
```

```
def genetic_algorithm(generations=20, pop_size=6, lower=-10, upper=10):
```

```
    population = create_population(pop_size, lower, upper)
```

```
    for gen in range(generations):
```

```
new_population = [ ]  
for _ in range(pop_size):  
    p1 = select(population)  
    p2 = select(population)  
    child = crossover(p1, p2)  
    child = mutate(child, lower, upper)  
    new_population.append(child)  
population = new_population  
best = max(population, key=fitness)  
print(f"Gen {gen+1}: Best = {best}, Fitness = {fitness(best)}")
```

# Run the GA

```
genetic_algorithm()
```

#P.7.B

#Compare different crossover/mutation rates

import random

# Objective function

def fitness(x):

return x \*\* 2

# Create initial population

def create\_population(size, lower, upper):

return [random.randint(lower, upper) for \_ in range(size)]

# Selection (tournament style)

def select(population):

a, b = random.sample(population, 2)

return a if fitness(a) > fitness(b) else b

# Crossover with crossover rate

def crossover(parent1, parent2, crossover\_rate):

if random.random() < crossover\_rate:

return (parent1 + parent2) // 2

return parent1

# Mutation with mutation rate

def mutate(x, lower, upper, mutation\_rate):

if random.random() < mutation\_rate:

return random.randint(lower, upper)

return x

# Genetic Algorithm with customizable rates

```
def genetic_algorithm(crossover_rate, mutation_rate, generations=20, pop_size=6, lower=-10, upper=10):
```

```
    population = create_population(pop_size, lower, upper)
```

```
    print(f"\nRunning GA with crossover_rate={crossover_rate}, mutation_rate={mutation_rate}")
```

```
    for gen in range(generations):
```

```
        new_population = []
```

```
        for _ in range(pop_size):
```

```
            p1 = select(population)
```

```
            p2 = select(population)
```

```
            child = crossover(p1, p2, crossover_rate)
```

```
            child = mutate(child, lower, upper, mutation_rate)
```

```
            new_population.append(child)
```

```
    population = new_population
```

```
    best = max(population, key=fitness)
```

```
    print(f"Gen {gen+1}: Best = {best}, Fitness = {fitness(best)}")
```

```
# Run GA with different configurations
```

```
genetic_algorithm(0.9, 0.05) # High crossover, low mutation
```

```
genetic_algorithm(0.6, 0.2) # Moderate crossover, higher mutation
```

```
# P.9.A
```

```
#Hebbian Learning Binary Input-Output
```

```
# Binary input-output pairs
```

```
inputs = [[1, 0], [0, 1], [1, 1]]
```

```
outputs = [1, 1, 0]
```

```
# Initialize weights
```

```
weights = [0, 0]
```

```
print("Initial Weights:", weights)
```

```
# Hebb Rule:  $\Delta w = x * y$ 
```

```
for x, y in zip(inputs, outputs):
```

```
    for i in range(len(weights)):
```

```
        weights[i] += x[i] * y
```

```
    print(f"After input {x}, output {y} → Weights: {weights}")
```

```
print("Final Weights:", weights)
```

```
# P.9.B.

#Hebbian Learning Modified Inputs

# New input-output pairs
new_inputs = [[1, 1], [0, 0], [1, 0]]
new_outputs = [1, 0, 1]

# Initialize weights
weights = [0, 0]
print("Initial Weights:", weights)

# Apply Hebb Rule with new data
for x, y in zip(new_inputs, new_outputs):
    for i in range(len(weights)):
        weights[i] += x[i] * y
    print(f"After input {x}, output {y} → Weights: {weights}")

print("Final Weights:", weights)
```



#P.10.A

#1D SOM Implementation on 2D Data

import numpy as np

import matplotlib.pyplot as plt

# Generate simple 2D dataset (two clusters)

np.random.seed(0) # for reproducibility

```
data = np.vstack([
    np.random.randn(50, 2) + np.array([2, 2]),
    np.random.randn(50, 2) + np.array([-2, -2])
])
```

# SOM parameters

n\_neurons = 10

n\_epochs = 50

learning\_rate = 0.3

sigma = 2.0 # neighbourhood width

# Initialize neuron weights randomly in 2D space

weights = np.random.rand(n\_neurons, 2) \* 4 - 2 # values in range [-2, 2]

# Training loop

for epoch in range(n\_epochs):

for x in data:

# Find Best Matching Unit (BMU)

bmu\_index = np.argmin(np.linalg.norm(weights - x, axis=1))

# Update BMU and its neighbours

for i in range(n\_neurons):

dist = abs(i - bmu\_index)

h = np.exp(-dist\*\*2 / (2 \* sigma\*\*2))

```
weights[i] += learning_rate * h * (x - weights[i])
```

```
# Plot final weights and data
```

```
plt.scatter(data[:, 0], data[:, 1], c='gray', alpha=0.5, label="Data")
```

```
plt.plot(weights[:, 0], weights[:, 1], 'ro-', label="SOM Neurons")
```

```
plt.legend()
```

```
plt.title("1D SOM on 2D Data")
```

```
plt.grid(True)
```

```
plt.show()
```

```

#P.10.B

#Visualizing Neighbourhood Effects

import numpy as np
import matplotlib.pyplot as plt

# Create simple 2D dataset in [-1, 1] range
np.random.seed(42)
data = np.random.rand(100, 2) * 2 - 1 # shape: (100, 2)

# SOM parameters
n_neurons = 8
epochs = 30
lr = 0.2 # initial learning rate
sigma = 1.5

# Initialize neurons in a straight line from [-1, -1] to [1, 1]
weights = np.linspace([-1, -1], [1, 1], n_neurons)

plt.ion() # interactive mode on

# Training loop
for epoch in range(epochs):
    for x in data:
        # Find Best Matching Unit (BMU)
        bmu_index = np.argmin(np.linalg.norm(weights - x, axis=1))

        # Update BMU and its neighbors
        for i in range(n_neurons):
            dist = abs(i - bmu_index)
            h = np.exp(-dist**2 / (2 * sigma**2)) # neighborhood function
            weights[i] += lr * h * (x - weights[i])

```

```
# Live plot update
```

```
plt.clf()
```

```
plt.scatter(data[:, 0], data[:, 1], c='lightgray', label="Data")
```

```
plt.plot(weights[:, 0], weights[:, 1], 'ro-', linewidth=2, label="SOM Neurons")
```

```
plt.title(f"Epoch {epoch+1}")
```

```
plt.legend()
```

```
plt.pause(0.3)
```

```
plt.ioff() # turn off interactive mode
```

```
plt.show()
```

```
#OP WILL BE 30 epoch
```