# UGANDA MARTYRS UNIVERSITY

## UNIVERSITY EXAMINATIONS

## FACULTY OF SCIENCE

## DEPARTMENT OF MATHEMATICS

## END OF SEMESTER FINAL ASSESSMENT

SEMESTER I August 2022/23 Intake (Nkozi Main Campus)

# FIRST YEAR EXAMINATIONS FOR BACHELOR OF BUSINESS ADMINISTRATION AND MANAGEMENT (BAM I NKOZI CAMPUS )

## Fundamentals of Mathematics

#### FOM 1101

DATE:  $14^{th}$  December 2022

TIME: 9:30 AM - 12:30 PM

**DURATION: 3 Hrs** 

## Instructions

- 1. Carefully read through ALL the questions before attempting.
- 2. ANSWER FOUR (4) Questions (All questions carry equal marks).
- 3. Ensure that your Reg. number is indicated on all pages of your work.
- 4. Ensure that your work is clear and readable. Untidy work will be penalized.
- 5. Any type of examination Malpractice will lead to automatic disqualification.
- Do not write anything on the question paper.

# QUESTION ONE

- (a) Write TRUE or FALSE.
  - (i) P = 6 if  $729 = 3^P$ .

[2 Marks]

(ii)  $4 + X^5 = (4 + X)^5$ 

[2 Marks]

(iii)  $\left(\frac{125}{27}\right)^{-\frac{1}{3}} = \frac{3}{5}$ .

[2 Marks]

(iv)  $\log_9 3 - 2\log_9 6 + \log_9 12 = 0$ .

[2 Marks]

(v) X = 3 is a root of  $X^2 - 5X + 6$ .

[2 Marks]

- (b) Solve for t
  - (i)  $3^{2t+1} + 3 = 10(3^t)$ .

[5 Marks]

(ii)  $16^{2t-1} \times 4^{4t-2} = 32$ .

[5 Marks]

(c) Solve for x in the equation

$$3 + \log_2(x - 5) = \log_2(3x + 4)$$

[5 Marks]

## QUESTION TWO

- (a) Simplify
  - (i)  $\frac{s-t}{6s-6t}$ ,

[2 Marks]

(ii)  $\frac{b+c}{b^2-c^2}.$ 

[2 Marks]

- (b) Solve
  - (i)  $\frac{x}{6} + \frac{(3x-2)}{4} = \frac{(x+5)}{8}$

[4 Marks]

(ii) 7(p+3) = 9 - 3p

[4 Marks]

(iii)  $\frac{5}{3x} + \frac{5}{4x} = \frac{7}{12}$ 

[4 Marks]

(c) Make m the subject in the formula

$$S = \frac{3r}{2x - m} - 1.$$

[4 Marks]

(d) Given that

$$P = 4\pi \sqrt{\frac{R}{Q}},$$

find the value of Q when R = 230,  $\pi = 3.142$  and A = 12

[5 Marks]

## QUESTION THREE

(a) Solve the simultaneous equations

$$x - 3y = 5$$

$$3y + 2x = 10$$

[4 Marks]

(b) Solve the quadratic equations

(i)  $3x^2 + 5x + 2 = 0$  by the quadratic formula.

[4 Marks]

(ii)  $2y^2 - 14y + 20 = 0$  by completing the square.

[4 Marks]

(c) When ten times a number is reduced by 12, the result is equal to twice the square of the number. Find the number. [4 Marks]

(d) Solve the simultaneous equations

$$6m + 9 = n$$

$$n = 2m^2 - 3m$$

[9 Marks]

## QUESTION FOUR

(a) If 
$$T = \begin{pmatrix} 4 & 2 \\ 5 & 1 \end{pmatrix}$$
 find the values of the

unknowns in 
$$2\begin{pmatrix} 2x & 4y \\ 3z & u \end{pmatrix} + 2T = 3T$$

[4 Marks]

(b) The determinant of  $A=\begin{pmatrix} 3r & 4\\ 3 & r \end{pmatrix}$  is 0. Calculate the possible values of r.

[4 Marks]

(c) Find the determinant of

(i) 
$$B = \begin{pmatrix} 3 & 2 & 1 \\ 3 & 2 & 1 \\ 1 & 0 & 2 \end{pmatrix}$$

[4 Marks]

(ii) 
$$N = \begin{pmatrix} 2 & 0 & 0 & 0 & 0 \\ 7 & 1 & 0 & 0 & 0 \\ -9 & 5 & 3 & 0 & 0 \\ 10 & 0 & 1 & 2 & 0 \\ 2 & 10 & 22 & 15 & 1 \end{pmatrix}$$

[4 Marks]

- (d) A poultry farm has 3 units A, B and C. Unit A produces 20 trays of eggs and 40 broilers every month. Unit B produces 30 trays of eggs and 50 broilers every month. Unit C produces 35 trays of eggs and 45 broilers during the same period. If a tray of eggs costs Shs. 9,000 and a broiler costs Shs. 15,000
  - (i) Represent the above information in matrix form of order  $3 \times 2$  for eggs and broilers. [2 Marks]
  - (ii) Form a  $2 \times 1$  matrix for the eggs and broilers sold on the farm. [2 Marks]
  - (iii) Use matrix multiplication to find the total sales of the farm if all eggs and broilers were sold. [5 Marks]

## QUESTION FIVE

(a) Differentiate with respect to the independent variable x

(i) 
$$y = 4x^3 - 3x^2 - 2x + 12$$

[2 Marks]

(i) 
$$y = (x^4 + 5x)^3$$

[2 Marks]

(ii) 
$$y = e^{3x}(x^2 + 12)$$

[2 Marks]

(iii) 
$$f(x) = \frac{x^2}{3+x}$$

[2 Marks]

(b) Find

(i) 
$$\int 4x^3 - 3x^2 - 2x + 12 \ dx$$

[2 Marks]

(ii) 
$$\int \frac{(3x^2 - 3)}{x^3 - 3x} dx$$

[3 Marks]

(ii) 
$$\int_{1}^{2} (\frac{2x}{x^2} + e^{2x}) dx$$

[3 Marks]

(c) If  $f(x) = x^2(3 - 2x)$  find the

(i) value of f(x) when x = 2,

[3 Marks]

(ii) gradient function f'(x)

[3 Marks]

(iii) slope for the graph of f(x) at the point where the x coordinate is 2.

[3 Marks]

End