# Pondo\_Allom\_Params

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### **Introduction:**

 $Information\ about\ allometric\ curves\ and\ functions\ used\ in\ FATES.\ https://fates-docs.readthedocs.io/en/latest/fates\_tech\_note.html\#allometry-and-growth-along-allometric-curves$ 

### Install the BAAD Package:

Install the package from github:

```
#install.packages("devtools")
#devtools::install_github("richfitz/datastorr")
#devtools::install_github("traitecoevo/baad.data")
```

#### Review the data:

```
baad <- baad.data::baad_data()
d_baad <- baad$data

# Check the data
#head(d_baad)</pre>
```

Refine (subset) the data for Pinus Ponderosa:

```
pipo <- d_baad[ which(d_baad$species == 'Pinus ponderosa'), ]

# Check the data
#head(pipo)</pre>
```

FATES allows for four different approaches to predicting height from dbh:

• A power function

$$h = p_1 * d^(p_2)$$

• O'Brien et al. (1995)

$$log_{10}Height = log_{10}DBH * slope + intercept$$

• Poorter et al. (2006)

$$h = p_1 * (1 - exp(p_2 * d^{(p_3)}))$$

• Martinex Cano et al. (2019)

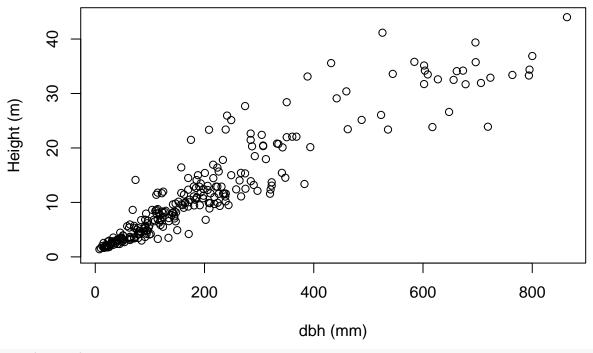
$$h = (p_1 * d^{(p_2)}/(p_3 + d^{(p_2)}))$$

For my research I use the dbh to height relationship from O'Brien et al., 1995. The log10Height (m) is regressed on log10DBH (mm). Where slope is p1 or fates\_allom\_d2h1 and intercept is p2 or fates\_allom\_d2h2 in the parameter file.

$$log_{10}Height = log_{10}DBH * slope + intercept$$

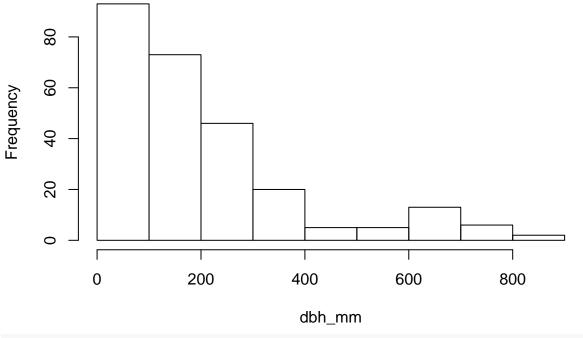
So modeled height would be. I want to solve for the best fit p1 and p2 given height and dbh data from BAAD.

$$Height = 10^{(log10(min(d,dbhmax))*p1+p2)}$$



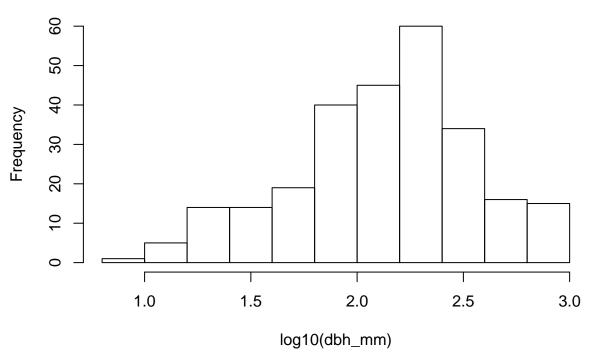
hist(dbh\_mm)

# Histogram of dbh\_mm



hist(log10(dbh\_mm))

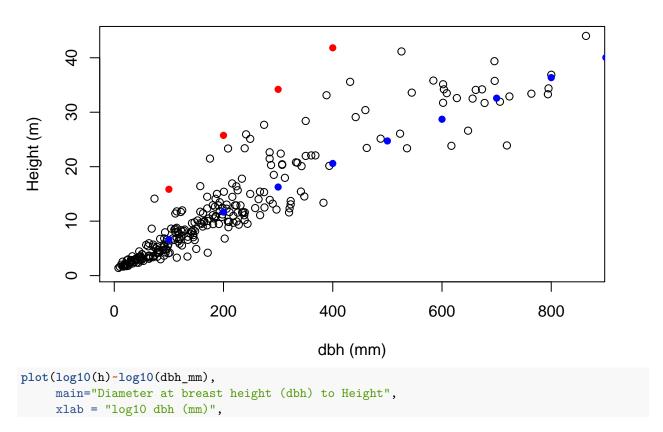
### Histogram of log10(dbh\_mm)



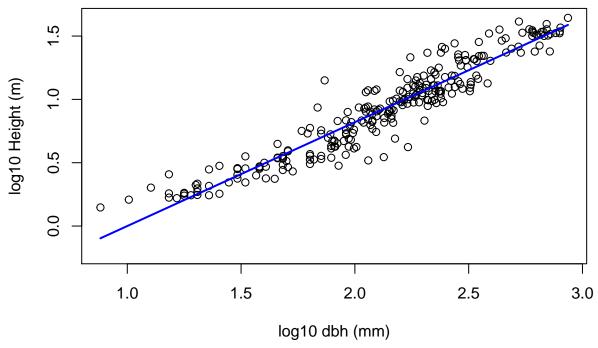
Initially I wanted to test out a simple linear function and then a log-log regression (basically O'Brien).

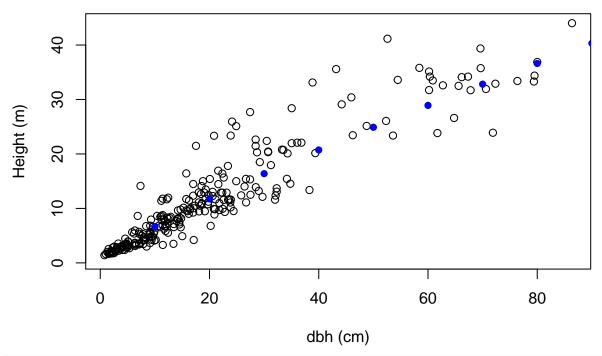
```
# But first I will test out just a linear model
d2hmod_mm \leftarrow lm(h~dbh_mm)
coef(d2hmod_mm)
## (Intercept)
                     dbh_mm
   1.88991834 0.04858541
# Then a linear model with log10(h) regressed on log10(dbh)
d2hmodlog_mm <- lm(log10(h)~log10(dbh_mm))</pre>
coef(d2hmodlog_mm)
##
     (Intercept) log10(dbh_mm)
##
      -0.8150832
                      0.8181127
d2hmodlog_cm <- lm(log10(h)~log10(dbh_cm))
coef(d2hmodlog_cm)
     (Intercept) log10(dbh_cm)
##
##
     0.003029536
                    0.818112721
Next, I will create a function to represent the O'Brien calculation used for dbh to height relationships.
obrien <- function(dbh, p1, p2){
  height <-10^{(\log 10(dbh))*} p1 + p2)
  return(height)
}
dbins_mm <- c(100,200,300,400,500,600,700,800,900) # Remember in O'Brien dbh is in mm.
dbins_cm <- c(10,20,30,40,50,60,70,80,90) # But FATES uses cm.
# Calculate the best fit parameters using dbh in cm.
```

```
# Use default parameters from O'Brien et al 1995
default_mm <- obrien(dbins_mm, 0.7, -0.2)</pre>
# Use the parameters from the log10 linear model d2hmodlog
lmfit_mm <- obrien(dbins_mm, 0.82, -0.82) # dbh in mm</pre>
lmfit_cm <- obrien(dbins_cm, 0.82, 0.003) # dbh in cm</pre>
coef(lm(default_mm~dbins_mm))
## (Intercept)
                  dbins_mm
## 11.67774249 0.07124032
coef(lm(lmfit_mm~dbins_mm))
## (Intercept)
                  dbins mm
## 3.45859976 0.04142493
coef(lm(lmfit_cm~dbins_cm))
## (Intercept)
                  dbins_cm
     3.4825736
                 0.4171207
##
plot(h~dbh_mm,
     main="Diameter at breast height (dbh) to Height",
     xlab = "dbh (mm)",
     ylab = "Height (m)")
points(default_mm~dbins_mm, col="red", pch=16) # default O'Brien slope (0.7) and intercept (-0.2)
points(lmfit_mm~dbins_mm, col="blue", pch=16) # BAAD data slope (0.82) and intercept (-0.82)
```



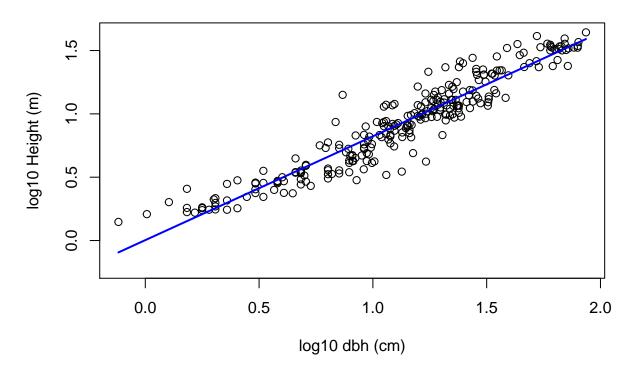
```
ylab = "log10 Height (m)")
curve(-0.82 + (0.82*x), add=T, col="blue", lwd=2) # log regression coefficients from d2hmodlog
```





```
plot(log10(h)~log10(dbh_cm),
    main="Diameter at breast height (dbh) to Height",
    xlab = "log10 dbh (cm)",
    ylab = "log10 Height (m)")
curve(0.003 + (0.82*x), add=T, col="blue", lwd=2) # log regression coefficients from d2hmodlog
```

# Diameter at breast height (dbh) to Height



#### Diameter at breast height (dbh) to above ground biomass (AGB) - d2bagw

FATES provides three different options for calculating AGB from dbh:

• Saldarriaga et al. (1998)

$$(C_{aqb} = f_{aqb} * p_1 * h^{p_2} * d^{p_3} * rho^{p_4})$$

• 2 parameter power function

$$(C_{aqb} = p_1/c2b * d^{p_2})$$

• Chave et al. (2014)

$$(C_{aqb} = p_1/c2b * (rho * d^2 * h)^{p_2})$$

For this project I will test Saldarriaga et al. (1998) as well as the 2 parameter power function.

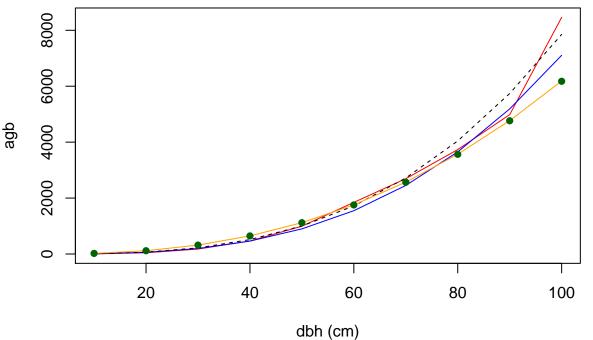
$$C_{agb} = f_{agb} * p_1 * h^{p_2} * d^{p_3} * rho^{p_4}$$

```
# In this case dbh and agb calculated from Chojnacky serves as
# the "observed data" to fit the other parameters against.
# Define the variables needed for the Saldarriaga function
rho = 0.367
f_{agb} = 0.6
d.agb \leftarrow c(10, 20, 30, 40, 50, 60, 70, 80, 90, 100)
h.agb \leftarrow c(2.82, 7.7, 13.9, 21.0, 29.1, 37.9, 37.9, 37.9, 37.9, 57.5)
#use heights from d2h
lmfit.h <- obrien(d.agb, 0.82, 0.003)</pre>
# Define the Saldarriaga function
sal <- function(f_agb, p1, h, p2, d, p3, rho, p4){</pre>
  agb <- f_agb * p1 * h^p2 * d^p3 * rho^p4
  return(agb)
}
# Define a 2 parameter power function (as a stand-in for Chojnakcy if those param values are used)
par2_pwr <- function(p1,d,p2,c2b){</pre>
  bagw <- (p1*(d^p2))/c2b
  return(bagw)
}
choj_eq <- function(b0,b1,d){</pre>
  biom <- b0 + (b1*log(d))
  return(biom)
}
choj_p1 = -2.6177
choj_p2 = 2.4638
c2b = 2
test_2par <- par2_pwr(0.146, d.agb, 2.464, c2b)
choj <- choj_eq(choj_p1, choj_p2, d.agb)</pre>
# Parameters from earlier Jupyter Notebook.
#p1 = 0.131
\#p2 = 0.626
#p3 = 2.46
#p4 = 2.18
```

```
# New parameters from bet fit below.

p1 = 0.11
p2 = 0.65
p3 = 2.45
p4 = 2.15

sal1 <- sal(f_agb, p1, h.agb, p2, d.agb, p3, rho, p4)
sal2 <- sal(f_agb, p1, lmfit.h, p2, d.agb, p3, rho, p4)
sal3 <- sal(f_agb, 0.131, lmfit.h, 0.626, d.agb, 2.46, rho, 2.18)
#plot(choj.h~d.agb, type="l", col="blue")
plot(sal1~d.agb, col="red", type="l", ylab="agb", xlab="dbh (cm)")
points(sal2~d.agb, col="blue", type="l")
points(sal3~d.agb, col="black", lty=2, type="l")
points(test_2par~d.agb, col="orange", type="l")
points(exp(choj)~d.agb, col="darkgreen", pch=16)
```



# Here I want to get the r2 or rmse to compare the different allom functions and params to the "observe

rmse <- function(y\_hat,y){
 return(sqrt(mean((y-y\_hat)^2)))
}

r2 <- function(y\_hat,y){
 RSS<-sum(((y\_hat))-(y))^2)
 TSS<-sum(((y)-(mean(y)))^2)
 return(1-RSS/TSS)}

# remember y\_hat is the model predicted aqb</pre>

 $\# y_hat(s) = test (sal), test2 (sal), test_2par, py_test (sal)$ 

# y observed = test\_choj

```
sal1_rmse <- rmse(sal1,exp(choj))
sal1_R2 <- r2(sal1, exp(choj))
sal2_rmse <- rmse(sal2,exp(choj))
sal2_R2 <- r2(sal2,exp(choj))
sal3_rmse <- rmse(sal3, exp(choj))
sal3_R2 <- r2(sal3, exp(choj))

test_2par_rmse <- rmse(test_2par, exp(choj))
test_2par_R2 <- r2(test_2par, exp(choj))
agb_rmse <- c(sal1_rmse, sal2_rmse, sal3_rmse, test_2par_rmse)
agb_r2 <- c(sal1_R2, sal2_R2, sal3_R2, test_2par_R2)
agb_names <- c("Sal test 1", "Sal test 2", "Sal test 3", "Two Param Power")
agb_mod_fits <- data.frame(agb_rmse, agb_r2, row.names = agb_names)
agb_mod_fits</pre>
```

```
## Sal test 1 734.098689 0.8675944

## Sal test 2 347.141465 0.9703919

## Sal test 3 636.566290 0.9004400

## Two Param Power 3.794937 0.9999965
```

### Diamter to Leaf Biomass (d2blmax)

FATES provides three different options for calculating leaf biomass from dbh:

• Saldarriaga et al. (1998)

$$(blmax = p_1 * d^{p_2} * rho^{p_3})$$

• 2 parameter power function

$$(blmax = p_1/c2b * d^{p_2})$$

• 2 parameter power function for large trees

$$(blmax = p_1/c2b * min(d, dbhmax)^{p_2})$$

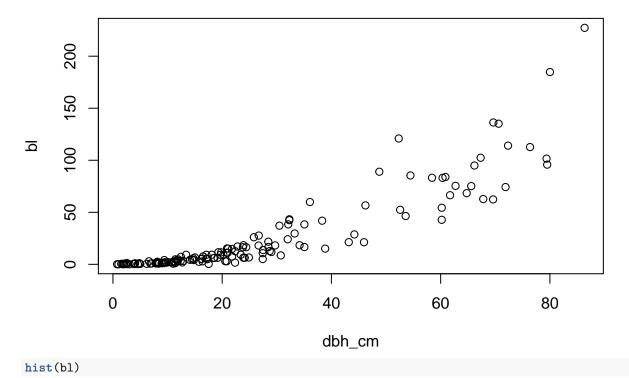
Here I will test the Saldarriaga and 2 parameter power functions.

```
bl <- pipo$m.lf

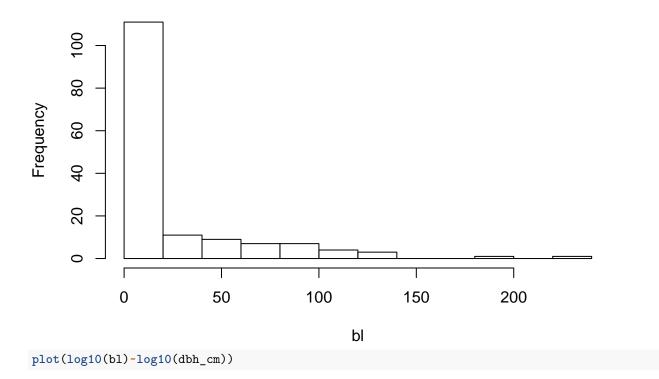
bl_test <-c(0.8, 4.6, 13.2, 30, 36.2, 60, 70.5, 93) # From Polly's sheets

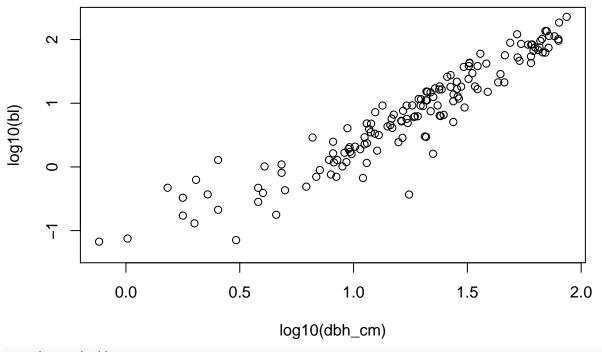
bl_dbh <- c(10, 20, 30, 40, 50, 60, 70, 80) #cm

plot(bl~dbh_cm)
```



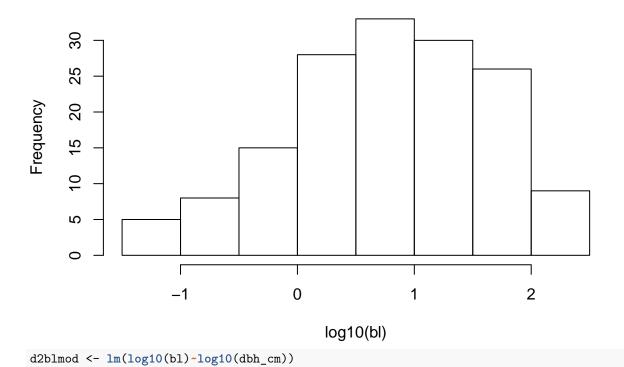
# Histogram of bl





hist(log10(bl))

# Histogram of log10(bl)



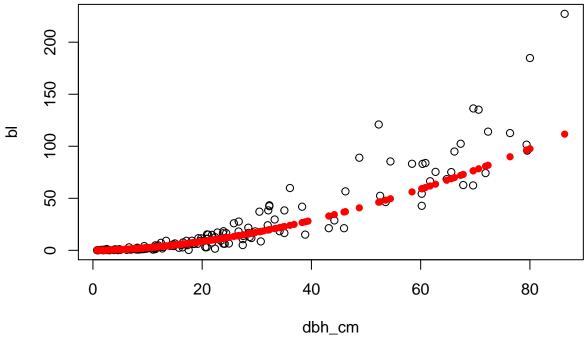
## (Intercept) log10(dbh\_cm) ## -1.363671 1.762904

coef(d2blmod)

```
plot(log10(bl)~log10(dbh_cm))
curve((-1.36 + 1.76*x),add=T, col="blue", lwd=2)
```

```
bl_lm <- function(dbh, p1, p2){
  blmax <- 10^((log10(dbh))* p1 + p2)
  return(blmax)
}
bl_lm_mod <- bl_lm(sort(dbh_cm), 1.76, -1.36)

plot(bl~dbh_cm)
points(bl_lm_mod~sort(dbh_cm), col="red", pch=16)</pre>
```



```
bl_sal <- function(p1,d,p2,rho,p3){</pre>
  blmax <- (p1 * (d^p2) * (rho^p3))
  return(blmax)
}
bl_2par <- function(p1,d,p2,c2b){</pre>
  blmax <- (p1 * (d^p2))/c2b
  return(blmax)
}
# Test difference params
\# Sal1: p1= 0.0169, p2= 2.592, p3= 2.251 (from Jupyter notebook curve_fit)
# Sal2: p1= 0.2, p2=1.55, p3=0.75 (from Polly)
# Sal3: p1=0.02, p2=2.011, p3=-0.01665 (from nls but setting p1=0.2)
# Sal4: p1= 0.115, p2= 1.834, p3= 1.33 (from nls below, p1=0.115, and using only mean bl for binned dbh
bl_sal1_mod <- bl_sal(0.0169, sort(dbh_cm), 2.592, rho, 2.251)
\#bl\_sal\_mod
bl_sal2_mod <- bl_sal(0.2, sort(dbh_cm), 1.55, rho, 0.75)
#bl_sal2_mod
bl_sal3_mod <- bl_sal(0.2, sort(dbh_cm), 2.011, rho, 2.28)
\#bl\_sal3\_mod
bl_sal4_mod <- bl_sal(0.115, bl_dbh, 1.834, rho, 1.33)
# 2 pwr1: p1=0.0035 , p2=2.592 (from jupyter notebook curve_fit)
# 2 pwr2: p1= 0.005, p2= 2
# 2 pwr3: p1=0.04, p2=2.01 (from r nls below using full bl and dbh data from BAAD)
# 2 pwr4: p1= 0.06, p2= 1.834 (from nls below using mean BL for binned dbh)
bl_2par_mod <- bl_2par(0.0035, sort(dbh_cm), 2.592, 2)
\#bl_2par_mod =
```

```
bl_2par2_mod <- bl_2par(0.001, sort(dbh_cm), 2.85, 2) # Brute force
#bl_2par2_mod
bl_2par3_mod <- bl_2par(0.041, sort(dbh_cm), 2.011, 2)
#bl_2par3_mod
bl_2par4_mod <- bl_2par(0.06, bl_dbh, 1.834, 2)
bl_2par5_mod <- bl_2par(0.06, sort(dbh_cm), 1.834, 2)
plot(bl~dbh_cm)
points(bl_sal1_mod~sort(dbh_cm), type="l", col="blue", lwd=2, lty=3)
points(bl_sal2_mod~sort(dbh_cm), type="1", col="darkgreen", lwd=2, lty=3)
points(bl_sal3_mod~sort(dbh_cm), type="1", col="green", lwd=2, lty=3)
points(bl_2par_mod~sort(dbh_cm), type="1", col="red", lwd=2, lty=3)
points(bl_2par2_mod~sort(dbh_cm), type="1", col="pink", lwd=2, lty=3)
points(bl_2par3_mod~sort(dbh_cm), type="1", col="orange", lwd=2, lty=3)
points(bl_2par5_mod~sort(dbh_cm), type="l", col="black", lwd=3)
                                                                                0
     200
     150
                                                     0
9
     100
     20
            0
                           20
                                           40
                                                           60
                                                                           80
                                           dbh cm
```

```
plot(bl_test~bl_dbh)
points(bl_sal4_mod~bl_dbh, type="l", col="blue", lwd=2, lty=3)
points(bl_2par4_mod~bl_dbh, type="l", col="orange", lwd=2, lty=3)
```

```
9
     4
            10
                     20
                               30
                                         40
                                                  50
                                                            60
                                                                     70
                                                                               80
                                           bl_dbh
bl_sal1_rmse <- rmse(bl_sal1_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_sal1_R2 <- r2(bl_sal1_mod, na.omit(bl))</pre>
## Warning in ((y_hat)) - (y): longer object length is not a multiple of
## shorter object length
bl_2par_rmse <- rmse(bl_2par_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_2par_R2 <- r2(bl_2par_mod, na.omit(bl))</pre>
## Warning in ((y_hat)) - (y): longer object length is not a multiple of
## shorter object length
bl_sal2_rmse <- rmse(bl_sal2_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_sal2_R2 <- r2(bl_sal2_mod, na.omit(bl))</pre>
## Warning in ((y_hat)) - (y): longer object length is not a multiple of
## shorter object length
bl_sal3_rmse <- rmse(bl_sal3_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_sal3_R2 \leftarrow r2(bl_sal3_mod, na.omit(bl))
```

## Warning in ((y\_hat)) - (y): longer object length is not a multiple of

```
## shorter object length
bl_sal4_rmse <- rmse(bl_sal4_mod, bl_dbh)</pre>
bl_sal4_R2 \leftarrow r2(bl_sal4_mod, bl_dbh)
bl_2par2_rmse <- rmse(bl_2par2_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_2par2_R2 <- r2(bl_2par2_mod, na.omit(bl))</pre>
## Warning in ((y_hat)) - (y): longer object length is not a multiple of
## shorter object length
bl_2par3_rmse <- rmse(bl_2par3_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_2par3_R2 <- r2(bl_2par3_mod, na.omit(bl))</pre>
## Warning in ((y_hat)) - (y): longer object length is not a multiple of
## shorter object length
bl_2par4_rmse <- rmse(bl_2par4_mod, bl_test)</pre>
bl_2par4_R2 <- r2(bl_2par4_mod, bl_test)</pre>
bl_2par5_rmse <- rmse(bl_2par5_mod, na.omit(bl))</pre>
## Warning in y - y_hat: longer object length is not a multiple of shorter
## object length
bl_2par5_R2 <- r2(bl_2par5_mod, na.omit(bl))
## Warning in ((y_hat)) - (y): longer object length is not a multiple of
## shorter object length
bl_rmse <- c(bl_sal1_rmse, bl_sal2_rmse, bl_sal3_rmse, bl_2par_rmse, bl_2par2_rmse, bl_2par3_rmse, bl_2
bl_r2 <- c(bl_sal1_R2, bl_sal2_R2, bl_sal3_R2, bl_2par_R2, bl_2par2_R2, bl_2par3_R2, bl_2par5_R2)
bl_names <- c("Sal test 1: BL", "Sal test 2: BL", "Sal test 3:BL", "Two Param Power: BL", "Two Param Pow
bl_mod_fits <- data.frame(bl_rmse, bl_r2, row.names = bl_names)</pre>
bl_mod_fits
##
                          bl_rmse
                                       bl_r2
## Sal test 1: BL
                          53.88777 -2.445608
                         46.79779 -1.598580
## Sal test 2: BL
## Sal test 3:BL
                         52.31379 -2.247265
## Two Param Power: BL 53.69626 -2.421160
## Two Param Power 2: BL 51.83128 -2.187640
## Two Param Power 3:BL 52.43524 -2.262360
## Two Param Power 5: BL 47.89558 -1.721926
bl2par.fit <- nls(bl_test ~ bl_2par(p1,bl_dbh, p2, 2), start=list(p1=0.0035, p2=2.5))
bl2par.fit
## Nonlinear regression model
## model: bl_test ~ bl_2par(p1, bl_dbh, p2, 2)
```

```
##
      data: parent.frame()
##
        р1
                p2
## 0.06039 1.83353
  residual sum-of-squares: 70.04
## Number of iterations to convergence: 20
## Achieved convergence tolerance: 6.307e-06
blsalda.fit <- nls(bl_test ~ bl_sal(0.12, bl_dbh, p2, 0.367, p3), start=list(p2=1,p3=0.5))
blsalda.fit
## Nonlinear regression model
    model: bl_test ~ bl_sal(0.12, bl_dbh, p2, 0.367, p3)
##
##
      data: parent.frame()
##
      р2
           рЗ
## 1.834 1.376
  residual sum-of-squares: 70.04
##
##
## Number of iterations to convergence: 6
## Achieved convergence tolerance: 6.26e-06
```

#### Diamter to Crown Area

FATES provides one option for calculating crown area from dbh. There are actually 3 modes to choose from, but they all reference the same equation.

• A 2 power crown area function

```
carea = spreadterm*dbh^{crownareatodbhexponent}
```

where

$$spreadterm = (spread * d2ca_{max}) + ((1 - spread) * d2ca_{min})$$

and

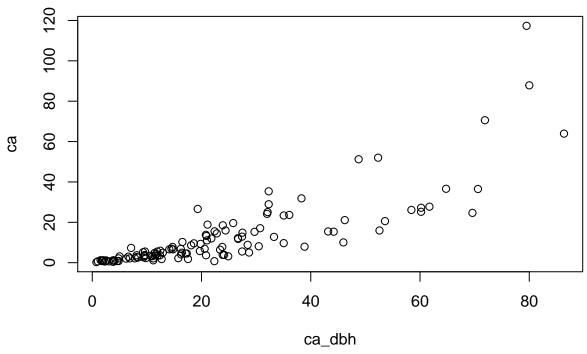
crown are at odbhex ponent = d2blp2 + d2ble diff

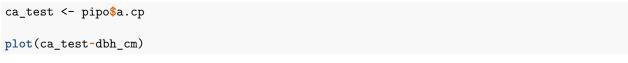
Combined all together:

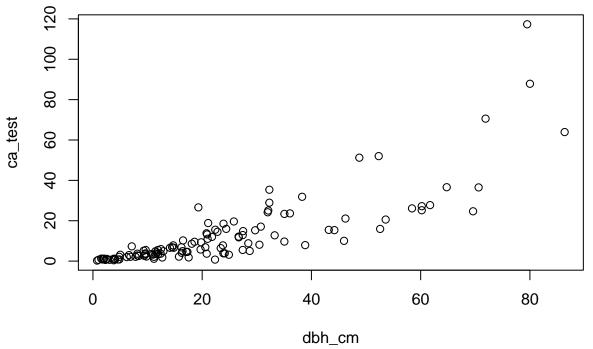
```
carea = (spread * d2ca_{max}) + ((1 - spread) * d2ca_{min}) * dbh^{(d2blp2 + d2blediff)}
```

We are given dbh, d2bl p2, d2bl ediff (0), and spread? We need to fit d2camax and min? Or we should know d2ca max and min and only need to fit for spread?

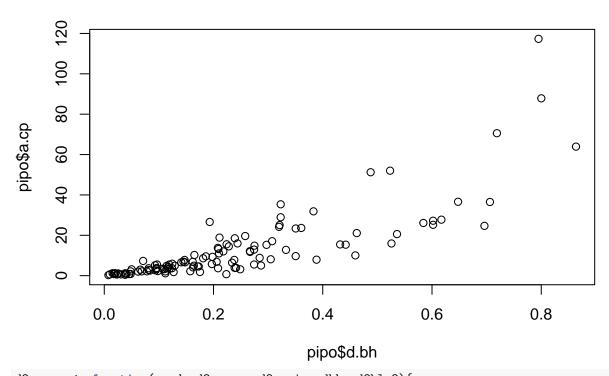
```
ca <- pipo$a.cp[which(pipo$a.cp>0, pipo$dbh>0)]
ca_dbh <- pipo$d.bh[which(pipo$a.cp > 0, pipo$d.bh>0)]*100
plot(ca~ca_dbh)
```







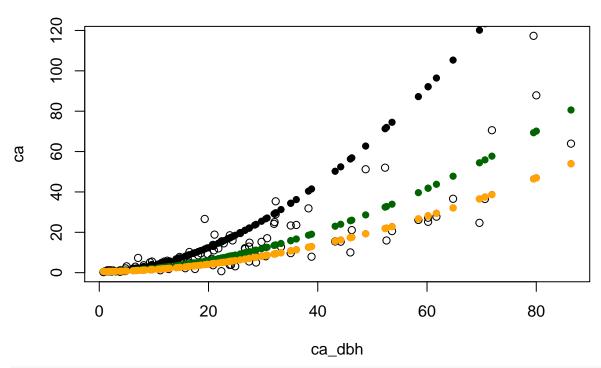
plot(pipo\$a.cp ~ pipo\$d.bh)



```
d2carea <- function(sprd, d2camax, d2camin, dbh, d2blp2){
    c.area <- ((sprd * d2camax) + ((1-sprd)*d2camin) * dbh^d2blp2)
    return(c.area)
}

ca_mod1 <- d2carea(0.5, 0.7, 0.1, ca_dbh, 1.834)
    ca_mod2 <- d2carea(0.85, 0.7, 0.1, ca_dbh, 1.834)
    ca_mod3 <- d2carea(0.85, 0.65, 0.15, ca_dbh, 1.834)
    ca_mod4 <- d2carea(0.85, 0.65, 0.1, ca_dbh, 1.834)

plot(ca~ca_dbh)
points(ca_mod1 ~ ca_dbh, pch=16, col="black")
points(ca_mod2 ~ ca_dbh, pch=16, col="red")
points(ca_mod3 ~ ca_dbh, pch=16, col="darkgreen")
points(ca_mod4 ~ ca_dbh, pch=16, col="orange")</pre>
```



```
# try to fit parameters  \#d2ca.fit \leftarrow nls(ca \sim d2carea(sprd,\ d2camax,\ 0.1,\ sort(dbh\_cm),\ 0.1834),\ start=list(sprd=0.4,\ d2camax=0.4,\ d2camax=0.4)
```

I want to try something where I step through spread values from 0.1 to 0.9 at intervals of 0.1 and calculate the d2camax.

In the mean time I need to figure out the issue with NAs so that I can calculate some  $\ r^2 \$  values.

```
#ca_mod1[is.na(ca_mod1)] <- min(ca)
#ca_mod2[is.na(ca_mod2)] <- min(ca)
#ca_mod3[is.na(ca_mod3)] <- min(ca)
#ca_mod4[is.na(ca_mod4)] <- min(ca)

ca_mod4[R2 <- r2(ca_mod4)] <- min(ca)

ca_mod2_R2 <- r2(ca_mod2[7:125], ca[7:125])

ca_mod3_R2 <- r2(ca_mod3[7:125], ca[7:125])

ca_mod4_R2 <- r2(ca_mod4[7:125], ca[7:125])

ca_mod4_R2 <- r2(ca_mod4[7:125], ca[7:125])

## [1] -1.191073

ca_mod2_R2

## [1] 0.5956255

ca_mod3_R2

## [1] 0.7179147

ca_mod4_R2
```

## [1] 0.5942858

### Diameter to sapwood carbon

FATES provides only one sapwood allometry model. The slope of the ratio of leaf area to stem area (la:sa) to diameter line is zero.

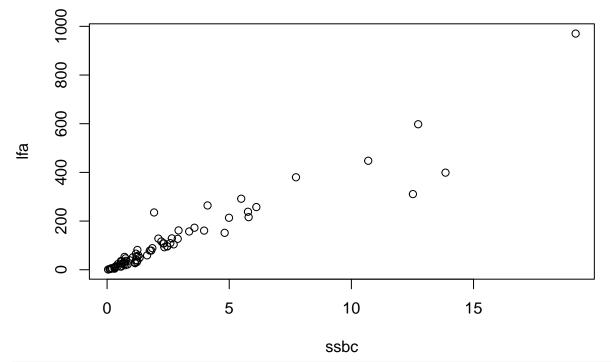
```
# Well I think one really only needs to determine the ratio of leaf area per sap area

# sapwood area

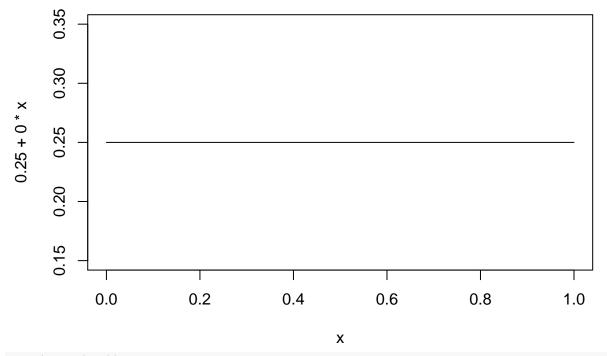
#ssba <- pipo$a.ssba
# ssbbh <= pipo$a.ssbh
ssbc <- pipo$a.ssbc *100 # sapwood area at base of crown

# leaf area

lfa <- pipo$a.lf
plot(lfa~ssbc)</pre>
```

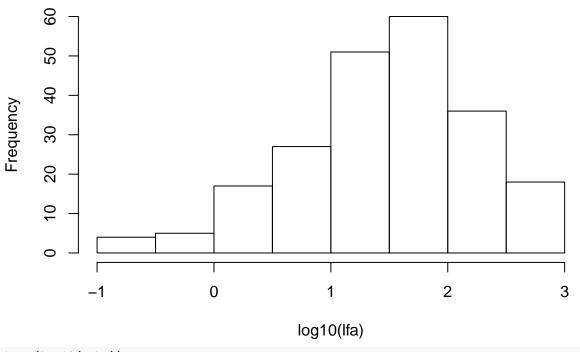


curve(0.25 + 0\*x)



hist(log10(lfa))

# Histogram of log10(lfa)



hist(log10(ssbc))

### Histogram of log10(ssbc)

```
Frequency
      15
      10
      2
      0
            -1.5
                         -1.0
                                      -0.5
                                                     0.0
                                                                  0.5
                                                                               1.0
                                                                                            1.5
                                               log10(ssbc)
```

```
# we know that the slope is set to O
# so we just need to find the intercept
sap_mod \leftarrow lm(log10(lfa) \sim log10(ssbc))
coef(sap_mod)
## (Intercept) log10(ssbc)
   1.584270
         1.097669
##
# Create a simple linear function to determine the intercept with a slope of O
sap_lin <- function(int, h, slope){</pre>
lapsa <- int + h * slope
return(lapsa)
sap_lin(-0.8, pipo$h.t, 0)
  ##
```

##