Derivate

Definitione
$$f(x)$$
 e derivabile in Xo se il limite $\lim_{h\to 0} \frac{f(x_0+h)-f(x_0)}{h}$ esiste ed e finito.

Rapporto incrementale
$$\frac{f(Xo+h)-f(Xo)}{h}$$

Coefficiente angolare di lim
$$h \to 0$$
 $\frac{f(x_0 + h) - f(x_0)}{h} = f'(x_0)$

Funzioni elementari

F(X)	f'(x)	F(X)	f'(x)
с	0	Tg x	4 200 <u>5 x</u>
x	4		602 >
χ ^α	or x _{or}	-1 cotgx	Zen _z x
ex	e x		2611-1
logx	¥	arcsenx	1 1-x2
senx	x 2Oo		N4-X-
x 203	- sen	x orccosx	- 4
$\sigma_{\mathbf{x}}$	a* Ir	10	N1-X-
	ı	arctgx	4+ 1/2
		агесотдх	- 1 1+ X²

Proprietà delle derivate

$$f(x) \setminus d(x) = \frac{f_1(x) \cdot d(x) - f(x) \cdot d_1(x)}{f(x)}$$

$$f(x) \cdot d(x) = f_1(x) \cdot d(x) + f(x) \quad d_1(x)$$

$$f(g(x)) - f_1(g(x)) \cdot d_1(x)$$

$$f(g(x)) - f_1(g(x)) \cdot d_1(x)$$

$$[G(x)]_{5}$$
 $(E_{-4}(x))_{,} = \frac{1}{4}$

$$f(x) \frac{\partial_{(x)}}{\partial_{(x)}} = e^{\frac{1}{2}(x) \cdot \log(x)} = f(x) \frac{\partial_{(x)}}{\partial_{(x)}} \left[\partial_{x}(x) \log f(x) + \partial_{x}(x) \cdot \frac{f(x)}{f(x)} \right]$$

Hopital

$$\lim_{x \to x_0} \frac{f(x)}{g(x)} \stackrel{F.I.}{=} \left[\frac{0}{0} \right] \circ \left[\frac{\infty}{\infty} \right]$$

$$\lim_{x \to x_0} \frac{f(x)}{g(x)} = \lim_{x \to x_0} \frac{f'(x)}{g'(x)} = \ell \in \mathbb{R}$$

Taylor

con centro in 0
$$Pn(x) = F(0) + F'(0)x + \frac{F''(0)}{2!}x^2 + \frac{F''''(0)}{3!}x^3 + ... + F^{(in)}(0)$$

Differenta fix) - Pnix) \longrightarrow fix) = Pnix) + Oixⁿ) per x \rightarrow 0

Sviluppi di Taylor

resto

$$e^{x} = 1 + x + \frac{1}{2}x^{2} + \frac{1}{3!}x^{3} + \frac{1}{4!}x^{4} + ... + \frac{1}{n!}x^{n} + O(x^{n})$$

$$\frac{360 \text{ X}}{3} = \text{ X} - \frac{1}{2!} \text{ X}^{5} + \frac{1}{4!} \text{ X}^{5} - \frac{1}{4!} \text{ X}^{2} + \dots + \frac{(2K+1)!}{(2K+1)!} \text{ X}^{2K+1} + \text{ O(} \text{ X}^{2K+1} \text{)}$$

$$COSX = 4 - \frac{1}{2}x^2 + \frac{1}{4!}x^4 - \frac{1}{6!}x^6 + ... + \frac{[-4]^K}{(2K)!}x^{2K} + O(x^{2K})$$

$$\frac{\log \left(\ 4+x \right)}{\pi} = x - \frac{1}{2} \, x^2 + \frac{1}{3} \, x^3 - \frac{1}{4} \, x^4 + ... + l - 1)^{n+1} \, \frac{x^n}{n} + O(x^n)$$

$$\frac{\text{Qretan(x)}}{3} = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^3}{7} + \dots + (-1)^K \cdot \frac{x^{2K+1}}{2K+1} + o(x^{2K+1})$$

$$|1+x|^{\frac{1}{2}} = |1+\alpha x| + \frac{\alpha(\alpha-1)}{2}x^{2} + \frac{\alpha(\alpha-1)(\alpha-2)}{3!}x^{3} + \dots + \frac{\alpha(\alpha-1)(\dots)(\alpha-n+1)}{n!}x^{n} + O(x^{n})$$

$$\frac{1}{4+x} = 4-x+x^2-x^3+...+(-1)^n x^n+0(x^n)$$

centro quaisiasi
$$\longrightarrow$$
 Pn(x-Xo) = f(Xo) + f'(Xo)(X-Xo) + $\frac{f''(Xo)}{2}$ [X-Xo)2 +... + $\frac{f^{(n)}(Xo)}{n!}$ [X-Xo)n