Congratulations! You passed!
TO PASS 75% or higher

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100%

Practice quiz on Bayes Theorem and the Binomial Theorem

TOTAL POINTS 9

1. A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers. **1 / 1 point**

The store does some research and learns that:

- **10% of the times that a jewelry store is robbed, a customer is in the store.**
- **A jewelry store has a customer on average 20% of each 24-hour day.**
- **The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.**

What is the probability that a robbery will occur while a customer is in the store?

- $\frac{1}{500000}$
- $\frac{1}{2000000}$
- ◉ $\frac{1}{4000000}$
- $\frac{1}{5000000}$

2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get exactly six heads? **1 / 1 point**

- 0.021
- 0.187
- ◉ 0.2051
- 0.305

Correct
By Binomial Theorem, equals

$$\binom{10}{6}(0.5^{10})$$

$$= \left(\frac{10!}{4! \times 6!}\right)\left(\frac{1}{1024}\right)$$
$$= 0.2051$$

3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting *exactly* 6 heads in 10 throws? **1 / 1 point**

- 0.0974
- 0.1045
- ◉ 0.1115

4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, what is the probability that I get at least 8 heads?

1 / 1 point

- 0.0312
- 0.0132
- 0.0213
- 0.0123

Correct

The answer is the sum of three binomial probabilities:

$$(\binom{10}{8} \times (0.4^8) \times (.6^2)) + (\binom{10}{9} \times (0.4^9) \times (0.6^1)) +$$

$$(\binom{10}{10}) \times (0.4^{10}) \times (0.6^0))$$

5. Suppose I have a bent coin with a 60% probability of coming up heads. I throw the coin ten times and it comes up heads 8 times.

1 / 1 point

What is the value of the "likelihood" term in Bayes' Theorem -- the conditional probability of the data given the parameter.

- 0.168835
- 0.122885
- 0.043945
- 0.120932

Correct

Bayesian "likelihood" --- the p(observed data | parameter) is

p(8 of 10 heads | coin has p = .6 of coming up heads)

$$\binom{10}{8} \times (0.6^8) \times (0.4^2) = 0.120932$$

6. We have the following information about a new medical test for diagnosing cancer.

1 / 1 point

Before any data are observed, we know that 5% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 90% of them get an accurate test result of "Negative" for cancer. The other 10% get a false test result of "Positive" for cancer.

What is the conditional probability that I have Cancer, if I get a "Positive" test result for Cancer?

****Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT.**

- 67.9%
- 32.1% probability that I have cancer
- 4.5%
- 9.5%

Correct

I still have a more than $\frac{2}{3}$ probability of not having cancer

Posterior probability:

7. We have the following information about a new medical test for diagnosing cancer. 1 / 1 point

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

- 88.2%
- 0.9%
- 99.1%
- $.80\%$

Correct

$$p(\text{cancer} \mid \text{negative test}) = \frac{p(\text{negative test} \mid \text{Cancer})\, p(\text{Cancer})}{}$$

8. An urn contains 50 marbles – 40 blue and 10 white. After 50 draws, exactly 40 blue and 10 white are observed. 1 / 1 point

You are not told whether the draw was done “with replacement” or “without replacement.”

What is the probability that the draw was done with replacement?

- 87.73%
- 13.98%
- 1
- 12.27%

Correct

p(40 blue and 10 white | draws without replacement) = 1 [this is the only possible outcome when 50 draws are made without replacement]

p(40 blue and 10 white | draws with replacement)

S = 40

N = 50

P = .8 [for draws with replacement] because 40 blue of 50 total means p(blue) = 40/50 = .8

9. According to Department of Customs Enforcement Research: 99% of people crossing into the United States are not smugglers. 1 / 1 point

The majority of all Smugglers at the border (65%) appear nervous and sweaty.

Only 8% of innocent people at the border appear nervous and sweaty.

If someone at the border appears nervous and sweaty, what is the probability that they are a Smuggler?

- 8.57%
- 92.42%
- 7.92%
- 7.58%

Correct

By Bayes’ Theorem, the answer is

$$\frac{(.65)(.01)}{((.65)(.01) + (.08)(.99))}$$