Nonparametric Statistics - Final Overview

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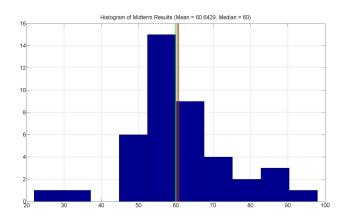
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STAT W4413: Nonparametric Statistics - Lecture 18

Grading: 30/25/45

- 30% Homeworks.
- 25% midterm exam (in class):
 - Results: Mean = 61 Median = 60
- 45% final (in class):
 - Thursday, May 12, 7:10PM-10:00PM, Schermerhorn 614
- Exams are closed-book, closed-notes.
- An Important Note: no make-up exams will be given.
- The final letter grade depends on your performance in homeworks, midterm, and final exam.

Midterm Results



Material for the Final Exam

- Lecture 10 Goodness of Fit Tests for Categorical Random Variables
- Lecture 11 Goodness of Fit Tests for Real Valued Random Variables
- Sample Problem

 Lecture 12 Two Sample Problem
- ullet Lecture 13 How to use "Goodness of fit Test" ${f Fg}$
- Lecture 14 Two Sample Problem: Permutation Test
- Lecture 15 *k*-Sample Test
- Lecture 16 Block Design Tests
- Lecture 17 Bootstrap Methods

Goodness of Fit Tests for Categorical Random Variables

Lec₁₀

- Visual Analysis of Goodness of Fit pp-plot vs. qq-plot (these plots are for both categorical and continuous random variables).
- χ²-test and examples of use. **HW**, 模拟考
- Composite null hypothesis.

Lec 10 两个例子会算

Goodness of Fit Tests for Continuous Random Variables

Lec11

Lec11 P9 P11 P14

会背会算记分布

• Kolmogorov-Smirnov test, Cramer-Von Mises and Anderson-Darling test. 双重MAX, N阶乘

Lilliefors test for composite null hypothesis

Two Sample Problem

Lec₁₂

问题定义,

• Parametric two sample tests

P6算例

Weaknesses of parametric tests

Z-test~Norm Pg8; ParVSNonpar

- Nonparametric test for the location (shift) problem
- Rank and order statistics 考算例, P24, 1/阶乘 由来
- Wilcoxon rank-sum test
 笔记本, when to use what test
 BF检验(作业), P13

最后两页PPT 优缺点!!

How to use "Goodness of fit Test"

Lec13

PP_QQ图 定义,图解 Pg7

- Example with χ^2 -test: Derive the ML for the probability of success in a sample from Binomial distribution.
- KS test vs. Lilliefors test: Why KS test is misleading?

Si no se nada de los parameters , Lilliefor; Else, KS (otherwise KS has large P-VAL)

Two Sample Problem: Permutation Test

- $L14 \circ H_0$ and H_1 of the one sided loaction (shift) problem,
 - \bullet derivation of p-value, $Pg8\sim 9$

permutation for a given data set P5

- the steps of the test, **Steps: P10**
- comparing different test statistics

Abs, Ratio??? eg P19

• two-sided location (shift) test

Perm Test要求 Exchangeable

- one-sided domination problem !!! 分部积分
- two-sided domination problem

RD P31 PPT 页尾问题

- scale problem Can you explain what the permutation test looks like with this new statistic?
- scale problem: unequal shifts and the problem of nonexchangeable datasets PG33,USE MC 模拟; TILL PG43CI

k-Sample Test

Lec15

P10, 证明 P14, 背 P15, 引理

- pairwise *T*-test vs. ANOVA to test equality of *k* means
- what is the difference between ANOVA and Kruskal-Wallis statistics?

• *k*-sample permutation test

Block Design Tests

Lec₁₆

P5表~P6的1式 Pg9 H0H1 Pg13 会算

- parametric two-way ANOVA (idea behind the test)
- permutation test Pg18 算例
- Friedman's statistics

Bootstrap Methods

L17 • Bootstrap estimates of standard errors vs. asymptotic standard errors P6 SE P10~12 两类Boot

- Bootstrap confidence intervals
- Bootstrapping regression models
- Bootstrapping regression models with heteroskedasticity

 P13
- ullet Permutation tests vs. Monte Carlo tests vs. Bootstrap tests P14
- ullet Sources of approximation error bias/variance trade-off ${f P15}$
- Parametric vs. nonparametric bootstrap

P29 data sufficiently dense

Bootstrap for dependent data from population

Format of the Final Exam

- 1. Question about a simple derivation from the lecture with hints.
- 2. A series of short questions about general understanding of different tools and methods discussed in the lecture.
- 3. Theoretical question two parts:
 - (i) an easy question like the ranks Problem 2 (a) or (b) in practice final.
 - (ii) slightly more difficult question like Problem 2 (c) in practice final.
- 4. Question which utilizes one or two test from the lecture but you do not have to memorize the test statistics.