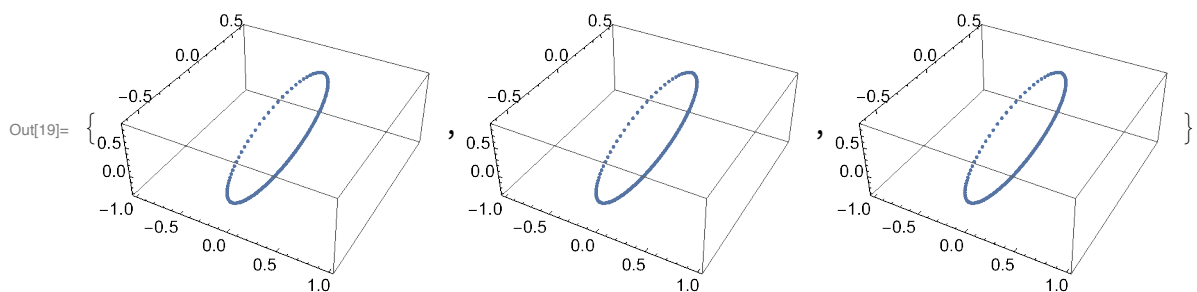
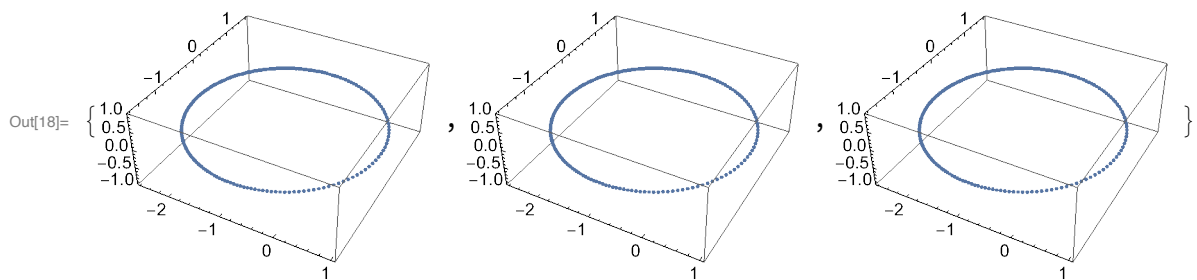


Лабораторная 4 (MPI + OMP)

```
In[1]:= ClearAll["Global`*"];  
SetDirectory[NotebookDirectory[]];
```

Проверка (+cuda)

```
In[3]:= seq = Import["seq.txt", "Data"];  
tSeq = seq[[;;, 1]];  
xSeq = seq[[;;, 2 ;; 4]];  
vSeq = seq[[;;, 13 ;; 15]];  
mpi = Import["mpi.txt", "Data"];  
tMpi = mpi[[;;, 1]];  
xMpi = mpi[[;;, 2 ;; 4]];  
vMpi = mpi[[;;, 13 ;; 15]];  
cuda = Import["cuda.txt", "Data"];  
tCuda = cuda[[;;, 1]];  
xCuda = cuda[[;;, 2 ;; 4]];  
vCuda = cuda[[;;, 13 ;; 15]];  
On[Assert];  
Assert[Norm[Flatten[seq[[;;, 2 ;;]]] - Flatten[mpi[[;;, 2 ;;]]] == 0.0];  
Assert[Norm[Flatten[seq[[;;, 2 ;;]]] - Flatten[cuda[[;;, 2 ;;]]] == 0.0];  
{ListPointPlot3D[xSeq], ListPointPlot3D[xMpi], ListPointPlot3D[xCuda]}  
{ListPointPlot3D[vSeq], ListPointPlot3D[vMpi], ListPointPlot3D[vCuda]}
```



Порядок

```

In[20]:= tauInit = 0.1;
orderExact = 2;
trajCnt = 4;
runsCnt = 5;
tau =  $\frac{\text{tauInit}}{\text{orderExact}^\#}$  & /@ Range[0, runsCnt - 1];
data = Import[ToString[#] <> ".txt", "Data"] & /@ tau;
trajCalc = {data[[#, ;;, 2 ;; 4]], data[[#, ;;, 5 ;; 7]],
             data[[#, ;;, 8 ;; 10]], data[[#, ;;, 11 ;; 13]]} & /@ Range[runsCnt];
trajExact = Import["traj" <> ToString[#] <> ".txt", "Data"][[;;, 2 ;; 4]] & /@
             Range[trajCnt];
(*trajCalc[[4,1]]
   trajExact[[1]]*)
err = Norm[Flatten[trajExact] - Flatten[trajCalc[[#]]], 1] & /@ Range[runsCnt];
orderCalc = Log[err[[1 ;; runsCnt - 1]] / err[[2 ;; runsCnt]]] / Log[orderExact];
Grid[{{{" $\tau$ ", "Err =  $\|u - y_\tau\|$ ", "Order =  $\frac{\text{Log}\left[\frac{\|u - y_\tau\|}{\|u - y_{\tau/2}\|}\right]}{\text{Log}[2]}$ "}}} ~
      Join~Transpose@{tau, err, Append[orderCalc, "-"]}, Frame → All]

```

Out[30]=

τ	Err = $\ u - y_\tau\ $	Order = $\frac{\text{Log}\left[\frac{\ u - y_\tau\ }{\ u - y_{\tau/2}\ }\right]}{\text{Log}[2]}$
0.1	10.799	1.92766
0.05	2.83857	1.96654
0.025	0.726294	1.98743
0.0125	0.183162	2.00891
0.00625	0.0455086	-

Проверка для большой задачи

```

In[31]:= seq = ToExpression[StringSplit[#]] & /@ Import["seq_10000.txt", "Data"];
xSeq = seq[[;;, 2 ;; 4]];
vSeq = seq[[;;, 23 ;; 25]];
mpi = ToExpression[StringSplit[#]] & /@ Import["mpi_10000.txt", "Data"];
xMpi = mpi[[;;, 2 ;; 4]];
vMpi = mpi[[;;, 23 ;; 25]];
On[Assert];
Assert[Norm[Flatten[seq[[;;, 2 ;;]]] - Flatten[mpi[[;;, 2 ;;]]] == 0.0];

```

Сравнение результатов для различных пар (np, nth)

N = 10000

Time seq: 7.856 secs

(2 процесса на разных узлах)

np = 2

nth = 1
Time mpi: 4.162 secs
Acceleration: **1.88755**

(2 процесса на одном узле)
np = 2
nth = 1
Time mpi: 4.132 secs
Acceleration: **1.90126**

(3 процесса на разных узлах)
np = 3
nth = 1
Time mpi: 2.868 secs
Acceleration: **2.73919**

(3 процесса на одном узле)
np = 3
nth = 1
Time mpi: 2.749 secs
Acceleration: **2.85777**

(4 потока на 1 узле)
np = 1
nth = 4
Time mpi + omp: 2.06 secs
Acceleration: **3.81359**

(8 потоков на 2 узлах)
np = 2
nth = 4
Time mpi + omp: 1.283
Acceleration: **6.12315**

(12 потоков на 3 узлах)
np = 3
nth = 4
Time mpi + omp: 0.941
Acceleration: **8.34857**

Сравнение результатов для различных значений числа точек

(N = 5000)

Time exec: 2.78783

Time copy: 0.000324736

Time cuda: 1.525 (Tesla T4)

Time seq: 4.232

Acceleration: **2.7751**

(N = 20000)

Time exec: 10.7356

Time copy: 0.00101994

Time cuda: 5.561 (Tesla T4)

Time seq: 32.935

Acceleration: **5.9225**

(N = 50000)

Time exec: 52.5237

Time copy: 0.00201072

Time cuda: 26.536 (Tesla T4)

Time seq: 208.012

Acceleration: **7.83886**