

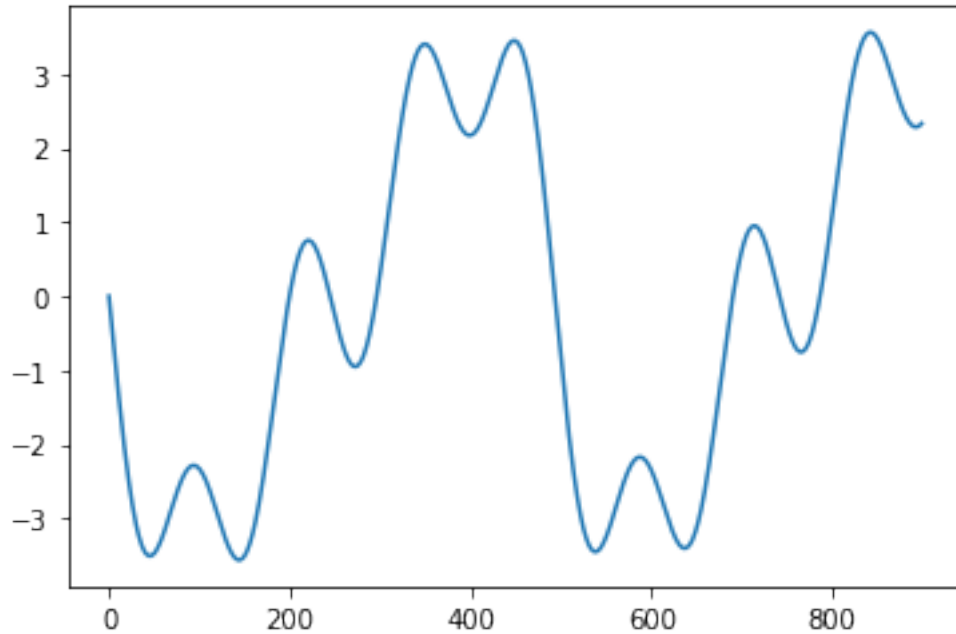
# AdditiveSynn

October 21, 2019

```
[15]: import numpy as np
import scipy as sp
import matplotlib.pyplot as plt
import pandas as pd
import random
```

## 0.1 i create a dummy signal

```
[16]: t=np.arange(10000)
omega=2*3.14*2
a=0.1*np.sin(omega*t)
a1=np.sin(omega*t)
b=3*np.sin(2*omega*t)
b1=np.sin(2*omega*t)
c=np.sin(4*omega*t)
d=5*np.sin(8*omega*t)
d1=np.sin(8*omega*t)
e=a+b+c+d/4
plt.plot(e[0:900])
z=np.random.uniform(-0.5,0.5,900).reshape(1,900)
```



```
[17]: m=e[0:900]+z
      m.reshape(1,-1)
```

```
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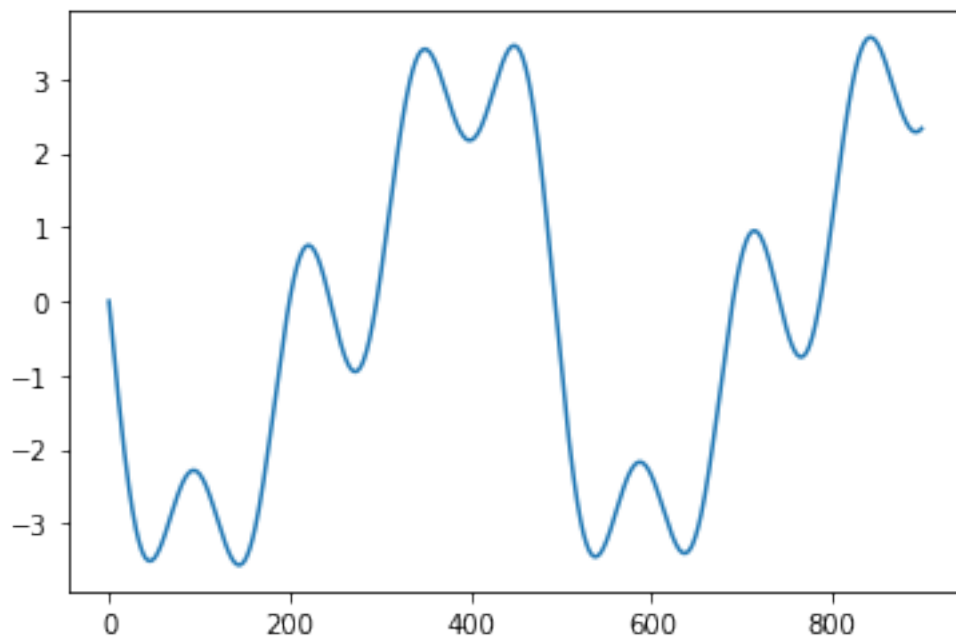
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```

```

[18]: plt.plot(e[0:900])
      plt.show()

```



```

[19]: kk=pd.DataFrame()

```

```

[20]: kk['a']=a1[0:900]
      kk['b']=b1[0:900]
      kk['c']=c[0:900]
      kk['d']=d1[0:900]

```

```
kk['sigint']=m[0:900].reshape(-1,1)
```

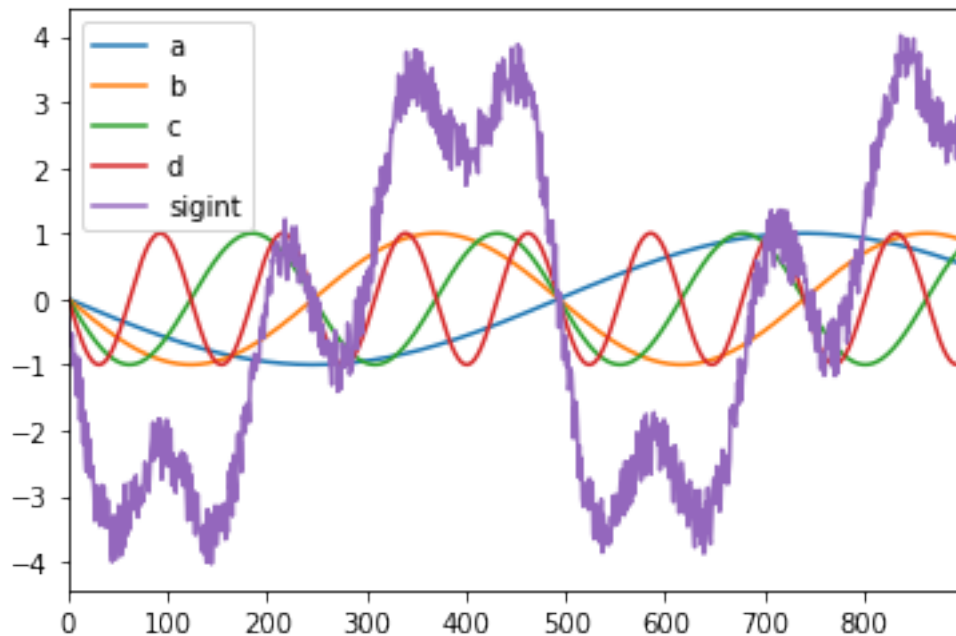
```
[21]: kk.head()
```

```
[21]:
```

	a	b	c	d	sigint
0	0.000000	0.000000	0.000000	0.000000	-0.289972
1	-0.006371	-0.012741	-0.025480	-0.050943	-0.577846
2	-0.012741	-0.025480	-0.050943	-0.101753	-0.658654
3	-0.019111	-0.038214	-0.076373	-0.152300	-0.714567
4	-0.025480	-0.050943	-0.101753	-0.202451	-0.531117

```
[22]: kk.plot()
```

```
[22]: <matplotlib.axes._subplots.AxesSubplot at 0x22736e38988>
```



```
[26]: from sklearn.linear_model import LinearRegression
X=kk[["a","b","c","d"]]
y=kk[["sigint"]]
X.head()
y.head()
reg = LinearRegression().fit(X, y)
reg.score(X,y)
```

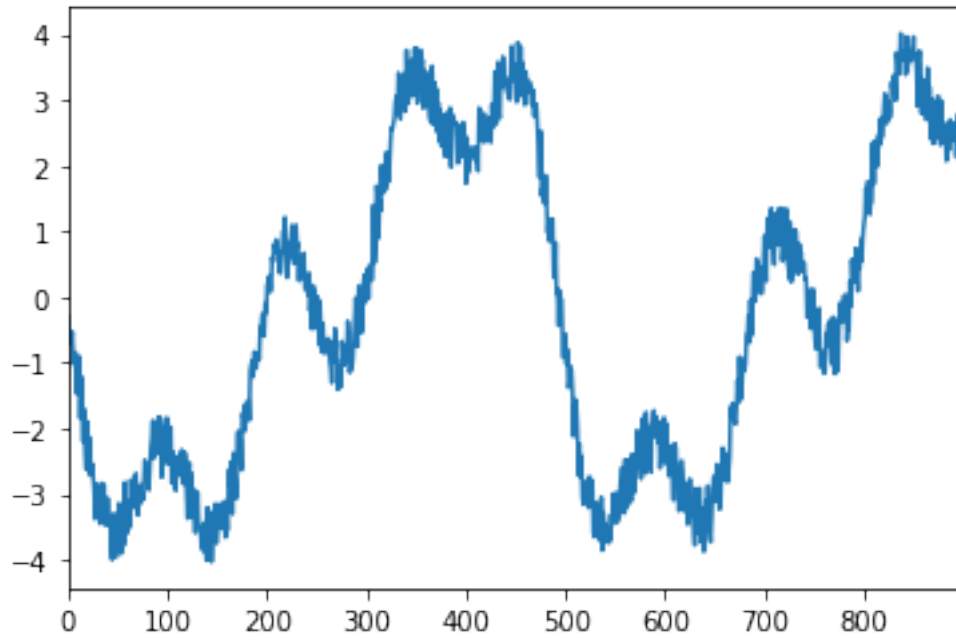
```
[26]: 0.9852518521904758
```

```
[27]: pred=reg.predict(X)
```

```
[28]: kk["Predicted"]=pred
```

```
[29]: kk["sigint"].plot()
```

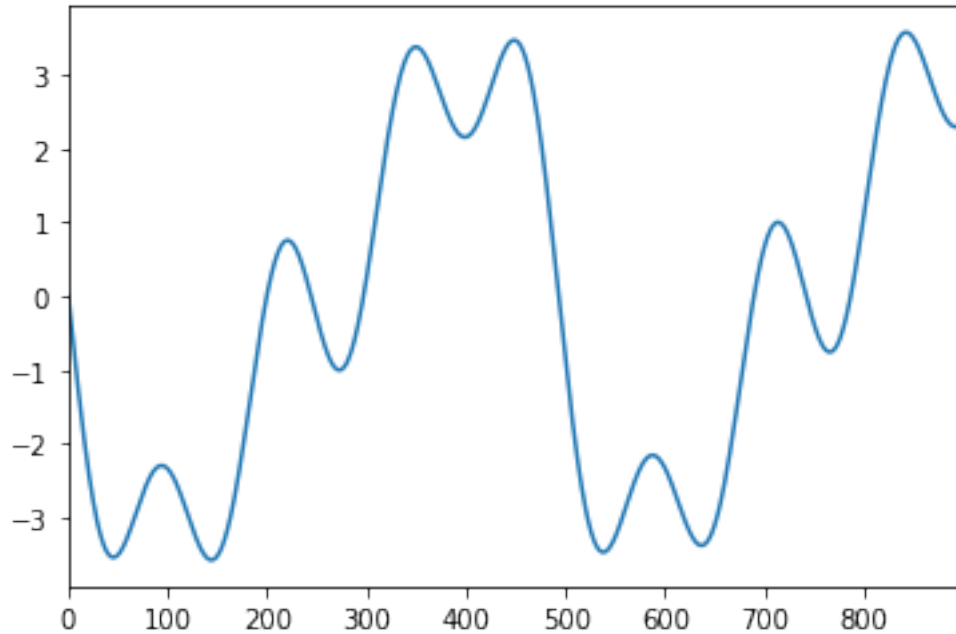
```
[29]: <matplotlib.axes._subplots.AxesSubplot at 0x22736ef7c48>
```



```
[30]: kk["Predicted"].plot()
```

```
[30]: <matplotlib.axes._subplots.AxesSubplot at 0x22736f38d88>
```





```
[31]: reg.coef_
```

```
[31]: array([[0.12412582, 2.99521059, 1.02202689, 1.26271616]])
```

*What i am trying to do is create a general formula for a sound signal of an instrument for its one note by using collection of sin wave harmonics* What i have done: \* created a signal using different amplitudes for sinwaves whose frequencies increase in by 2 every time \* i have used  $f$   $2f$   $4f$  and  $8f$  sinwaves with varying amplitude to generate a wave. I add them and divide resultant vector by 4 \* Then i add noise to the resultant wave \* so this somehow represents how a real world arbitrary sound wave would look

- now i take a table with vectors of each frequency of sinwave
- i append the input wave to this
- Apply least squares linear regression to this to calculate the weights

Observations till now :

- we get a good waveform which is similar to the input waveform

**0.2 Most Important Observation here is that the we obtain a general formula for the input noisy wave and can now generate a wave which is perfect with no noise**

```
[ ]:
```