

Appendix E: Torsion calculations

	Maximum Torque [Nm]	Experienced Torque [Nm]	Maximum tangential force [N]	Experienced tangential force [N]	Experienced radial force [N]	Rotational speed [rad/s]
Gear 1 [12T]	3	0.941	450	148.228	53.95	14.537
Gear 2 [36T]	3.4	2.627	700	137.879	50.184	4.508
Gear 3 [24T]	3	2.627	300	206.819	75.276	4.508
Gear 4 [24T]	3	2.489	300	195.99	71.335	4.272
Gear 5 [12T]	3	2.489	450	391.98	142.669	4.272
Gear 6 [36T]	3.4	6.946	700	364	132.709	1.324
Gear 7 [24T]	1	6.946	580	546.923	199.064	1.324
Gear 8 [48T]	1.2	13.269	580	522.417	190.144	0.638
Gear 9 [48T]	1.2	12.922	580	508.74	185.166	0.621

Figure 1: Table from appendix C

The table above shows the summary torque calculated

Torsional shear stress

- We can state the *torsional shear stress formula* as:

$$\tau_{\max} = \frac{TC}{J}$$

$$J = \frac{\pi D^4}{32} \text{ (for solid bar)}$$

τ = applied Torque

C = radius of the cross section

J = Polar moment of inertia of the cross section

The above equation from "Mechanic of Materials" 11th edition, written by Russell C. Hibbeler will be used to determine shear strength

Shaft 1

Given yield strength of the shaft:

$$\sigma_{shaft_1} := 450 \text{ MPa}$$

Given maximum torque the shaft can withstand:

$$T_{max_shaft1} := 5 \text{ N}\cdot\text{m}$$

Radius of the cross section:

$$c_{shaft_1} := 1.59 \text{ mm}$$

Polar moment of inertia of a square shaft:

$$J_{shaft_1} := \frac{2 \cdot c_{shaft_1}^4}{6}$$

$$J_{shaft_1} = 2.13 \text{ mm}^4$$

Maximum shear stress the shaft can withstand:

$$\tau_{max_shaft1} := \frac{T_{max_shaft1} \cdot c_{shaft_1}}{J_{shaft_1}}$$

$$\tau_{max_shaft1} = 3.732 \text{ GPa}$$

The shear strength that the shaft will experience will be calculated using the torque it is experiencing from table 1

Shaft 1 experienced torque:

$$T_{shaft1_ex} := 0.941 \text{ N}\cdot\text{m}$$

Shaft 1 experienced shear stress:

$$\tau_{shaft1_ex} := \frac{T_{shaft1_ex} \cdot c_{shaft_1}}{J_{shaft_1}}$$

$$\tau_{shaft1_ex} = 702.295 \text{ MPa}$$

Shaft 2

Given yield strength of the shaft:

$$\sigma_{shaft_2} := 450 \text{ MPa}$$

Given maximum torque the shaft can withstand:

$$T_{max_shaft2} := 5 \text{ N}\cdot\text{m}$$

Radius of the cross section:

$$c_{shaft_2} := 1.59 \text{ mm}$$

Polar moment of inertia of a square shaft:

$$J_{shaft_2} := \frac{2 \cdot c_{shaft_2}^4}{6}$$

$$J_{shaft_2} = 2.13 \text{ mm}^4$$

Maximum shear stress the shaft can withstand:

$$\tau_{max_shaft2} := \frac{T_{max_shaft2} \cdot c_{shaft_2}}{J_{shaft_2}}$$

$$\tau_{max_shaft2} = 3.732 \text{ GPa}$$

The shear strength that the shaft will experience will be calculated using the torque it is experiencing from table 1

Shaft 2 experienced torque:

$$T_{shaft2_ex} := 2.627 \text{ N}\cdot\text{m}$$

Shaft 2 experienced shear stress:

$$\tau_{shaft2_ex} := \frac{T_{shaft2_ex} \cdot c_{shaft_2}}{J_{shaft_2}}$$

$$\tau_{shaft2_ex} = 1.961 \text{ GPa}$$

Shaft 3

Given yield strength of the shaft:

$$\sigma_{shaft_3} := 450 \text{ MPa}$$

Given maximum torque the shaft can withstand:

$$T_{max_shaft3} := 5 \text{ N}\cdot\text{m}$$

Radius of the cross section:

$$c_{shaft_3} := 1.59 \text{ mm}$$

Polar moment of inertia of a square shaft:

$$J_{shaft_3} := \frac{2 \cdot c_{shaft_3}^4}{6}$$

$$J_{shaft_3} = 2.13 \text{ mm}^4$$

Maximum shear stress the shaft can withstand:

$$\tau_{max_shaft3} := \frac{T_{max_shaft3} \cdot c_{shaft_3}}{J_{shaft_3}}$$

$$\tau_{max_shaft3} = 3.732 \text{ GPa}$$

The shear strength that the shaft will experience will be calculated using the torque it is experiencing from table 1

Shaft 3 experienced torque:

$$T_{shaft3_ex} := 2.489 \text{ N}\cdot\text{m}$$

Shaft 3 experienced shear stress:

$$\tau_{shaft3_ex} := \frac{T_{shaft3_ex} \cdot c_{shaft_3}}{J_{shaft_3}}$$

$$\tau_{shaft3_ex} = 1.858 \text{ GPa}$$

Shaft 4

Given yield strength of the shaft:

$$\sigma_{shaft_4} := 450 \text{ MPa}$$

Given maximum torque the shaft can withstand:

$$T_{max_shaft4} := 13 \text{ N}\cdot\text{m}$$

Radius of the cross section:

$$c_{shaft_4} := 1.59 \text{ mm}$$

Polar moment of inertia of a square shaft:

$$J_{shaft_4} := \frac{2 \cdot c_{shaft_2}^4}{6}$$

$$J_{shaft_4} = 2.13 \text{ mm}^4$$

Maximum shear stress the shaft can withstand:

$$\tau_{max_shaft4} := \frac{T_{max_shaft4} \cdot c_{shaft_4}}{J_{shaft_4}}$$

$$\tau_{max_shaft4} = 9.702 \text{ GPa}$$

The shear strength that the shaft will experience will be calculated using the torque it is experiencing from table 1

Shaft 3 experienced torque:

$$T_{shaft4_ex} := 6.946 \text{ N}\cdot\text{m}$$

Shaft 3 experienced shear stress:

$$\tau_{shaft4_ex} := \frac{T_{shaft4_ex} \cdot c_{shaft_4}}{J_{shaft_4}}$$

$$\tau_{shaft4_ex} = 5.184 \text{ GPa}$$

Shaft 5

Given yield strength of the shaft:

$$\sigma_{shaft_5} := 450 \text{ MPa}$$

Given maximum torque the shaft can withstand:

$$T_{max_shaft5} := 15 \text{ N}\cdot\text{m}$$

Radius of the cross section:

$$c_{shaft_5} := 1.59 \text{ mm}$$

Polar moment of inertia of a square shaft:

$$J_{shaft_5} := \frac{2 \cdot c_{shaft_5}^4}{6}$$

$$J_{shaft_5} = 2.13 \text{ mm}^4$$

Maximum shear stress the shaft can withstand:

$$\tau_{max_shaft5} := \frac{T_{max_shaft5} \cdot c_{shaft_5}}{J_{shaft_5}}$$

$$\tau_{max_shaft5} = 11.195 \text{ GPa}$$

The shear strength that the shaft will experience will be calculated using the torque it is experiencing from table 1

Shaft 3 experienced torque:

$$T_{shaft5_ex} := 13.269 \text{ N}\cdot\text{m}$$

Shaft 3 experienced shear stress:

$$\tau_{shaft5_ex} := \frac{T_{shaft5_ex} \cdot c_{shaft_5}}{J_{shaft_5}}$$

$$\tau_{shaft5_ex} = 9.903 \text{ GPa}$$

Shaft 6

Given yield strength of the shaft:

$$\sigma_{shaft_6} := 450 \text{ MPa}$$

Given maximum torque the shaft can withstand:

$$T_{max_shaft6} := 15 \text{ N}\cdot\text{m}$$

Radius of the cross section:

$$c_{shaft_6} := 1.59 \text{ mm}$$

Polar moment of inertia of a square shaft:

$$J_{shaft_6} := \frac{2 \cdot c_{shaft_6}^4}{6}$$

$$J_{shaft_6} = 2.13 \text{ mm}^4$$

Maximum shear stress the shaft can withstand:

$$\tau_{max_shaft6} := \frac{T_{max_shaft6} \cdot c_{shaft_6}}{J_{shaft_6}}$$

$$\tau_{max_shaft6} = 11.195 \text{ GPa}$$

The shear strength that the shaft will experience will be calculated using the torque it is experiencing from table 1

Shaft 3 experienced torque:

$$T_{shaft6_ex} := 12.922 \text{ N}\cdot\text{m}$$

Shaft 3 experienced shear stress:

$$\tau_{shaft6_ex} := \frac{T_{shaft6_ex} \cdot c_{shaft_6}}{J_{shaft_6}}$$

$$\tau_{shaft6_ex} = 9.644 \text{ GPa}$$