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# -*- coding: utf-8 -*-
Created on Sun Aug 31 04:16:05 2025
@author: ugims
 import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
 from mpl_toolkits.mplot3d import Axes3D # noga: F401
from scipy.interpolate import griddata
 import matplotlib.patches as patches
 # CONFIGURATION
 "file_path = r*C:/Users/ugims/inegi.up.pt/Teses & Est gios - Teses_Est gios - Miguel Ant nio Costa - Teses_Est gios - Miguel Ant nio Costa/3. Reposit rio do Migue
 # Target dimension of mould
MOLD_X = 900.0 # mm
MOLD_Z = 420.0 # mm
\# Adjust by zone (parameters are adjustable) K = 1.5 $\# thermic correction factor (gain) P\_MEN = 10 $\#$ \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} \mbox{$\#$} (minimum allowed) \mbox{$\#$} \mbox{$\#$}
    real center (mm) of 15 resistances
                                                                     " of drawing
 CENTROS = [
       ROS = [
29.60, 88.80, 148.00, 207.20, 266.40,
331.60, 390.80, 450.00, 509.20, 568.40,
633.60, 692.80, 752.00, 811.20, 870.40
 CENTROS = sorted(CENTROS)
 assert len(CENTROS) == 15
 assert 0 <= min(CENTROS) and max(CENTROS) <= 900
 # READ + CLEAN
 df = pd.read_csv(
       file path.
        skiprows=8,
       skip blank lines=True,
        engine='python',
encoding='windows-1252'
df.columns = [c.strip() for c in df.columns]
df = df.applymap(lambda x: x.strip() if isinstance(x, str) else x)
for col in df.columns:
    df[col] = pd.to_numeric(df[col], errors='coerce')
df.dropna(inplace=True)
 # RESCALING TO 900 x 420
 x_raw = df['X (mm)']
 z_raw = df['Z (mm)']
x_min_raw, x_max_raw = x_raw.min(), x_raw.max()
z_min_raw, z_max_raw = z_raw.min(), z_raw.max()
 if x_max_raw == x_min_raw:
    raise ValueError("X interval in file is Null; Rescaling is impossible.")
 if z max raw == z min raw:
       raise ValueError("Z interval in file is Null; Rescaling is impossible.")
df['X (mm)'] = (x_raw - x_min_raw) / (x_max_raw - x_min_raw) * MOLD_X
df['Z (mm)'] = (z_raw - z_min_raw) / (z_max_raw - z_min_raw) * MOLD_Z
x = df['X (mm)']
 z = df['Z (mm)']
T = df['Value (Celsius)']
 " # BASE GRAPHICS (3D and 2D interpolated)
 fig = plt.figure(figsize=(10, 8))
fig = plt.figure(figsize=(10, 8))
ax = fig.add_subplot(111, projection='3d')
sc = ax.scatter(x, z, T, c=T, cmap='plasma')
ax.set_xlabel('X (mm) - Comprimento (0 "900)')
ax.set_ylabel('Z (mm) - Largura (0 "420)')
ax.set_zlabel('Temperatura ( °C)')
ax.set_title('Distribui § o de Temperatura " 3D')
plt.colorbar(sc, ax=ax, pad=0.1, label='Temperatura ( °C)')
plt.tight_layout()
plt.show()
plt.show()
xi = np.linspace(x.min(), x.max(), 220)
zi = np.linspace(z.min(), z.max(), 220)
XI, ZI = np.meshgrid(xi, zi)
TI = griddata((x, z), T, (XI, ZI), method='cubic')
plt.figure(figsize=(10, 8))
cf = plt.contourf(XI, ZI, TI, levels=100, cmap='plasma')
plt.xlabel('X (mm) - Comprimento (0 "900)')
plt.ylabel('Z (mm) - Largura (0 "420)')
plt.title('Mapa 2D de Temperatura " Interpolado')
plt.colorbar(cf, label='Temperatura ( °C)')
plt.tight_layout()
plt.tight_layout()
 plt.show()
 # 15 REAL ZONES (limited by MEDIUM DOTS between CENTERS)
limites.append(0.5 * (CENTROS[i-1] + CENTROS[i]))
limites.append(MOLD_X)
 x_edges = np.array(limites, dtype=float) # 16 borders †' 15 zones
 def zona15_por_x(xp, edges):
       for i in range(len(edges) - 1):
    if edges[i] <= xp < edges[i + 1]:
        return i + 1</pre>
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if np.isclose(xp, edges[-1]):
 return len(edges) - 1

 $df['Zona_15'] = df['X (mm)'].apply(lambda v: zona15_por_x(v, x_edges))$

return np.nan

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# SUBDIVISION 15 - 4 (60 subzones) " aligned to 15 longitudinal real zones
ncols = len(x_edges) - 1 # 15
nrows = len(z_edges) - 1 # 4
def identificar_zona_15x4(xp, zp, xed, zed):
       # columm (X)
       i = None
       for ii in range(len(xed) - 1):
            if xed[ii] <= xp < xed[ii + 1]:</pre>
                  i = ii
break
      if i is None and np.isclose(xp, xed[-1]):
    i = len(xed) - 2 # incluir extremo superior
       # line (Z)
         = None
      for jj in range(len(zed) - 1):
    if zed[jj] <= zp < zed[jj + 1]:
        j = jj</pre>
                  break
      if j is None and np.isclose(zp, zed[-1]):
    j = len(zed) - 2
       if i is None or j is None:
      return np.nan
return j * (len(xed) - 1) + i + 1 # numeration by line
   atributing subzone 15 -4 to each dot
 df['Zona_15x4'] = df.apply(\textbf{lambda} \ r: identificar_zona_15x4(r['X \ (mm)'], \ r['Z \ (mm)'], \ x\_edges, \ z\_edges), \ axis=1) 
# statistics by subzone
stat_15x4 = df.groupby('Zona_15x4')['Value (Celsius)'].agg(['min', 'max', 'mean']).reset_index()
estat_15x4['Delta (max - min)'] = estat_15x4['max'] - estat_15x4['min']
estat_dict_15x4 = estat_15x4.set_index('Zona_15x4').to_dict(orient='index')
# GRAPHIC of 60 subzones
fig, ax = plt.subplots(figsize=(16, 9))
for i in range(ncols):  # 15 columns
    for j in range(nrows):  # 4 lines
            zona_id = j * ncols + i + 1
x_start = x_edges[i]
z_start = z_edges[j]
            largura = x_edges[i + 1] - x_edges[i]
altura = z_edges[j + 1] - z_edges[j]
             stats = estat_dict_15x4.get(zona_id)
             if stats:
                  media_temp = stats['mean']
delta_temp = stats['Delta (max - min)']
cor = plt.cm.plasma(
                        = pit.cm.piasma(
(media_temp - estat_15x4['mean'].min()) /
(estat_15x4['mean'].max() - estat_15x4['mean'].min() + le-12)
                  media_temp = np.nan
                  delta_temp = np.nan
cor = 'gray'
            ax.add patch(rect)
                  text(
x_start + largura / 2, z_start + altura / 2,
f"{media_temp:.1f} °C\nZona {zona_id}",
color='white', ha='center', va='center', fontsize=6.2, weight='bold',
bbox=dict(boxstyle='round,pad=0.28', facecolor='black', edgecolor='white', linewidth=0.8, alpha=0.6)
ax.set_xlim(0.0, MOLD_X)
ax.set_ylim(0.0, MOLD_Z)
ax.set_xlabel('X (mm) - Comprimento (0 "900)')
ax.set_ylabel('Z (mm) - Largura (0 "420)')
ax.set_title('Subdivis o 15 -4: Temperatura M @dia e "T por Subzona (60 zonas)')
sm = plt.cm.ScalarMappable(
      norm=plt.Normalize(vmin=estat 15x4['mean'].min(), vmax=estat 15x4['mean'].max())
plt.colorbar(sm, ax=ax).set_label('Temperatura M @dia ( °C)')
plt.grid(False)
plt.tight_layout()
plt.show()
# 3 MACRO ZONES (5+5+5)
def macro zona(z15):
      if 1 <= z15 <= 5:
            return 1
      if 6 <= z15 <= 10:
            return 2
11 <= z15 <= 15:
      if 11
            return 3
      return np.nan
df['Zona_Macro'] = df['Zona_15'].apply(macro_zona)
# Average temperature of macro zones (based on data)
medias_macro = df.groupby('Zona_Macro')['Value (Celsius)'].mean().reindex([1, 2, 3])
print("\nAverage temperature per macro zone (confirmed data):")
for zmac in [1, 2, 3]:
   val = float(medias_macro.loc[zmac]) if zmac in medias_macro.index and pd.notna(medias_macro.loc[zmac]) else np.nan
   print(f" Zona {zmac}: {val:.2f} °C")
def pedir_float(msg):
    while True:
            try:
                 return float(input(msg))
            except ValueError:
    print("Invalid Value. Insert a number.")
# (Re)Calculate macro-zone in case it doesn't exist
if 'Zona_Macro' not in df.columns:
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def macro_zona(z15):
             if 1 <= z15 <= 5:    return 1
if 6 <= z15 <= 10:    return 2
if 11 <= z15 <= 15:    return 3</pre>
              return np.nan
       df['Zona_Macro'] = df['Zona_15'].apply(macro_zona)
 # Average temperature per zone (SECURITY: write in missing data with average global)
medias_macro = df.groupby('Zona_Macro')['Value (Celsius)'].mean().reindex([1, 2, 3])
if medias_macro.isna().any():
       medias_macro = medias_macro.fillna(df['Value (Celsius)'].mean())
print("\nDefine a TARGET TEMPERATURE ( °C) for each zone:")
T_SET_1 = pedir_float(" Zona 1 (resist ncias 1 "5): ")
T_SET_2 = pedir_float(" Zona 2 (resist ncias 6 "10): ")
T_SET_3 = pedir_float(" Zona 3 (resist ncias 11 "15): ")
print("\nInsert an INICIAL POTENCY (W) for each zone:")
PZ1 = pedir_float("    Zona 1 (1 "5): ")
PZ2 = pedir_float("    Zona 2 (6 "10): ")
PZ3 = pedir_float("    Zona 3 (11 "15): ")
# Simple equation per zone: P_new = P_nold * (1 - K * (T_med - T_set)/T_set), with limits K = K # use K already defined on top of script P_min = P_min
P_MAX = P_MAX
T1 = float(medias_macro.loc[1])
T2 = float(medias_macro.loc[2])
T3 = float(medias_macro.loc[3]
def ajusta(P old, T med, T set):
       denom = max(T_set, le-6)
fator = 1 - K * ((T_med - T_set) / denom)
return float(np.clip(P_old * fator, P_MIN, P_MAX)), fator
PZ1_new, f1 = ajusta(PZ1, T1, T_SET_1)
PZ2_new, f2 = ajusta(PZ2, T2, T_SET_2)
PZ3_new, f3 = ajusta(PZ3, T3, T_SET_3)
print("\n== EQUIVALENT Potency per zone (unique for each zone resistance) ===")
print(f" Z1 (1 "5):    Tmed={T1:.2f} °C †' Tset={T_SET_1:.2f} °C | fator={f1:.3f} | P_old={P21:.1f} W †' P_new={P21_new:.1f} W")
print(f" Z2 (6 "10):    Tmed={T2:.2f} °C †' Tset={T_SET_2:.2f} °C | fator={f2:.3f} | P_old={P22:.1f} W †' P_new={P22_new:.1f} W")
print(f" Z3 (11 "15):    Tmed={T3:.2f} °C †' Tset={T_SET_3:.2f} °C | fator={f3:.3f} | P_old={P23:.1f} W †' P_new={P23_new:.1f} W")
 # Final vector to apply per
                                                resistance (uniformity within each zone)
pot_ajustada_15 = [PZ1_new]*5 + [PZ2_new]*5 + [PZ3_new]*5
pot_inicial_15 = [PZ1]*5 + [PZ2]*5 + [PZ3]*5
targets_vec = [T_SET_1]*5 + [T_SET_2]*5 + [T_SET_3]*5
 # GRAPHICS: PER ZONE (BEFORE vs AFTER) + errors vs target
ray, axr = pir.swiprotes(rigsree=(5.0, 5.2))
zonas = np.array([[7.2, 3])
pot_ini = np.array([PZ1, PZ2, PZ3])
pot_new = np.array([PZ1_new, PZ2_new, PZ3_new])
erros z = np.array([T1 - T_SET_1, T2 - T_SET_2, T3 - T_SET_3])
larg = 0.35
larg - 0.33 axl.bar(zonas - larg/2, pot_ini, width=larg, label='Pot ncia Inicial (W)', alpha=0.9) axl.bar(zonas + larg/2, pot_new, width=larg, label='Pot ncia Nova (W)', alpha=0.9)
 ax1 set xticks(zonas)
 ax1.set_xticklabels(['Z1 (1 "5)', 'Z2 (6 "10)', 'Z3 (11 "15)'])
ax1.set_xlabel('Zona')
ax1.set_ylabel('Pot ncia (W)')
ax1.set_title(f'Ajuste de Pot ncia por Zona (K={K})')
ax1.legend()
ax1.grid(True, axis='y', linestyle='--', alpha=0.5)
ax2 = ax1.twinx()
ax2.plot(zonas, erros_z, linestyle='-', marker='s', label='Erro vs alvo ( °C)') ax2.set_ylabel('Erro vs alvo ( °C)') ax2.tick_params(axis='y')
plt.tight_layout()
plt.show()
 # OVERLAY 2D: show 3 bands with new potency per zone
"plt.figure(figsize=(10, 8))
cont = plt.contourf(XI, ZI, TI, levels=100, cmap='plasma')
  Vertical lines of limits from 15 zones
 for e in x_edges:
      plt.axvline(e, linewidth=0.8, alpha=0.5, linestyle='--')
# Shade 3 bands (edges [0..5], [5..10], [10..15])
plt.axvspan(x_edges[0], x_edges[5], alpha=0.10, label=f"Z1: {PZ1_new:.0f} W (alvo {T_SET_1:.0f} °C)")
plt.axvspan(x_edges[5], x_edges[10], alpha=0.10, label=f"Z2: {PZ2_new:.0f} W (alvo {T_SET_2:.0f} °C)")
plt.axvspan(x_edges[10], x_edges[15], alpha=0.10, label=f"Z3: {PZ3_new:.0f} W (alvo {T_SET_3:.0f} °C)")
plt.xlabel('X (mm) - Comprimento (0 "900)')
plt.xlabel('X (mm) - Comprimento (0 "420)')
plt.ylabel('Z (mm) - Largura (0 "420)')
plt.title('Mapa 2D | Pot ncia equivalente por zona (ap s ajuste)')
plt.colorbar(cont, label='Temperatura ( °C)')
plt.legend(loc='lower center', ncol=3, frameon=False)
plt.tight layout()
 plt.show()
 # RESISTENCE GRAPHICS: 15 BANDS (uniform potency per zone)
 fig, ax = plt.subplots(figsize=(12, 5.8))
idx = np.arange(1, 16, dtype=int)
macro_labels = np.array(['Z1']*5 + ['Z2']*5 + ['Z3']*5)
bars = ax.bar(idx, pot_ajustada_15, alpha=0.95, label='Pot ncia Nova (W)')
ax.set_xlabel('Resist ncia | Zona | Posi § o X (mm)')
ax.set_ylabel('Pot ncia (W)')
ax.set_title('Pot ncia aplicada por resist ncia (uniforme dentro da zona)')
ax.set xticks(idx)
ax.set_xticklabels([f"R{i} | {macro_labels[i-1]}\n{CENTROS[i-1]:.1f} mm" for i in idx], rotation=0)
for k in range(0, 16):
    ax.axvline(k + 0.5, linestyle='--', alpha=0.35, linewidth=0.7)
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for b in bars:
    b.set_edgecolor('black'); b.set_linewidth(0.6)

y_max = max(pot_ajustada_15) if len(pot_ajustada_15) else 1
ax.set_ylim(0, y_max * 1.15)
ax.grid(True, axis='y', linestyle='--', alpha=0.5)
ax.legend()
plt.tight_layout()
plt.show()
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