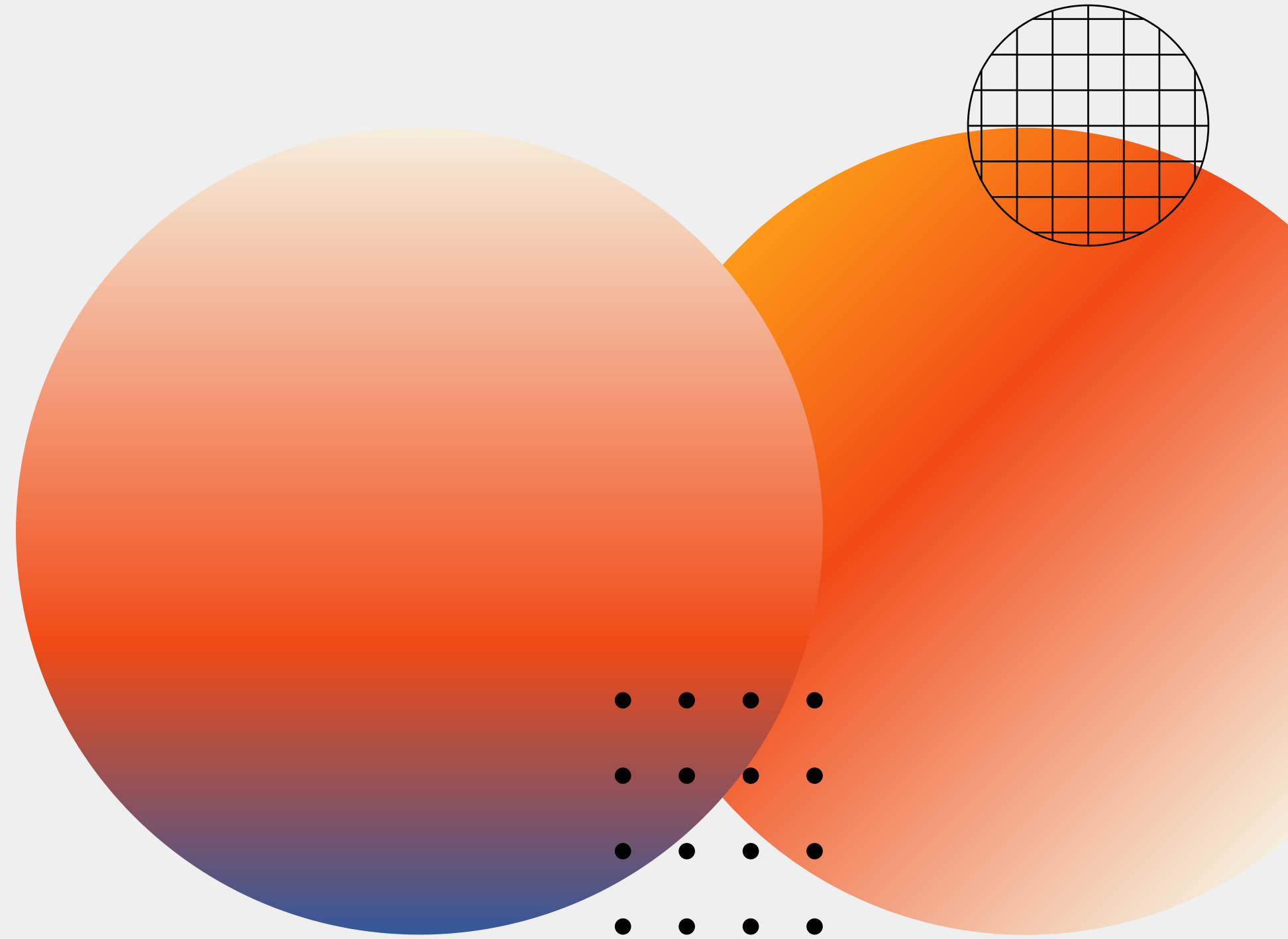


Let's Start

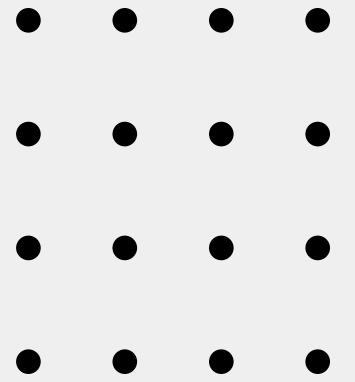
Multicollinearity and its impact on estimates of model parameters



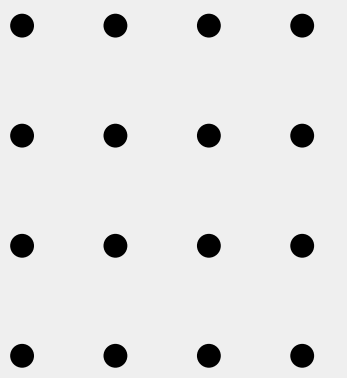
Pylypiva Oleksandra, Katrich Constantine, Koval Oleg



Multicollinearity



Multicollinearity is a phenomenon in which there is a dense linear relationship between two or more factor variables of the model or, in other words, factor variables have a high degree of correlation

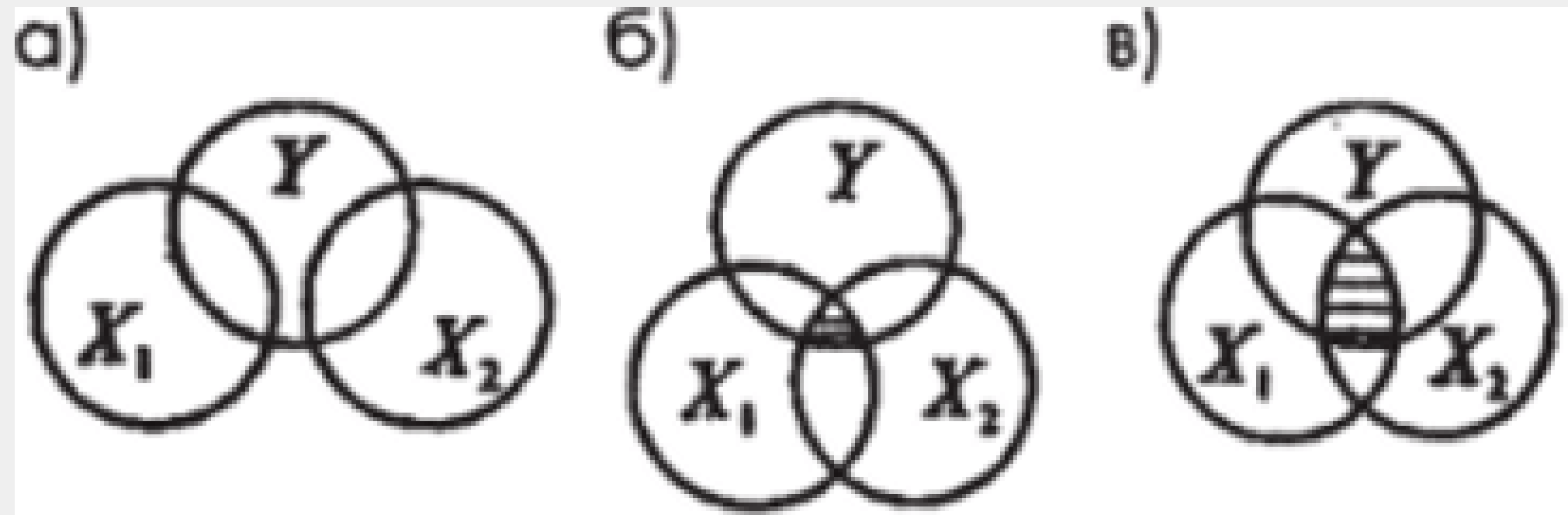


The term "multicollinearity" means that in a multivariate regression model, two or more independent variables, factors are interconnected by a linear relationship or, in other words, have a high degree of correlation.

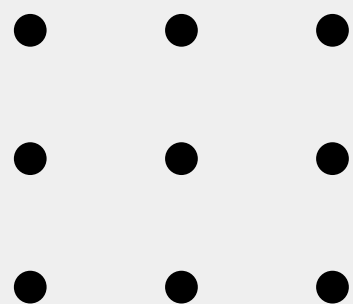
$$R = \begin{pmatrix} 1 & r_{12} & r_{13} & \dots & r_{1m} \\ r_{21} & 1 & r_{23} & \dots & r_{2m} \\ \dots & \dots & \dots & \dots & \dots \\ r_{m1} & r_{m2} & r_{m3} & \dots & 1 \end{pmatrix}$$



Graphically, this situation is presented in the form of a pie chart:

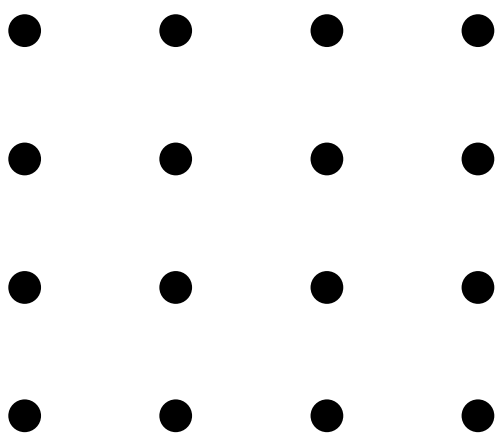


- **Subset 1** - describes the individual effect of factor x_1 .
- **Subset 2** - describes the individual effect of factor x_2 .
- **Subset 3** - the combined effect of both factors on the variable y , which can not be separated. Graphically describes the situation of collinearity.



The inevitability of multicollinearity

- Multicollinearity is a normal phenomenon.
- Almost any model contains multicollinearity.
- We do not pay attention to multicollinearity until the appearance of obvious symptoms.
- Only excessively strong connections get in the way.

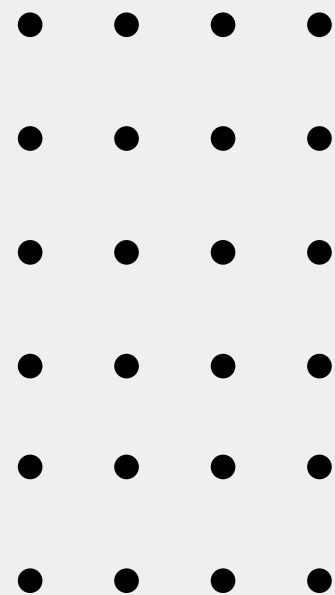




Methods for determining multicollinearity

The most complete study of multicollinearity is carried out according to the Farrar-Glober algorithm, which uses three types of statistical criteria and allows to detect multicollinearity:

- the whole array of independent variables (criterion 2)
- each independent variable with all others (F-criterion)
- each pair of independent variables (t-test)





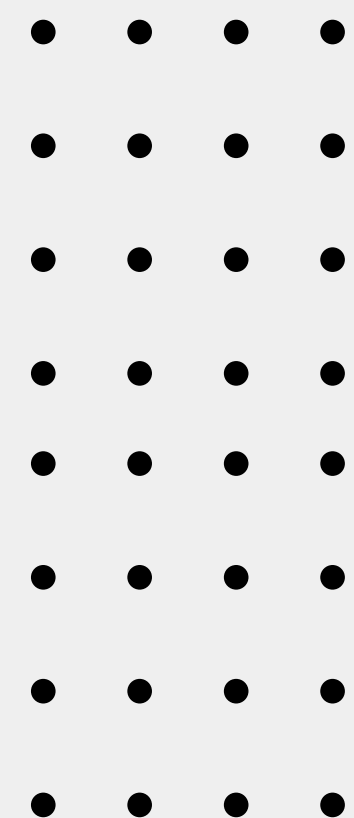
The Farrar-Glober algorithm

Seven steps

Step 1:

Normalize variables x_1, x_2, \dots, x_m of econometric model, calculating new (normalized) values of variables x_j

$$x_{ij} = \frac{x_{ij} - \bar{x}_j}{\sqrt{n\sigma_j}}$$

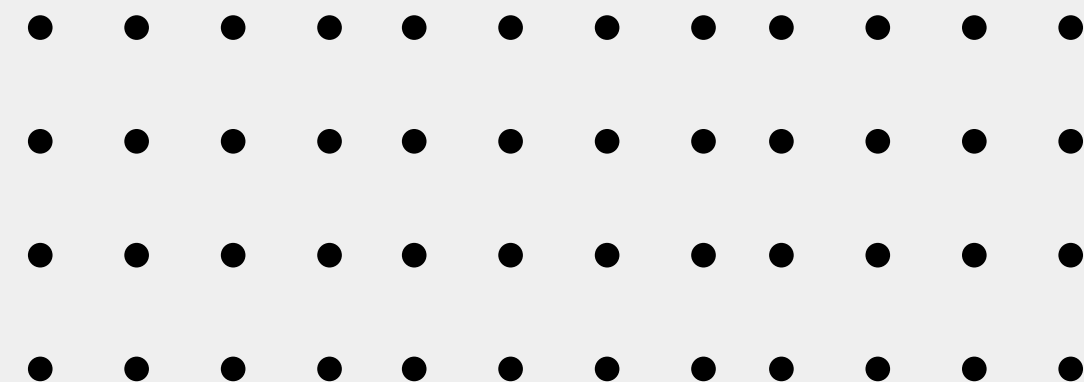


Step 2:



Based on the matrix X^* , the elements of which are normalized independent variables X_{ij}^* , calculate the correlation matrix (matrix of moments of the normalized system of normal equations):

$$R = X^{*T} X^* = \begin{pmatrix} 1 & r_{12} & \dots & r_{1m} \\ r_{21} & 1 & \dots & r_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ r_{m1} & r_{m2} & \dots & 1 \end{pmatrix}$$

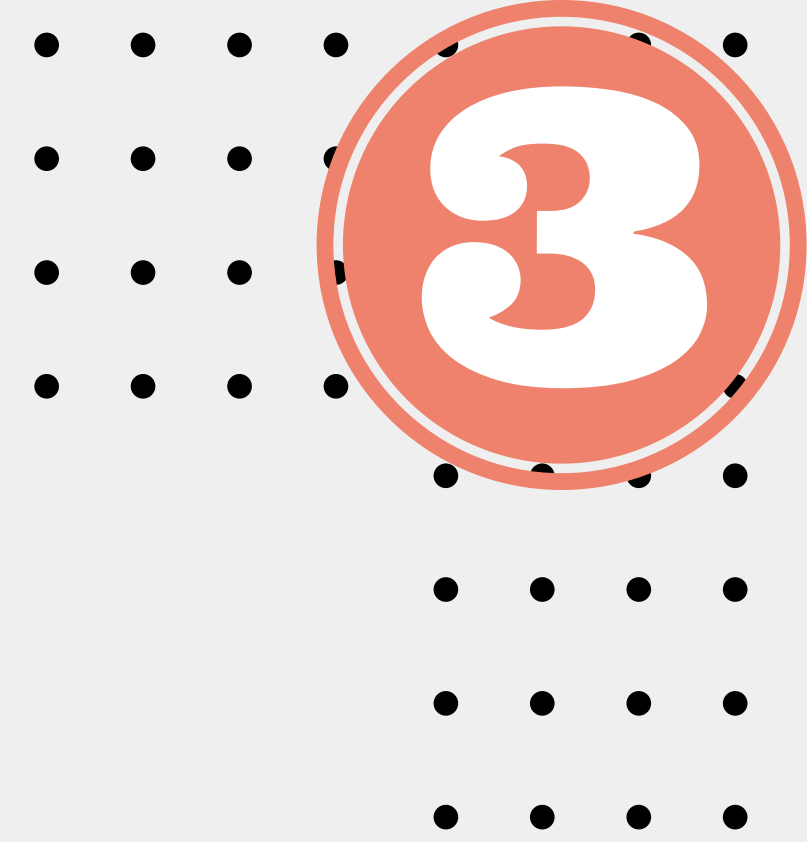


Step 3:

Determine $|R|$ - the determinant of the correlation matrix R ;
calculate the experimental value of criterion 2:

$$\chi^2_{exp} = -\left[n - 1 - \frac{1}{6}(2m + 5)\right] \ln |R|$$

Compare the value of χ^2 with the table at degrees $1 / 2m (m-1)$ of
freedom and the significance of α



Step 4:



Determine the matrix of errors:

$$C = R^{-1} = \begin{pmatrix} c_{11} & c_{12} & \dots & c_{1m} \\ c_{21} & c_{22} & \dots & c_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ r_{m1} & r_{m2} & \dots & c_{mm} \end{pmatrix}$$



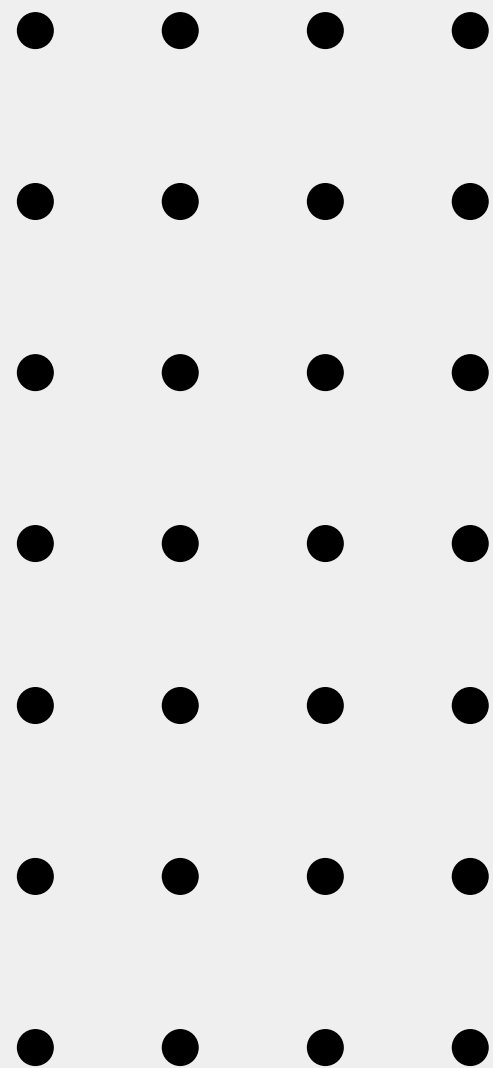
Step 5:

Calculate F-criteria:

$$F = \frac{(c_{kk} - 1)(n - m)}{m - 1}$$

Calculate the coefficients of determination for each variable:

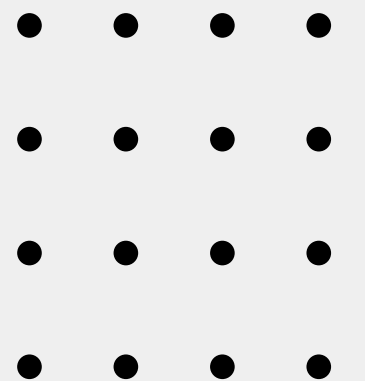
$$R_k^2 = 1 - \frac{1}{c_{kk}}$$



Step 6:

Find the partial correlation coefficients that characterize the density of the relationship between two variables, provided that other variables do not affect this relationship (the existence of paired multicollinearity):

$$r_{kj} = \frac{-c_{kj}}{\sqrt{c_{kk}c_{jj}}}$$



Step 7:

Calculate t-criteria:

$$t_{kj} = |r_{kj}| \frac{\sqrt{n-m}}{\sqrt{1-r_{kj}^2}}$$

The values of the t_{kj} criteria are compared with the tabular ones at $n-m$ degrees of freedom and significance levels α ; if $t_{kj} > t_{table}$, then there is multicollinearity between the independent variables x_k and x_i .



Conclusions of the method:

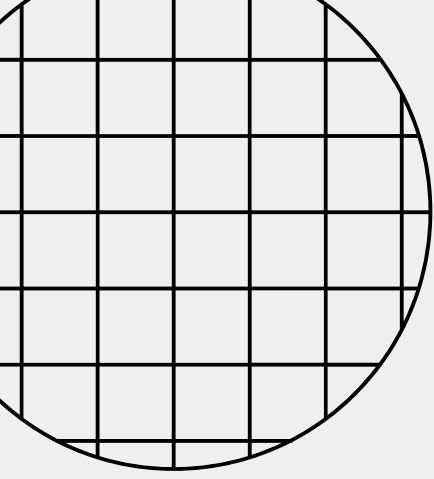
There may be a linear relationship between independent variables, but it may not be a phenomenon of multicollinearity

If $F_{\text{exp}} > F_{\text{table}}$, then x_k depends on all other independent variables and it is necessary to decide whether to exclude it from the list of variables

If $t_{kj} > t_{\text{table}}$, then x_k and x_i are closely related

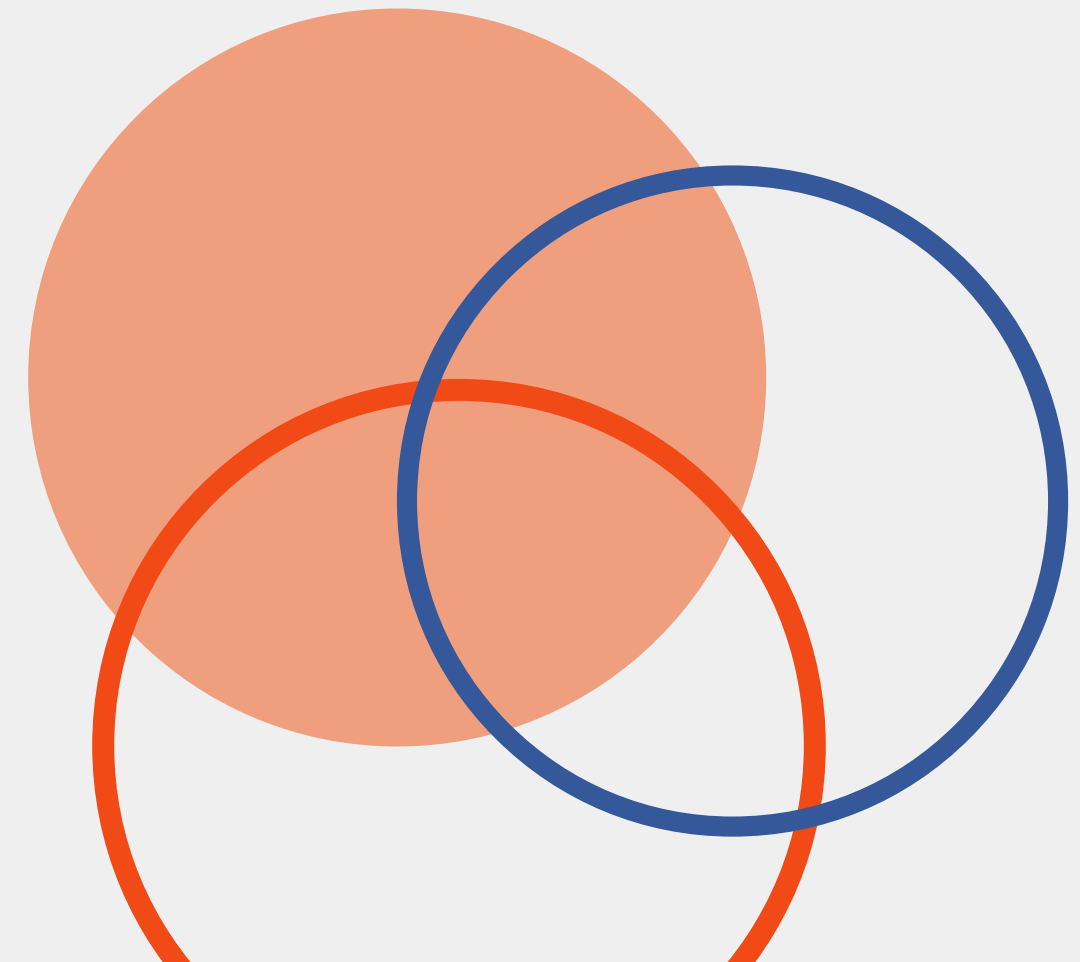
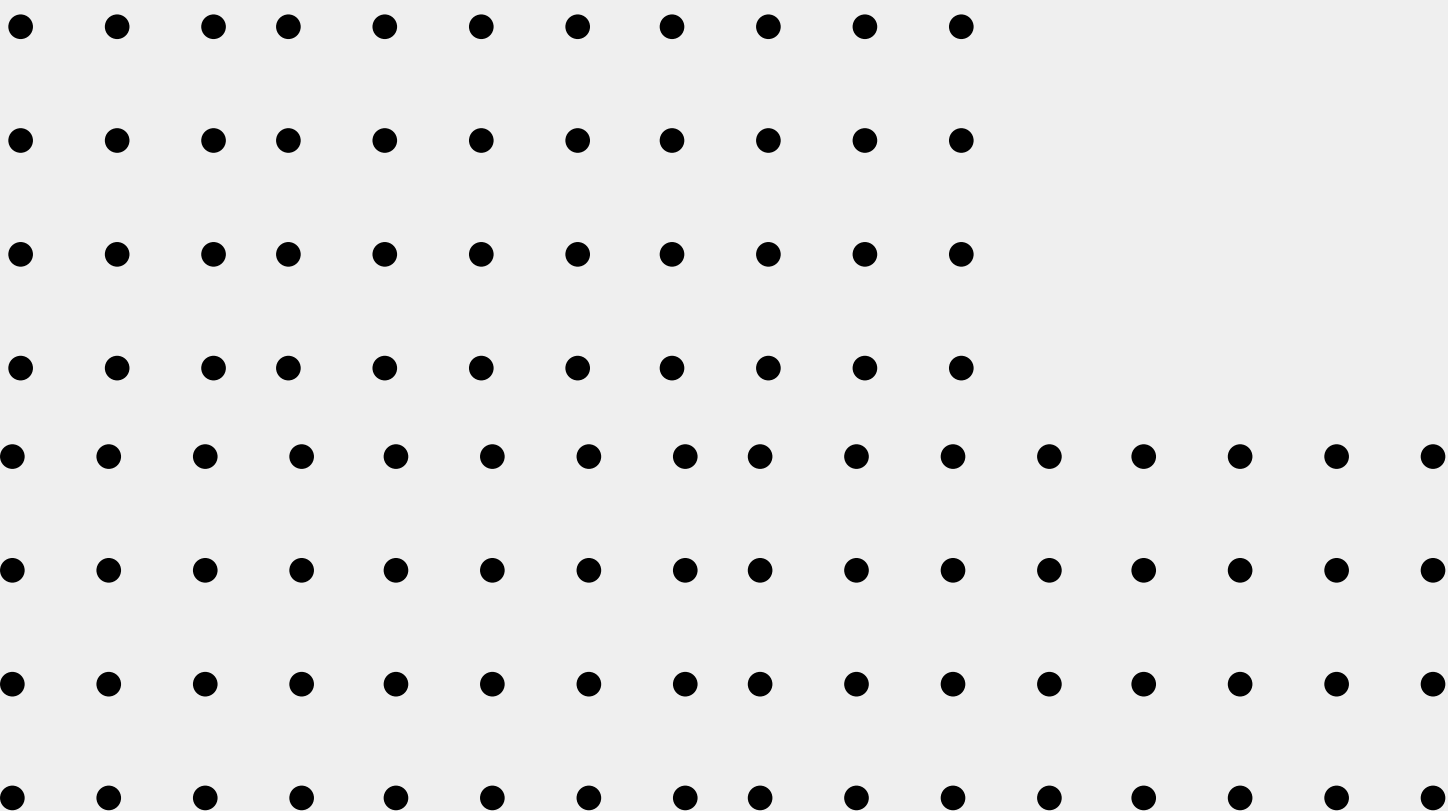
Analyzing the F- and t-criteria, we conclude which of the variables should be excluded from the model (of course, if possible for economic, logical and theoretical reasons)

If following paragraphs. 2-4, we did not achieve the goal, ie did not eliminate multicollinearity, the estimation of the model parameters should be calculated using another method



Conclusion

Multicollinearity and its impact on estimates of model parameters



End

Thank you

Do you have any questions?

