

23MA101 - Matrices and Calculus

UNIT 4
Simha's Classes

Integrals

Substitution method

1.Evaluate $\int \sqrt{a^2 - x^2} \, dx$ by using substitution rule.

Solution: [Click Here](#)

2.Evaluate $\int x^3 \sqrt{x^2 + 1} \, dx$

Solution: [Click Here](#)

3.Evaluate $\int x \sqrt{1 + x - x^2} \, dx$

Solution: [Click Here](#)

4.Evaluate $\int_0^1 \frac{dx}{(1 + \sqrt{x})^4}$

Solution: [Click Here](#)

5.Evaluate $\int \frac{\sqrt{9 - x^2}}{x^2} \, dx$ using trigonometric substitution.

Solution: [Click Here](#)

Integration by parts

1.Evaluate $\int e^{ax} \cos bx \, dx$

Solution: [Click Here](#)

2.Evaluate $\int e^{ax} \sin bx \, dx$

Solution: [Click Here](#)

3.Evaluate $\int_0^\infty e^{-ax} \cos bx \, dx$.

Solution: [Click Here](#)

4.Evaluate $\int_0^{\infty} e^{-ax} \sin bx \, dx$

Solution: [Click Here](#)

5.Evaluate $\int \frac{(\log x)^2}{x^2} \, dx$

Solution: [Click Here](#)

Integration by method of partial fractions

1.Evaluate $\int \frac{3x+1}{(x-1)^2(x+3)} \, dx$

Solution: [Click Here](#)

2.Evaluate $\int \frac{x^2+2x-1}{2x^3+3x^2-2x} \, dx$

Solution: [Click Here](#)

3.Integrate $\int_0^{\frac{\pi}{2}} \frac{\sin x \cos x}{\cos^2 x + 3 \cos x + 2} \, dx.$

Solution: [Click Here](#)

Property

1.Evaluate $\int_0^{\frac{\pi}{4}} \log(1 + \tan \theta) \, d\theta$

Solution: [Click Here](#)

2.Evaluate $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x} + \sqrt{x}} \, dx$

Solution: [Click Here](#)

3. Evaluate $\int_0^{\frac{\pi}{2}} \log \sin x dx$ and hence find the value of $\int_0^1 \frac{\sin^{-1} x}{x} dx$.

Solution: [Click Here](#)

Integration function involving in square root

1. Evaluate $\int \frac{dx}{\sqrt{3x - x^2 - 2}}$.

Solution: [Click Here](#)

2. Evaluate $\int \frac{3x - 2}{\sqrt{4x^2 - 4x - 5}} dx$.

Solution: [Click Here](#)

3. Evaluate $\int \frac{2x + 5}{\sqrt{x^2 - 2x + 10}} dx$.

Solution: [Click Here](#)

4. Evaluate $\int \frac{x}{\sqrt{x^2 + x + 1}} dx$.

Solution: [Click Here](#)