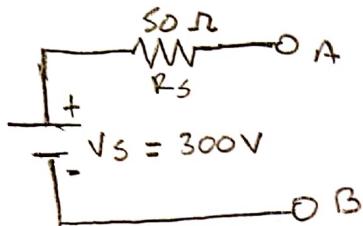


Sección 8-3 Conversiones de Fuente

1.- Una fuente de voltaje tiene los valores $V_s = 300\text{ V}$ y $R_s = 50\text{ }\Omega$.
Conviéntala en una fuente de corriente equivalente.



Solución

$$I_s = \frac{V_s}{R_s}$$

$$I_s = \frac{300\text{ V}}{50\text{ }\Omega}$$

$$\underline{I_s = 6\text{ A}}$$

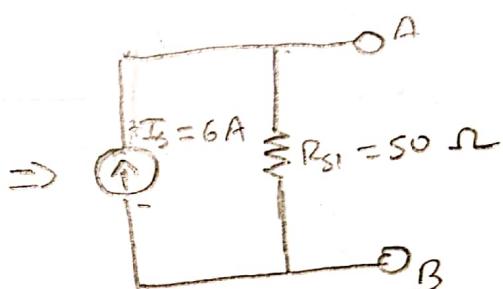
$$R_s = R_{s1}$$

$$R_{s1} = 50\text{ }\Omega$$

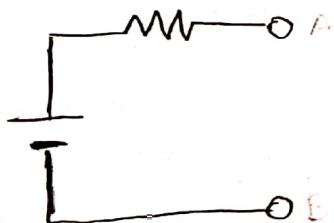
Datos

$$V_s = 300\text{ V}$$

$$R_s = 50\text{ }\Omega$$



3.- Una batería tipo D nueva tiene entre sus terminales un voltaje de 1.6 V y puede suministrar hasta 8.0 A a un cortocircuito durante muy poco tiempo. ¿Cuál es la resistencia interna de la batería?



Solución

$$V_s = I_s \cdot R_s$$

$$R_s = \frac{V_s}{I_s}$$

Datos

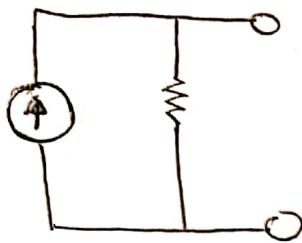
$$V_s = 1.6\text{ V}$$

$$I_s = 8.0\text{ A}$$

$$R_s = \frac{1.6\text{ V}}{8.0\text{ A}}$$

$$\underline{R_s = 200\text{ m}\Omega}$$

5.- Una fuente de corriente tiene una I_s de 600mA y una R_s de $1,2\text{k}\Omega$.
Conviéntela en una fuente de voltaje equivalente.



Solución

$$I_s = \frac{V_s}{R_s}$$

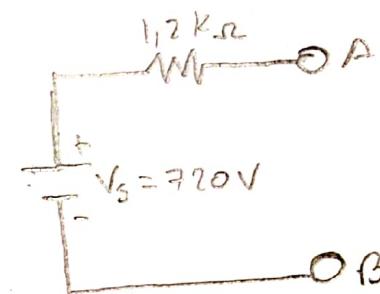
$$V_s = I_s R_s$$

$$V_s = 600\text{m} \cdot 1,2\text{k}$$

$$\underline{V_s = 720\text{ V}}$$

$$R_s = R_{s1}$$

$$R_{s1} = 1,2\text{k}\Omega$$



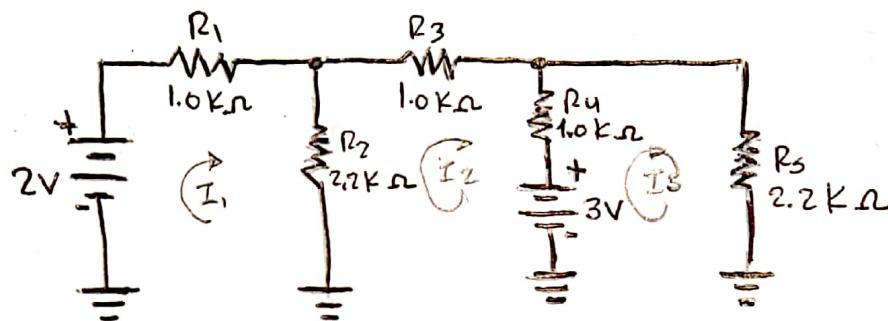
Datos

$$I_s = 600\text{mA}$$

$$R_s = 1,2\text{k}\Omega$$

Sección 8-4 El teorema de superposición

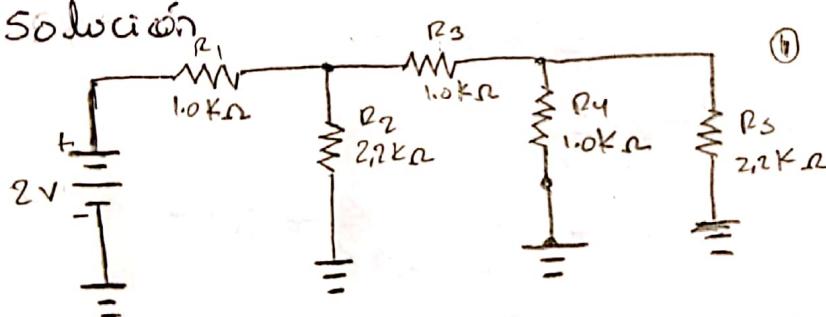
T.: Con el método de superposición, encuentre la corriente a través de R_S en la figura.



1ero

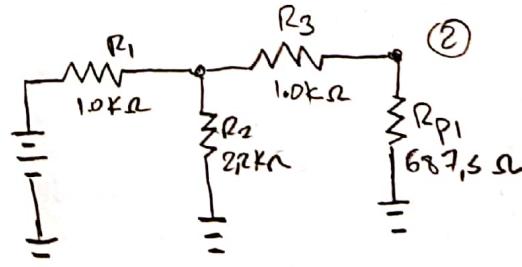
Apagamos todas las fuentes independientes dejando la que se procedera analizar. Determinamos la corriente de salida. Repetimos por cada una de las fuentes independientes.

Solución



Divisor de corriente con V_{S1}

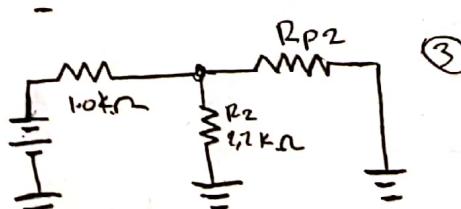
$$I_{TS1} = \frac{V_{S1}}{R_{TS1}}$$



$$R_{P1} = R_4 \parallel R_S$$

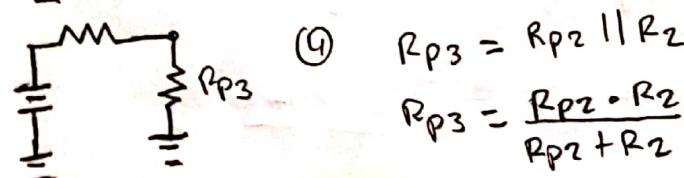
$$R_{P1} = \frac{R_4 \cdot R_S}{R_4 + R_S} \rightarrow R_{P1} = \frac{1K \cdot 2,2K}{1K + 2,2K}$$

$$\rightarrow R_{P1} = 687,5 \Omega$$



$$R_{P2} = R_3 + R_{P1}$$

$$R_{P2} = 1K + 687,5 \rightarrow R_{P2} = 1687,5 \Omega$$



$$R_{P3} = R_{P2} \parallel R_2$$

$$R_{P3} = \frac{R_{P2} \cdot R_2}{R_{P2} + R_2} \rightarrow R_{P3} = \frac{1687,5 \cdot 2,2K}{1687,5 + 2,2K}$$

$$\rightarrow R_{P3} = 954,98 \Omega$$

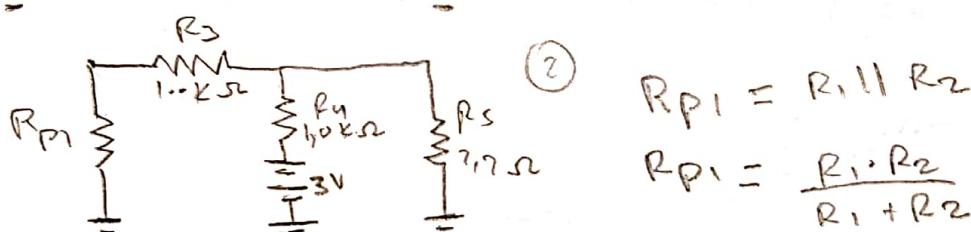
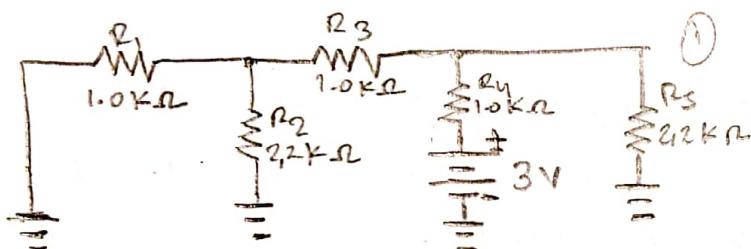
$$\rightarrow R_{TS1} = R_1 + R_{P3} \rightarrow R_{TS1} = 1K + 954,98 \rightarrow R_{TS1} = 1954,98 \Omega$$

$$\rightarrow I_{TS1} = \frac{V_{S1}}{R_{TS1}} \rightarrow I_{TS1} = \frac{2V}{1954,98\Omega} \rightarrow I_{TS1} = 1,023 \text{ mA}$$

$$+ I_{RSS1} = \left(\frac{R_4}{R_S + R_4} \right) I_{TS1} \rightarrow I_{RSS1} = \left(\frac{1K}{2,7K + 1K} \right) \cdot 1,023 \text{ mA}$$

$$\rightarrow I_{RSS1} = 0,313 \text{ mA}$$

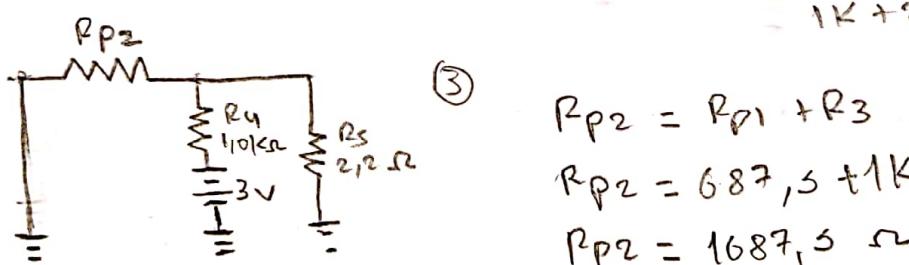
Divisor de corriente con V_{S2}



$$RP_1 = R_1 \parallel R_2$$

$$RP_1 = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

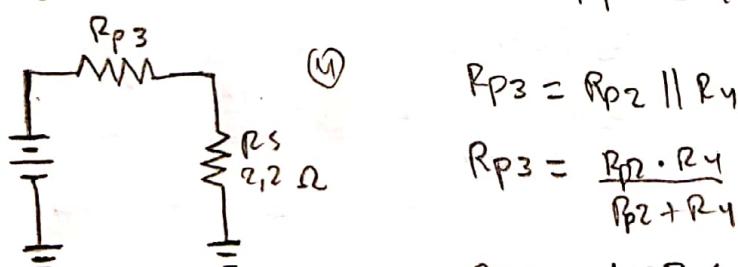
$$RP_1 = \frac{1K \cdot 2,2K}{1K + 2,2K} \rightarrow RP_1 = 687,5 \Omega$$



$$RP_2 = RP_1 + R_3$$

$$RP_2 = 687,5 + 1K$$

$$RP_2 = 1687,5 \Omega$$



$$RP_3 = RP_2 \parallel R_4$$

$$RP_3 = \frac{RP_2 \cdot R_4}{RP_2 + R_4}$$

$$RP_3 = \frac{1687,5 \cdot 1K}{1687,5 + 1K}$$

$$RP_3 = 627,91 \Omega$$

$$\rightarrow R_{TS2} = RS + RP_3 \rightarrow R_{TS2} = 2,2K + 627,91 \rightarrow R_{TS2} = 2827,91 \Omega$$

$$\rightarrow I_{TS2} = \frac{V_{S2}}{R_{TS2}} \rightarrow I_{TS2} = \frac{3V}{2827,91\Omega} \rightarrow I_{TS2} = 1,06 \text{ mA}$$

$$\rightarrow I_{RSS_2} = \left(\frac{R_3}{R_S + R_3} \right) I_{TS_2} \rightarrow I_{RSS_2} = \left(\frac{1K}{1,2K + 1K} \right) \cdot 1,06 \times 10^{-3}$$

$$\rightarrow \underline{\underline{I_{RSS_2} = 0,331 \text{ mA}}}$$

2do

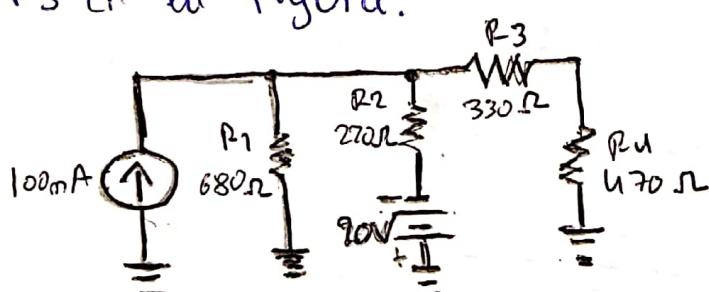
Hallamos la contribución total sumando algebraicamente todas las contribuciones debidas a las fuentes independientes.

$$I_{es} = I_{RSS_1} + I_{RSS_2}$$

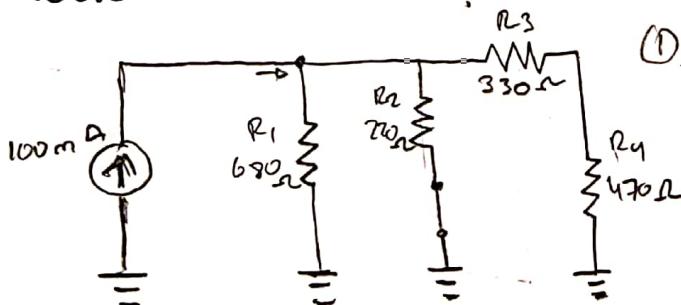
$$I_{RS} = 0,318 \times 10^{-3} + 0,331 \times 10^{-3}$$

$$\underline{\underline{I_{es} = 0,651 \text{ mA}}} //$$

9: Con el teorema de superposición, determine la corriente a través de R_3 en la figura.



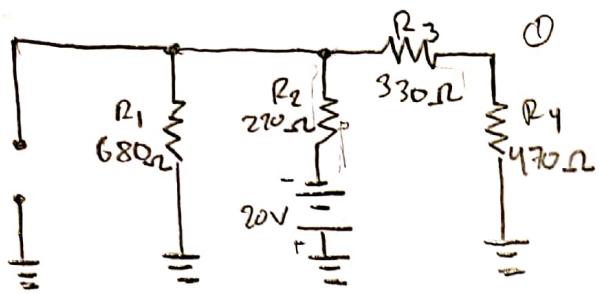
Solución



División de corriente con I_s .

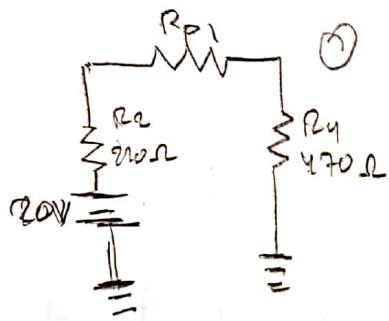
$$I_{R3S_1} = \frac{I_s (R_2)}{R_1 + R_2 + R_3 + R_4} \rightarrow I_{R3S_1} = \frac{100 \times 10^{-3} \cdot 270}{680 + 270 + 330 + 470}$$

$$\rightarrow I_{R3S_1} = 0,0129 \text{ A}$$



División de corriente con V_{S2}

$$I_{TS1} = \frac{V_{S2}}{R_{TS2}}$$



$$R_{P1} = R_1 \parallel R_3$$

$$R_{P1} = \frac{R_1 \cdot R_3}{R_1 + R_3} \rightarrow R_{P1} = \frac{680 \cdot 330}{680 + 330}$$

$$\rightarrow R_{P1} = 222,18 \Omega$$

$$R_{TS2} = R_{P1} + R_4 + R_2$$

$$R_{TS2} = 222,18 + 470 + 220$$

$$R_{TS2} = 912,18 \Omega$$

$$I_{TS2} = \frac{20V}{912,18} \rightarrow I_{TS2} = 0,022 A$$

$$I_{R3S2} = \left(\frac{R_1}{R_3 + R_1} \right) I_{TS2} \rightarrow I_{R3S2} = \left(\frac{680}{330 + 680} \right) \cdot 0,022$$

$$\rightarrow I_{R3S2} = 0,015 A$$

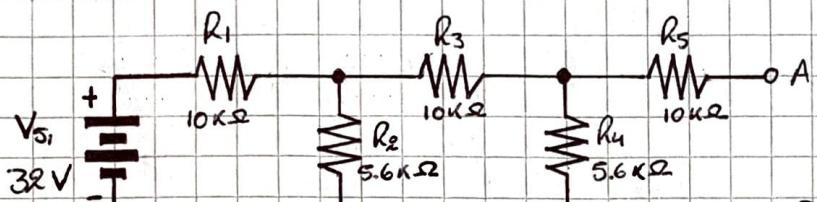
$$I_{R3} = I_{R3S1} + I_{R3S2}$$

$$I_{R3} = 0,0129 + 0,015$$

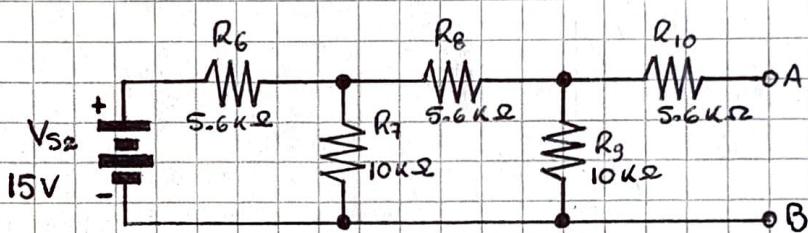
$$\underline{I_{R3} = 0,026 A \parallel},$$

Sección 8.4 El teorema de superposición

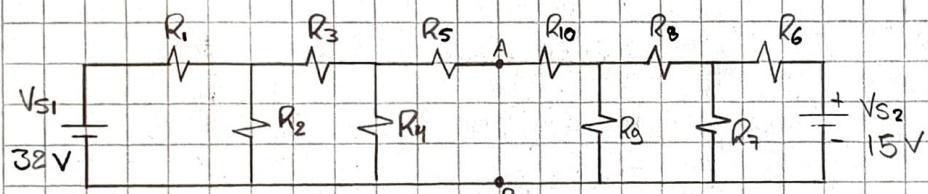
* 15.- La figura 8-75 muestra dos redes en escalera. Determine la corriente producida por cada uno de las baterías cuando se conectan las terminales A (A a A) y las terminales B (B a B).



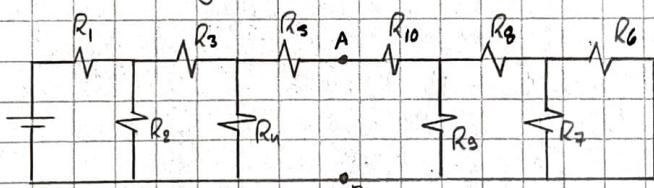
(a)



(b)

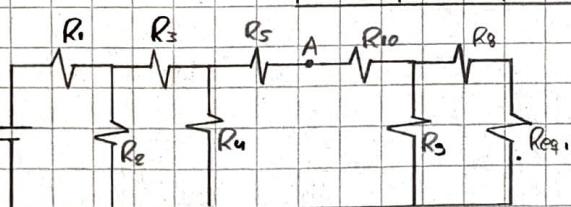


Apagando V_{S2}

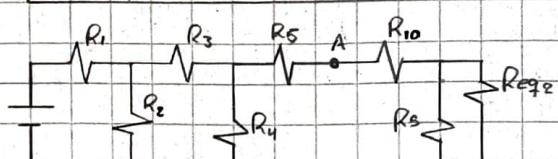


$R_6 \parallel R_7$

$$R_{eq1} = \frac{10 \cdot 5.6}{10 + 5.6} = 3.59 \text{ k}\Omega$$

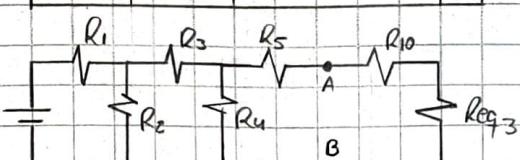


$$R_{eq2} = R_8 + R_{eq1} = 5.6 + 3.59 = 9.19 \text{ k}\Omega$$

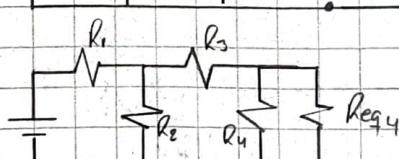


$R_9 \parallel R_{eq2}$

$$R_{eq3} = \frac{10 \cdot (9.19)}{10 + 9.19} = 4.79 \text{ k}\Omega$$

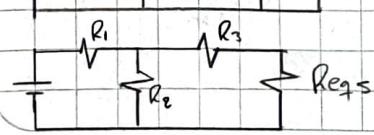


$$R_{eq4} = R_5 + R_{10} + R_{eq3} = 10 + 5.6 + 4.79 = 20.39 \text{ k}\Omega$$

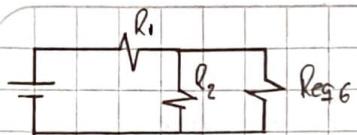


$R_6 \parallel R_{eq4}$

$$R_{eq5} = \frac{(5.6)(20.39)}{5.6 + 20.39} = 4.39 \text{ k}\Omega$$

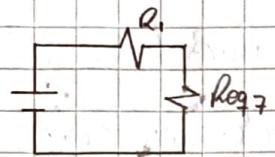


$$R_{eq6} = R_3 + R_{eq5} = 10 + 4.39 = 14.39 \text{ k}\Omega$$

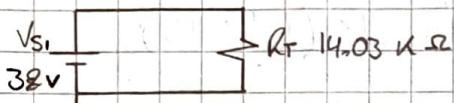


$R_2 \parallel R_{req6}$

$$R_{req6} = \frac{(5.6)(14.39)}{5.6 + 14.39} = 4.03 \text{ k}\Omega$$



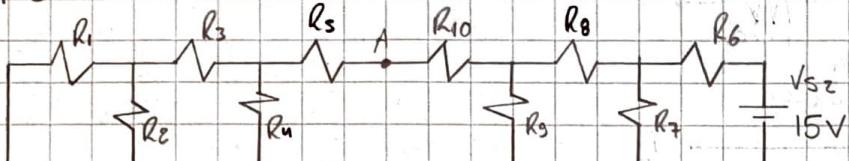
$$R_T = R_1 + R_{req7} = 10 + 4.03 = 14.03 \text{ k}\Omega$$



$$I = \frac{32 \text{ V}}{14.03 \cdot 10^3 \text{ }\Omega} = 2.28 \cdot 10^{-3}$$

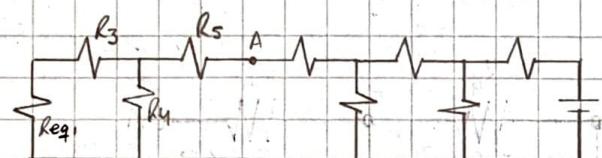
$$I = 2.28 \text{ mA}$$

Apagando V_{S1}

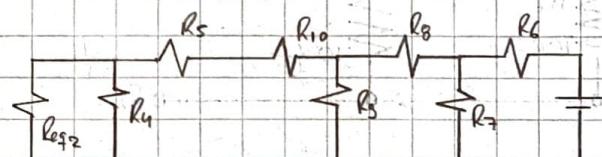


$R_1 \parallel R_2$

$$R_{req1} = \frac{(10)(5.6)}{10 + 5.6} = 3.59 \text{ k}\Omega$$

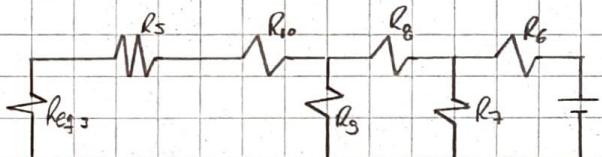


$$R_{req2} = R_{req1} + R_3 = 3.59 + 10 = 13.59 \text{ k}\Omega$$

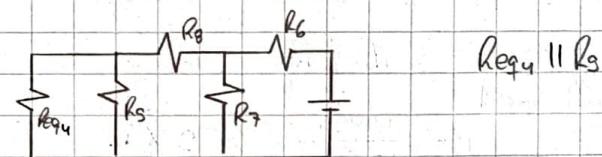


$R_{req2} \parallel R_4$

$$R_{req3} = \frac{13.59(5.6)}{13.59 + 5.6} = 3.97 \text{ k}\Omega$$

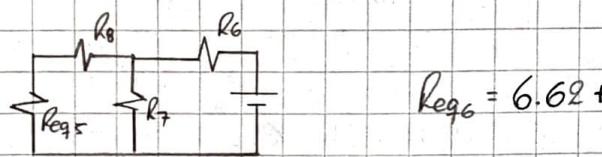


$$R_{req4} = 3.97 + 10 + 5.6 = 19.57 \text{ k}\Omega$$

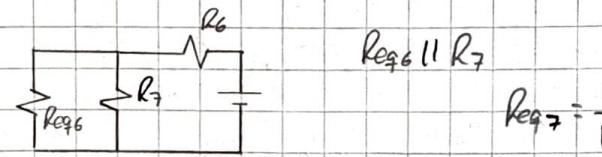


$R_{req4} \parallel R_3$

$$R_{req5} = \frac{(19.57)(10)}{19.57 + 10} = 6.62 \text{ k}\Omega$$

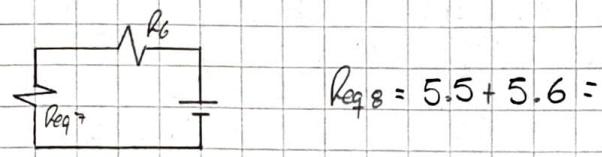


$$R_{req6} = 6.62 + 5.6 = 12.22 \text{ k}\Omega$$

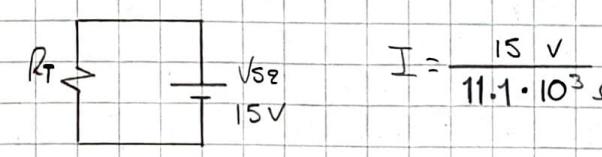


$R_{req6} \parallel R_7$

$$R_{req7} = \frac{(12.22)(10)}{12.22 + 10} = 5.5 \text{ k}\Omega$$



$$R_{req8} = 5.5 + 5.6 = 11.1 \text{ k}\Omega = R_T$$

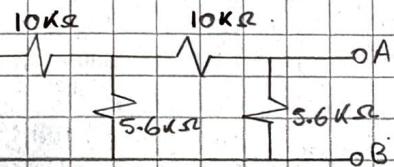
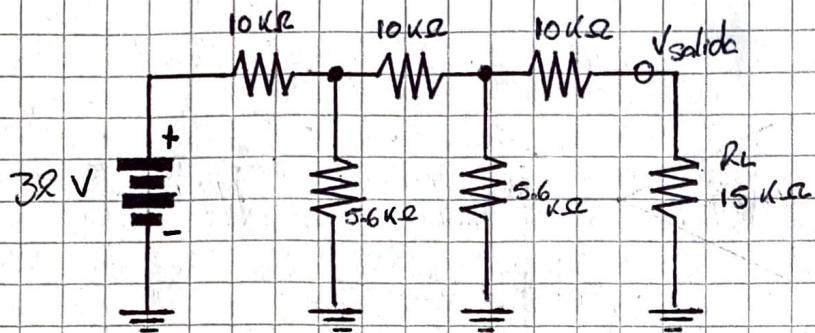


$$I = \frac{15 \text{ V}}{11.1 \cdot 10^3 \text{ }\Omega} = 1.35 \cdot 10^{-3} \text{ A}$$

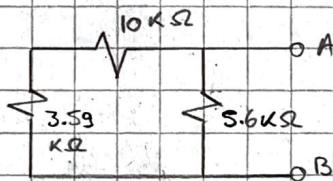
$$I = 1.35 \text{ mA}$$

Sección 8.5 Teorema de Thevenin

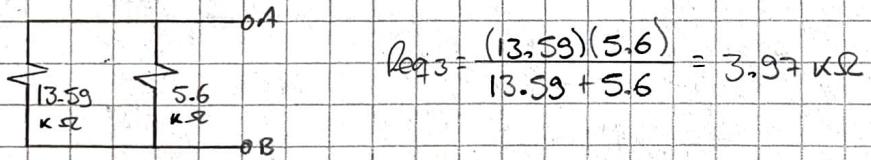
17.- Con el teorema de Thevenin, determine la corriente a través de la carga R_L en la figura 8-77.



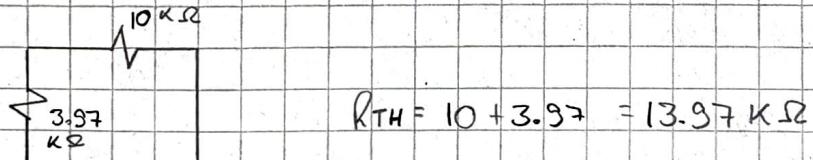
$$R_{\text{req}_1} = \frac{(10)(5.6)}{10 + 5.6} = 3.59 \text{ k}\Omega$$



$$R_{\text{req}_2} = 10 + 3.59 = 13.59 \text{ k}\Omega$$

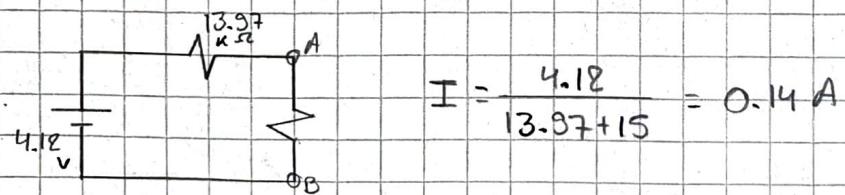


$$R_{\text{req}_3} = \frac{(13.59)(5.6)}{13.59 + 5.6} = 3.97 \text{ k}\Omega$$



$$R_{\text{TH}} = 10 + 3.97 = 13.97 \text{ k}\Omega$$

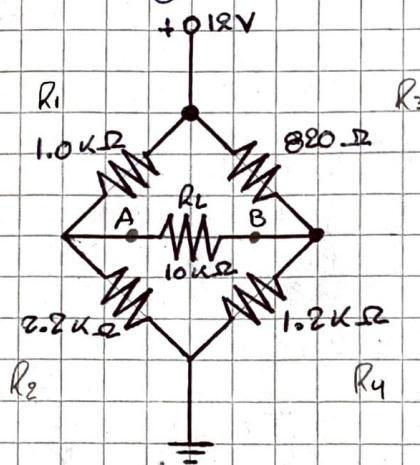
$$\boxed{R_{\text{TH}} = 13.97 \text{ k}\Omega}$$



$$I = \frac{4.18}{13.97 + 15} = 0.14 \text{ A}$$

$$\boxed{I_L = 0.14 \text{ A.}}$$

* 21.- Determine la corriente a través del resistor de carga en el circuito puente de la figura 8-81.

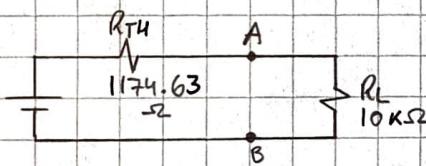


$$V_{TH} = V_A - V_B = 12 \left(\frac{2.2 \cdot 10^3}{2.2 \cdot 10^3 + 1 \cdot 10^3} \right) - 12 \left(\frac{1.2 \cdot 10^3}{820 + 1.2 \cdot 10^3} \right) = 1.12 \text{ V}$$

$$V_{TH} = 1.12 \text{ V.}$$

$$R_{TH} = \frac{(1 \cdot 10^3)(2.2 \cdot 10^3)}{1 \cdot 10^3 + 2.2 \cdot 10^3} + \frac{(820)(1.2)(10^3)}{820 + 1.2 \cdot 10^3} = 1174.63 \Omega$$

$$R_{TH} = 1174.63 \Omega$$



$$V_L = \left(\frac{10 \cdot 10^3}{10 \cdot 10^3 + 1174.63} \right) \cdot (1.12) = 1.00227 \text{ V}$$

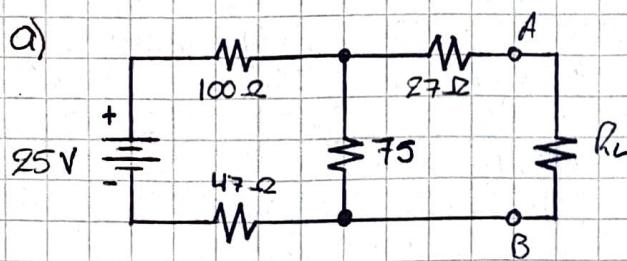
$$V_L = 1.00227 \text{ V.}$$

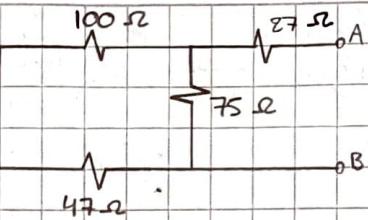
$$I_L = \frac{V_L}{R_L} = \frac{1.00227}{10 \cdot 10^3} = 100 \mu\text{A}$$

$$I_L = 100 \mu\text{A.}$$

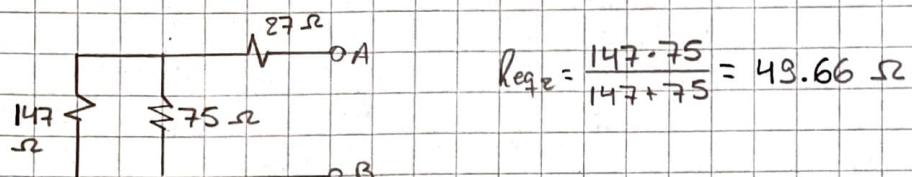
Sección 8.6 Teorema de Norton

23.- Para cada uno de los circuitos mostrados en la figura 8-76, determine el equivalente Norton visto por R_L .

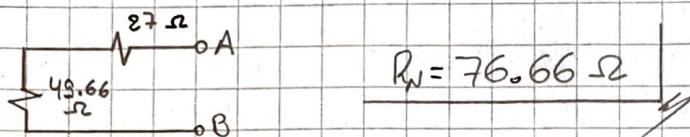




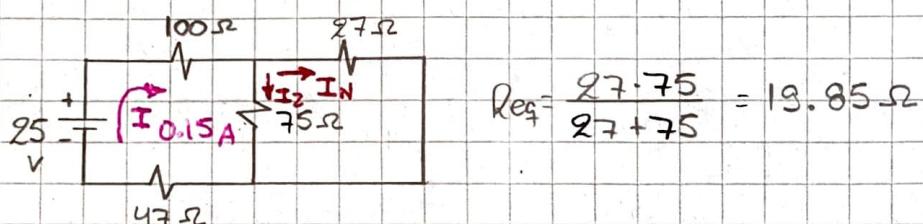
$$R_{eq1} = 100 + 47 = 147 \Omega$$



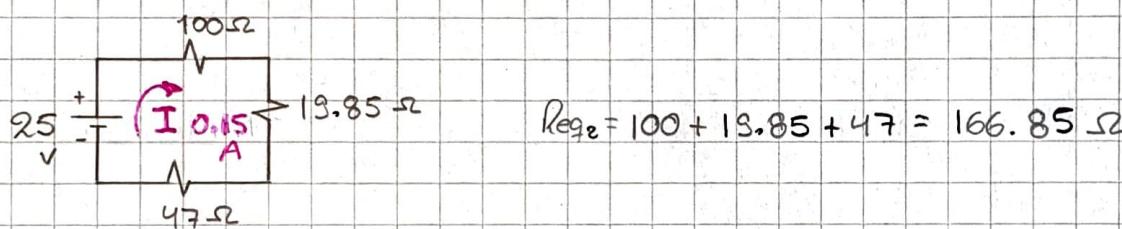
$$R_{eq2} = \frac{147 \cdot 75}{147 + 75} = 49.66 \Omega$$



$$R_N = 76.66 \Omega$$



$$R_{eq} = \frac{27 \cdot 75}{27 + 75} = 19.85 \Omega$$



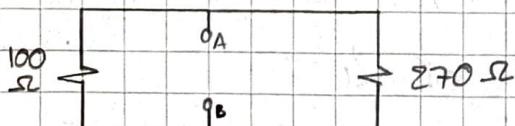
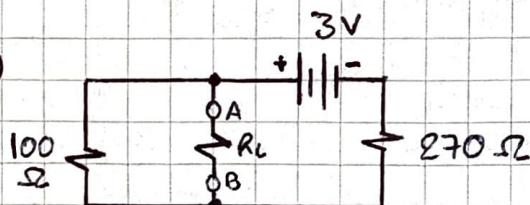
$$R_{eq2} = 100 + 19.85 + 47 = 166.85 \Omega$$

$$I = \frac{25}{166.85} = 0.15 A$$

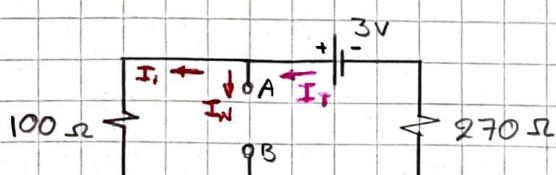
$$I_N = 0.15 \left(\frac{75}{75+27} \right) = 0.110 A$$

$$\underline{I_N = 110 mA}$$

b)



$$R_N = \frac{100 \cdot 270}{100 + 270} = 72.97 \Omega$$

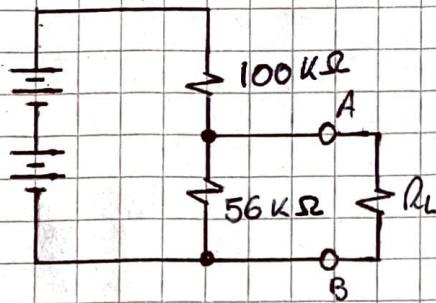


$$I_T = \frac{3}{72.97} = 0.041 A.$$

$$I_N = 0.041 \left(\frac{100}{100+270} \right) = 0.01108 A$$

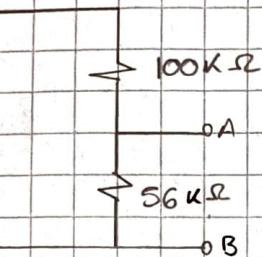
$$\underline{I_N = 11.08 mA}$$

c)

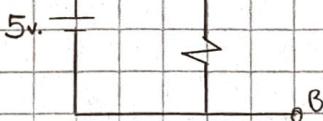


$$R_N = \frac{(100)(56)}{100 + 56} = 35.83 \text{ k}\Omega$$

$$\underline{R_N = 35.83 \text{ k}\Omega}$$



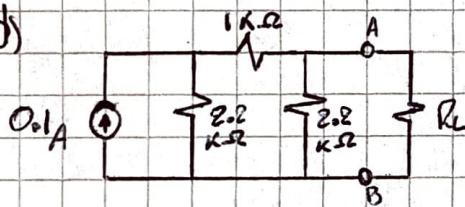
$$V_L = 5 \left(\frac{56 \cdot 10^3}{56 \cdot 10^3 + 100 \cdot 10^3} \right) = 1.79 \text{ V.}$$



$$I_N = \frac{1.79}{35.83 \cdot 10^3} = 50 \mu\text{A.}$$

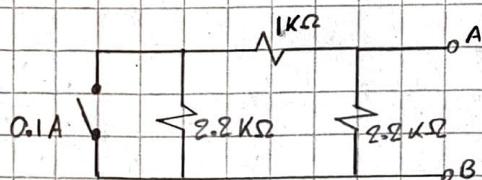
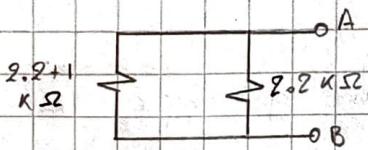
$$\underline{I_N = 50 \mu\text{A.}}$$

d)



$$R_N = \frac{(3.2)(2.2)}{3.2 + 2.2} = 1.30 \text{ k}\Omega$$

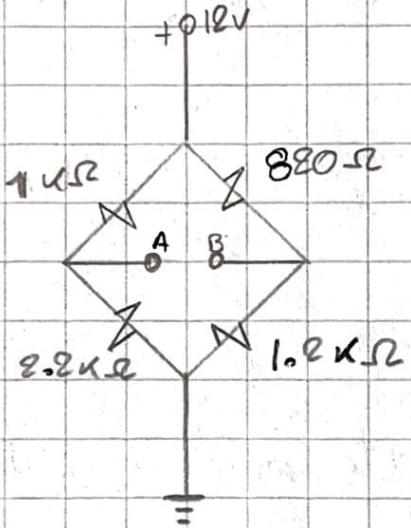
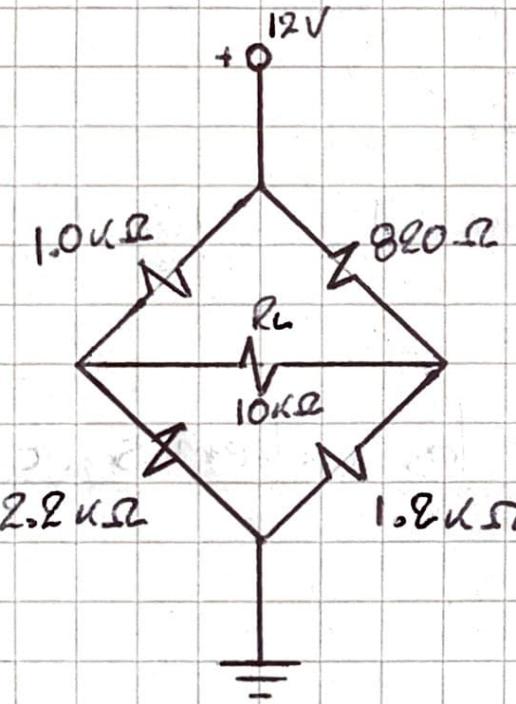
$$\underline{R_N = 1.30 \text{ k}\Omega}$$



$$I_N = 0.1 \left(\frac{2.2}{2.2 + 1} \right) = 68.75 \text{ mA.}$$

$$\underline{I_N = 68.75 \text{ mA.}}$$

27- Determine el circuito equivalente Norton para el puente que aparece en la figura 8-81 sin R_L .

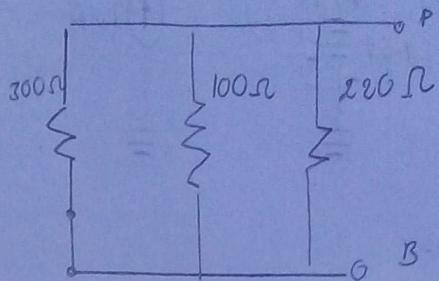
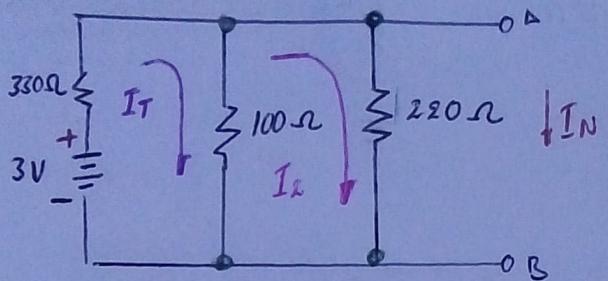


$$R_N = \frac{(10^3)(2.2 \cdot 10^3)}{10^3 + 2.2 \cdot 10^3} + \frac{(820)(1.2 \cdot 10^3)}{820 + 1.2 \cdot 10^3} = 1174.63 \Omega$$

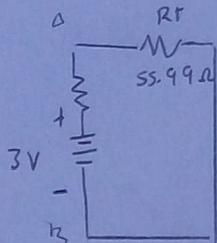
$R_N = 1174.63 \Omega$

TEOREMA DE NORTON

Aplique el teorema de Norton al circuito de la figura 8-84



OBTENER LA CORRIENTE TOTAL

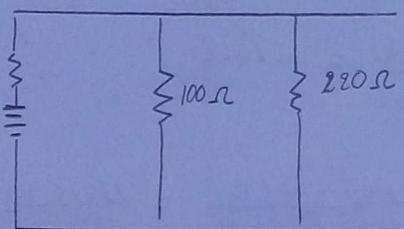


$$\frac{1}{R_T} = \frac{1}{330} + \frac{1}{100} + \frac{1}{220}$$

$$R_T = 55.93 \Omega$$

$$I_T = \frac{V_t}{R_T} = \frac{3}{55.93} = 53.96 \text{ mA}$$

OBTENCIÓN DE LA CORRIENTE DE NORTON (I_N)



$$\text{II MÓDULO 2 II}$$

$$220I_2 + 100(I_T - I_2) = 0$$

$$120I_2 + 100I_T = 0$$

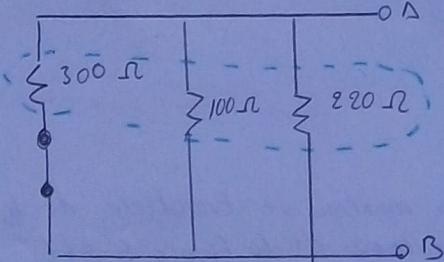
$$I_2 = \frac{-100(53.96)}{120}$$

$$I_2 = -44.71 \text{ mA}$$

$$I_2 = I_N$$

$$I_N = -44.71 \text{ mA}$$

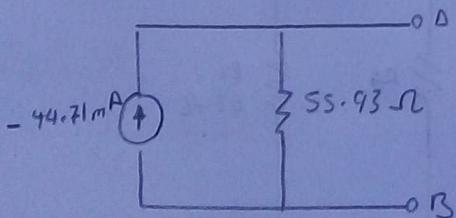
OBTENCIÓN DE LA RESISTENCIA DE NORTON



$$\frac{1}{R_T} = \frac{1}{300} + \frac{1}{100} + \frac{1}{220}$$

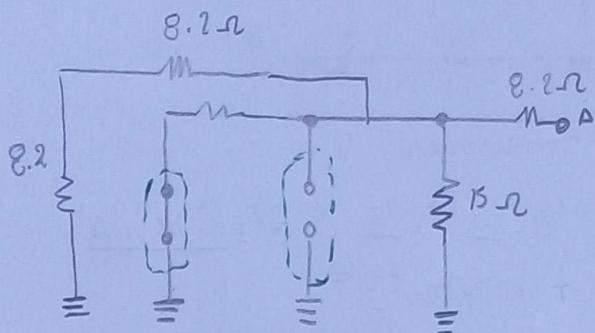
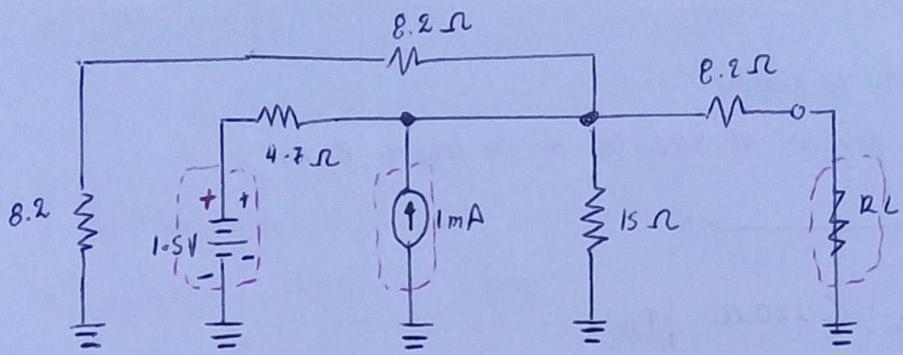
$$R_T = 55.93 \Omega$$

CIRCUITO DE NORTON



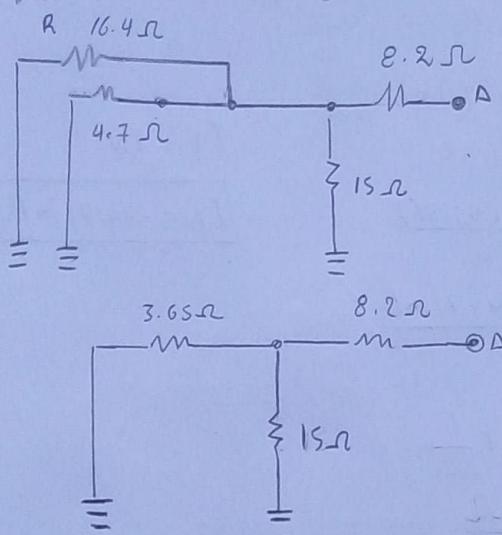
TEOREMA DE TRANSFERENCIA DE POTENCIA MÁXIMA

En el circuito de la figura 8-86 determine el valor de R_L para transferencia máxima



La fuente de voltaje se corto circuitan
La fuente de corriente se abre
La RL se abre

Reducir el circuito



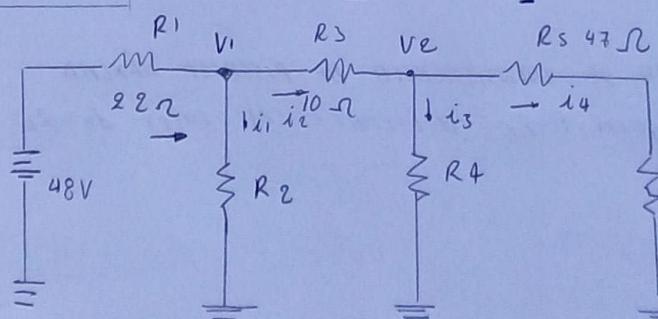
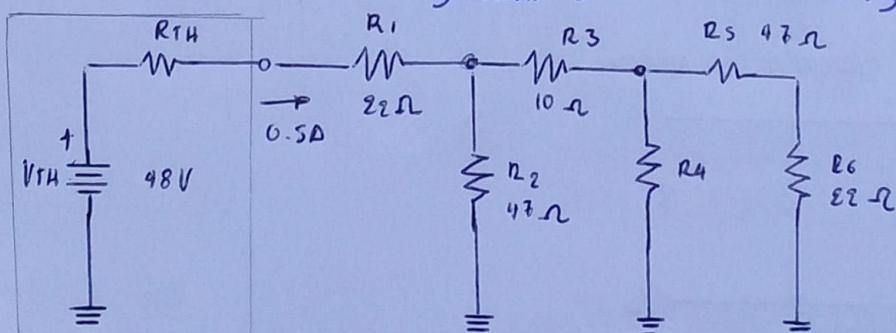
$$R_{8.2} + R_{8.2} = 16.4 \Omega$$

$$R_{16.4} \parallel R_{4.7} = \frac{16.4(4.7)}{16.4+4.7} = 3.65 \Omega$$

$$R_{8.2} + (R_{3.65} \parallel R_{15}) = 8.2 + \frac{(3.65)(15)}{3.65+15} = 11.13 \Omega$$

$$R_L = 11.1 \Omega$$

Calcule los valores de R_4 y R_{TH} cuando la potencia máxima se transfiera de la fuente thevenizada a la red en configuración de escalera de la figura 8-87?



$$i_1 = \frac{V_1 - 0}{47}$$

$$i_2 = \frac{V_1 - V_2}{10}$$

$$i_3 = \frac{V_2}{47}$$

$$i_4 = \frac{V_2}{R_4}$$

$$0 \cdot S = i_1 + i_2$$

$$0 \cdot S = \frac{V_1}{47} + \frac{V_L}{10} - \frac{V_2}{10}$$

$$\textcircled{1} \quad 0 \cdot S = 0.12V_1 - 0.1V_2$$

$$i_2 = i_4 + i_3$$

$$\frac{V_1}{10} - \frac{V_L}{10} = \frac{V_2}{R_4} + \frac{V_L}{47}$$

$$\textcircled{2} \quad 0 \cdot I = 0.12V_2 + \frac{V_L}{R_4}$$

$$V = [R]$$

$$V = (0.5)(22) = 11 \text{ V}$$

Reemplazo en $\textcircled{1}$ y en $\textcircled{2}$

$$\textcircled{3} \quad 0 \cdot S = 0.12(11) - 0.1V_2$$

$$V_2 = 8.2 \text{ V}$$

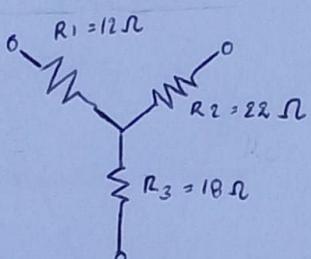
$$\textcircled{4} \quad 0 \cdot I = 0.12(8.2) + \frac{0.2}{R_4}$$

$$\boxed{R_4 = 70.64 \Omega}$$

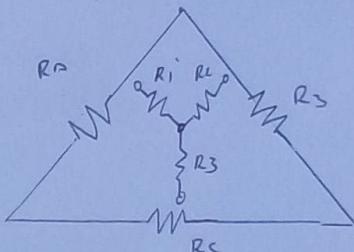
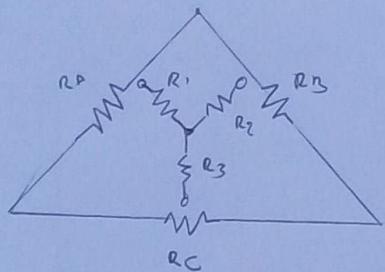
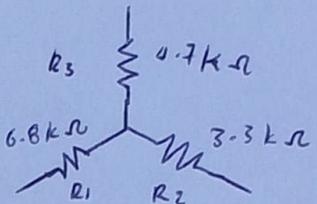
CONVERSIÓNES DELTA a Y ($\Delta A Y$) y Y a Δ

En la figura 8-89, convierte la red Y en una red delta

a)



b)



$$R_D = \frac{(R_1 \cdot R_2) + (R_2 \cdot R_3) + (R_1 \cdot R_3)}{R_2}$$

$$R_A = \frac{(12 \times 22) + (22 \times 18) + (12 \times 18)}{22}$$

$$\underline{R_A = 39.81 \Omega}$$

$$R_B = \frac{(R_1 \cdot R_2) + (R_2 \cdot R_3) + (R_1 \cdot R_3)}{R_1}$$

$$R_B = \frac{(12 \times 22) + (22 \times 18) + (12 \times 18)}{12}$$

$$\underline{R_B = 73 \Omega}$$

$$R_C = \frac{(R_1 \cdot R_2) + (R_2 \cdot R_3) + (R_1 \cdot R_3)}{R_3}$$

$$R_C = \frac{(12 \times 22) + (22 \times 18) + (12 \times 18)}{18}$$

$$\underline{R_C = 48.7 \Omega}$$

$$R_D = \frac{(R_1 \cdot R_2) + (R_2 \cdot R_3) + (R_1 \cdot R_3)}{R_2}$$

$$R_D = \frac{(6.8 \times 3.3) + (3.3 \times 4.7) + (6.8 \times 4.7)}{3.3}$$

$$\underline{R_D = 21.2 \Omega}$$

$$R_B = \frac{(R_1 \cdot R_2) + (R_2 \cdot R_3) + (R_1 \cdot R_3)}{R_1}$$

$$R_B = \frac{(6.8 \times 3.3) + (3.3 \times 4.7) + (6.8 \times 4.7)}{6.8}$$

$$\underline{R_B = 10.3 \Omega}$$

$$R_C = \frac{(R_1 \cdot R_2) + (R_2 \cdot R_3) + (R_1 \cdot R_3)}{R_3}$$

$$R_C = \frac{(6.8 \times 3.3) + (3.3 \times 4.7) + (6.8 \times 4.7)}{4.7}$$

$$\underline{R_C = 14.9 \Omega}$$