

NC Assignment 1

11762 Muhammad Kashif

Question 1 Derivative

Code

```
import math as m
import sympy as s
x = s.Symbol('x')
eq = s.sqrt(x)-s.cos(x)
ans = s.diff(eq).evalf(subs={x:2})
print("True Value = ",ans)
a = m.sqrt(2+0.3)-m.cos(2+0.3)
b = m.sqrt(2)-m.cos(2)
apprx = (a-b)/0.3
print("Approximatly value = ",apprx)
print("True Error = ",abs(apprx-ans))
```

Output

```
True Value = 1.26285081741896
Approximatly value = 1.1749690372329877
True Error = 0.0878817801859677
```

Question 2 RegulaFalsi Method

Code

```
def f(x):
    return m.exp(-2*x)+4*x**2-36
def RegulaFalsi(xL,xU):
    for i in range(15):
        xR = ((xL*f(xU))-(xU*f(xL)))/(f(xU)-f(xL))
        print(" ",i,"t\t",round(xL,4),"t\t",round(xU,4),"t\t",round(xR,4),"t\t",abs(round(f(xR),4)))

        if f(xR)<0:
            xU = xR
        else:
            xL = xR
        if abs(f(xR))<= 0.0001:
            break
print("=====")
print("Regula Falsi Method")
print("=====")
print("Iteration\txL\t\txU\t\txR\t\tTolerance")
RegulaFalsi(1,2)
```

Output

```
=====
Regula Falsi Method
=====
Iteration      xL      2      xU      xR      Tolerance
0              1              3.6815      18.2155
1      3.6815      2      2.8796      2.8274
2      3.6815      2.8796      2.9874      0.2994
3      3.6815      2.9874      2.9986      0.0307
4      3.6815      2.9986      2.9998      0.0031
5      3.6815      2.9998      2.9999      0.0003
6      3.6815      2.9999      2.9999      0.0
```

Code

```
import numpy as np
def f(x):
    return 2*x - np.exp(x) + 3*np.cos(x)
def muller( x0, x1, x2):
    for i in range(100):
        h1 = x1 - x0
        h2 = x2 - x1
        d1 = (f(x1) - f(x0)) / h1
        d2 = (f(x2) - f(x1)) / h2
        d = (d2 - d1) / (h2 + h1)
        b = d2 + h2*d
        D = np.sqrt(b**2 - 4*f(x2)*d)
        if abs(b-D) < abs(b+D):
            E = b + D
        else:
            E = b - D
        h = -2*f(x2) / E
        p = x2 + h
        print(" ",i,"t\t",round(x0,5),"t",round(x1,5),"t",round(x2,5),"t",round(p,5),"t",round(abs(h),5))
        if abs(h) < 0.00001:
            break
        x0 = x1
        x1 = x2
        x2 = p
print("=====")
print("                Muller's Method")
print("=====")
print("Iteration\tx0\ttx1\ttx2\ttxR\tTolerance")
muller(-2, 0, 2)
```

Output

```
=====
                        Muller's Method
=====
Iteration      x0      x1      x2      xR      Tolerance
0             -2      0      2      1.12278      0.87722
1             0      2      1.12278      1.23721      0.11443
2             2      1.12278      1.23721      1.2397      0.00249
3             1.12278      1.23721      1.2397      1.23971      1e-05
4             1.23721      1.2397      1.23971      1.23971      0.0
```

Question 4 Prove $A(BC)=AB+BC$

Code

```
import numpy as np
A= np.array([[1,2,3],[4,5,6]])
B= np.array([[2,3],[4,5],[6,7]])
C = np.array([[9,3],[1,2]])
result1 = np.array([[0,0],[0,0],[0,0]])
result = np.array([[0,0],[0,0]])
result2 = np.array([[0,0],[0,0],[0,0]])
result3 = np.array([[0,0],[0,0]])
print("A(BC) = AB + BC")
#BC
for i in range(3):
    for j in range(2):
        for k in range(2):
            result1[i,j] +=B[i,k]*C[k,j]
#A(BC)
for i in range(2):
    for j in range(2):
        for k in range(3):
            result[i,j] += A[i,k]*result1[k,j]
print("A(BC)")
print(result)
#AB
for i in range(2):
    for j in range(2):
        for k in range(3):
            result3[i,j] +=A[i,k]*B[k,j]
print("AB")
print(result3)
print("BC")
print(result1)
print("AB + BC is not possible because the size of the matrix is not same")
```

Output

```
A(BC) = AB + BC
A(BC)
[[ 286  152]
 [ 655  350]]
AB
[[ 28  34]
 [ 64  79]]
BC
[[ 21  12]
 [ 41  22]
 [ 61  32]]
AB + BC is not possible because the size of the matrix is not same
```
