

Computer Science & IT

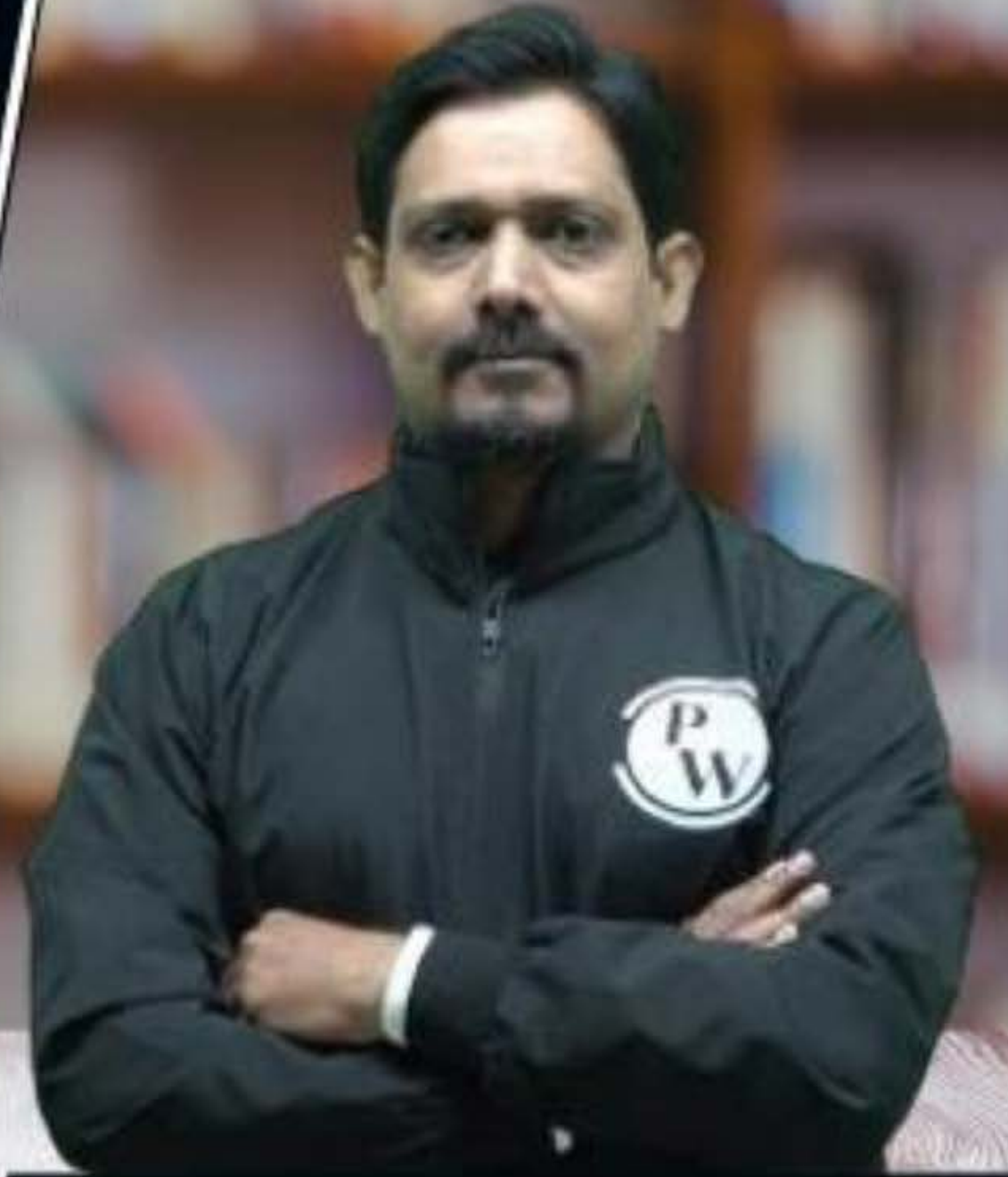
Data Structure & Programming



Queue

Lecture No. 01

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Recap of Previous Lecture



Topic

Expression

Topic

Evaluation of postfix prefix

Topic

Topic

Topic

Topics to be Covered



Topic

Queue

Topic

Linear queue

Topic

Topic

Topic



Topic : Question

#Q.

Compute the post fix equivalent of the following
expression $3 \times \log (x + 1) - a / 2$



Topic : Question



A function f defined on stacks of integers satisfies the following properties. $f(\phi) = 0$ and $f(\text{push}(S, i)) = \max(f(S), 0) + i$ for all stacks S and integers i . If a stack S contains the integers 2, -3, 2, -1, 2 in order from bottom to top, what is $f(S)$?

(A) 6

(B) 4

(C) 3

(D) 2

$$f(\emptyset) = 0, \quad f(\text{push}(S, i)) = \max(f(S), 0) + i$$

$$f\left(\begin{array}{|c|c|c|c|c|} \hline 2 & -3 & 2 & -1 & 2 \\ \hline \end{array}\right) = 3$$

S

$$f\left(\begin{array}{|c|c|c|c|} \hline 2 & -3 & 2 & -1 \\ \hline \end{array}, 2\right) = \max\left(f\left(\begin{array}{|c|c|c|} \hline 2 & -3 & 2 \\ \hline \end{array}, 0\right) + 2\right)$$

$$f(\text{push}(\begin{array}{|c|c|c|} \hline 2 & -3 & 2 \\ \hline \end{array}, -1)) = \max(f(\begin{array}{|c|c|c|} \hline 2 & -3 & 2 \\ \hline \end{array}, 0) - 1)$$

$$f(\text{push}(\begin{array}{|c|c|} \hline 2 & -3 \\ \hline \end{array}, 2)) = \max(f(\begin{array}{|c|c|} \hline 2 & -3 \\ \hline \end{array}, 0) + 2)$$

$$f(\text{push}(2, -3)) = \max(f(2), 0) - 3$$

$$f(\text{push}(\square, 2)) = \max(f(\square), 0) + 2$$



Topic : Question

A function f defined on stacks of integers satisfies the following properties. $f(\phi) = 0$ and $f(\text{push}(S, i)) = \max(f(S), 0) + 1$ for all stacks S and integers i . If a stack S contains the integers 2, -3, 2, -1, 2 in order from bottom to top, what is $f(S)$?

(A) 6

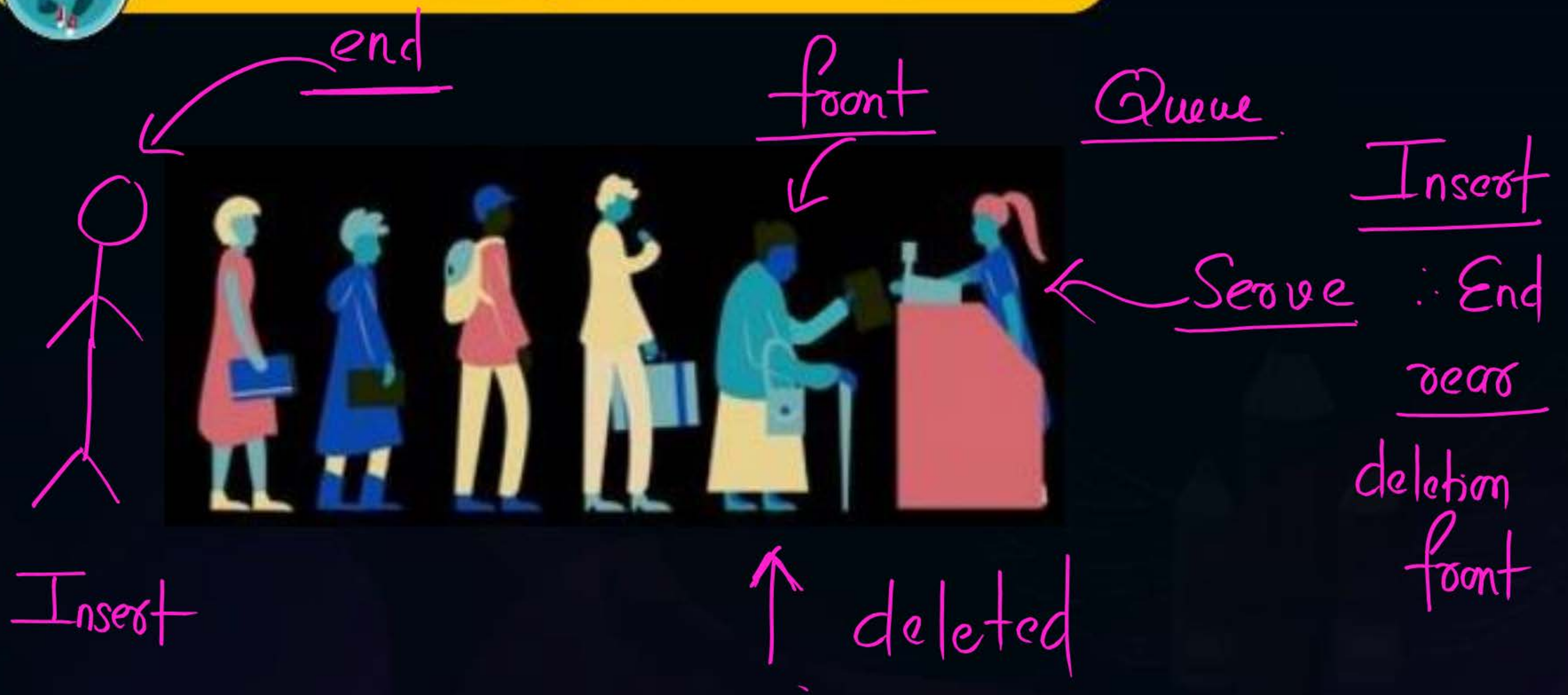
(B) 4

(C) 3

(D) 2



Queue





Topic : Queue



1. Queue is a Linear Data structure
2. Queue is 2 ended data structure
front (Deletion) rear (Insertion)
3. Queue is based on Logical property 'first in first out'



Topic : Queue



4. Insert operation Enqueue & Deletion operation is called dequeue

5.



Topic : Queue



global variable
define Max 100
int a[Max];
int front;
int rear;

void init()

Initialize value of front 2

rear:

rear = -1
front = -1



Topic : Queue



global variable
define Max 100
int a[Max];
int front;
int rear;

int IsEmpty()

it return 1 if queue is
Empty.

Empty condition is $\text{front} = -1$
if $\text{front} = -1$ then queue is Empty



Topic : Queue



```
void init() {  
    front = rear = -1  
}
```

```
int IsEmpty() {  
    if (front == -1)  
        return 1;  
    else  
        return 0;  
}
```




Topic : Queue



Enqueue : 1. if queue is full then return

2. Increment the rear

3. Insert the value

4. if first Insertion then Increment the front also.



Topic : Queue



```
void Enqueue( int data) {  
    if( rear == Max-1) {  
        printf( "queue is full");  
        return;  
    }  
    rear = rear + 1;  
    a[rear] = data;  
    if( front == -1)  
        front = 0;  
}
```

if(IsEmpty())



Topic : Queue



- Dequeue :
1. if queue is Empty then return (underflow)
 2. delete the element from queue (frontIndex)
 3. if front == rear then front & rear initialized to -1,
 4. else Increment the front
 5. return the value



Topic : Queue



```
int Dequeue() {  
    int data;  
    if (IsEmpty()) {  
        printf("queue is empty");  
        return -1;  
    }  
    data = a[front];  
    if (front == rear)  
        front = rear = -1;  
    else  
        front = front + 1;  
    return data;  
}
```




Queue

First Insertion
front Incremented to 0

~~front = -1, rear = -1~~

rear = 0

front = 0

1

0

1

2

3

4

0

1

2

3

4

front = 0, rear = 0
Enqueue(1)

front = 0
rear = 1

1

1

2

0

1

2

3

4

0

1

2

3

4

Enqueue(2)



Queue

front = 0, rear = 1

front = 0
rear = 2

1	2			
0	1	2	3	4

1	2	3		
0	1	2	3	4

front = 0 Enqueue(3)
rear = 2

front = 0
rear = 3

1	2	3		
0	1	2	3	4

1	2	3	4	
0	1	2	3	4

Enqueue(4)



Queue

front = 0, rear = 3

front = 0
rear = 4

1	2	3	4	
---	---	---	---	--

1	2	3	4	5
---	---	---	---	---

0 1 2 3 4

0 1 2 3 4

front = 0
rear = 4
Enqueue (5)

front = 0
rear = 4 ← (Max - 1)

1	2	3	4	5
---	---	---	---	---

1	2	3	4	5
---	---	---	---	---

0 1 2 3 4

0 1 2 3 4

Enqueue (6)

overflow



Queue



front = -1, rear = -1

queue is Empty

--	--	--	--	--

0

1

2

3

4

--	--	--	--	--

0

1

2

3

4

Dequeue()
front = 0, rear = 4

front = 1
rear = 4

underflow

1	2	3	4	5
---	---	---	---	---

0

1

2

3

4

1	2	3	4	5
--------------	---	---	---	---

0

1

2

3

4

Dequeue()

first Delete then Increment



Queue

-front(1), rear=4

overflow rear = Max-1

	2	3	4	5
--	---	---	---	---

0 1 2 3 4

Enqueue(6) ✓

-front=1, rear=4

-front=2
rear=4

	2	3	4	5
--	---	---	---	---

0 1 2 3 4

	2	3	4	5
--	--------------	---	---	---

0 1 2 3 4

Dequeue()



Queue

front = 2, rear = 4

		3	4	5
0	1	2	3	4

front = 3
rear = 4

Dequeue

			4	5
0	1	2	3	4

Dequeue()

front = 3
rear = 4

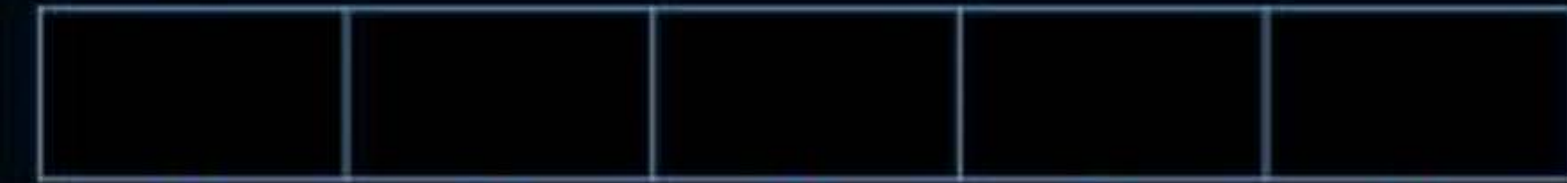
		3	4	5
0	1	2	3	4

front = 4
rear = 4

			4	5
0	1	2	3	4

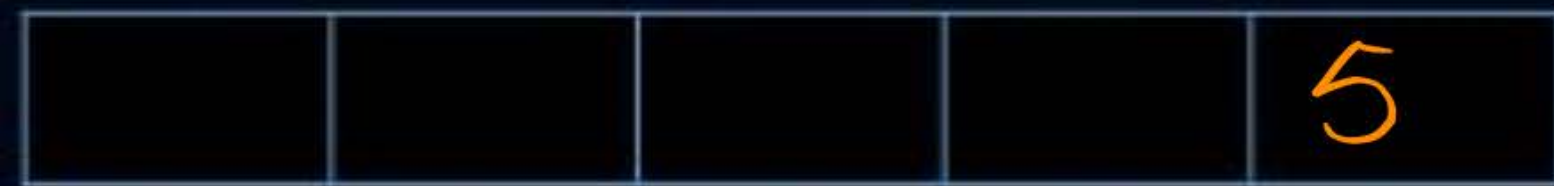


Queue



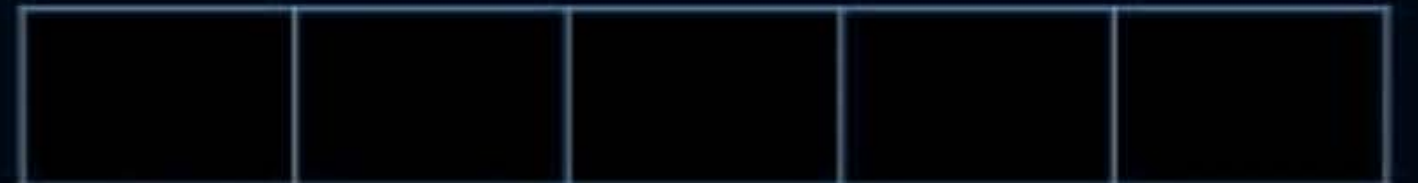
0 1 2 3 4

front = 4
rear = 4



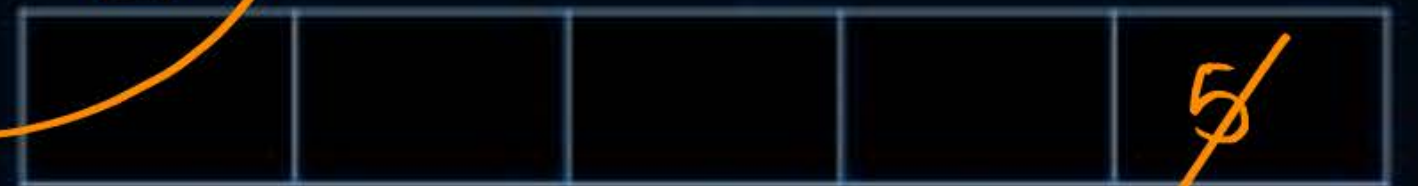
0 1 2 3 4

Dequeue ()



0 1 2 3 4

front = -1
rear = -1



0 1 2 3 4

after deletion before Incrementing
if front & rear points to same Index
both initialized to -1

of operations are performed

(15), Enqueue(60) $x = \text{dequeue}()$, $y = \text{dequeue}$

Enqueue(2), Enqueue(3), $z = \text{dequeue}$

value of $x + 2y - z$ is _____

$$15^2 = \underline{225}$$

60

2

$$225 + 120 - 2$$

$$345 - 2 = \underline{343}$$

60
15

3
2

z



Topic: GATE 2021 Set-I, 1-Mark

Consider the following sequence of operations on an empty stack.

push (54); push (52); pop (); push (55); push (62); s = pop ();

62
52 55
54

$x = \text{pop}()$

$x = 62$

Consider the following sequence of operations on an empty queue.

enqueue (21), enqueue (24), dequeue (); enqueue (28); enqueue (32); q = dequeue ();

The value of $s+q$ is $62+24=86$

21	24	28	32
---------------	---------------	----	----

$q = \text{dequeue}$

$q = 24$



Topic: GATE 2023, 2-Marks

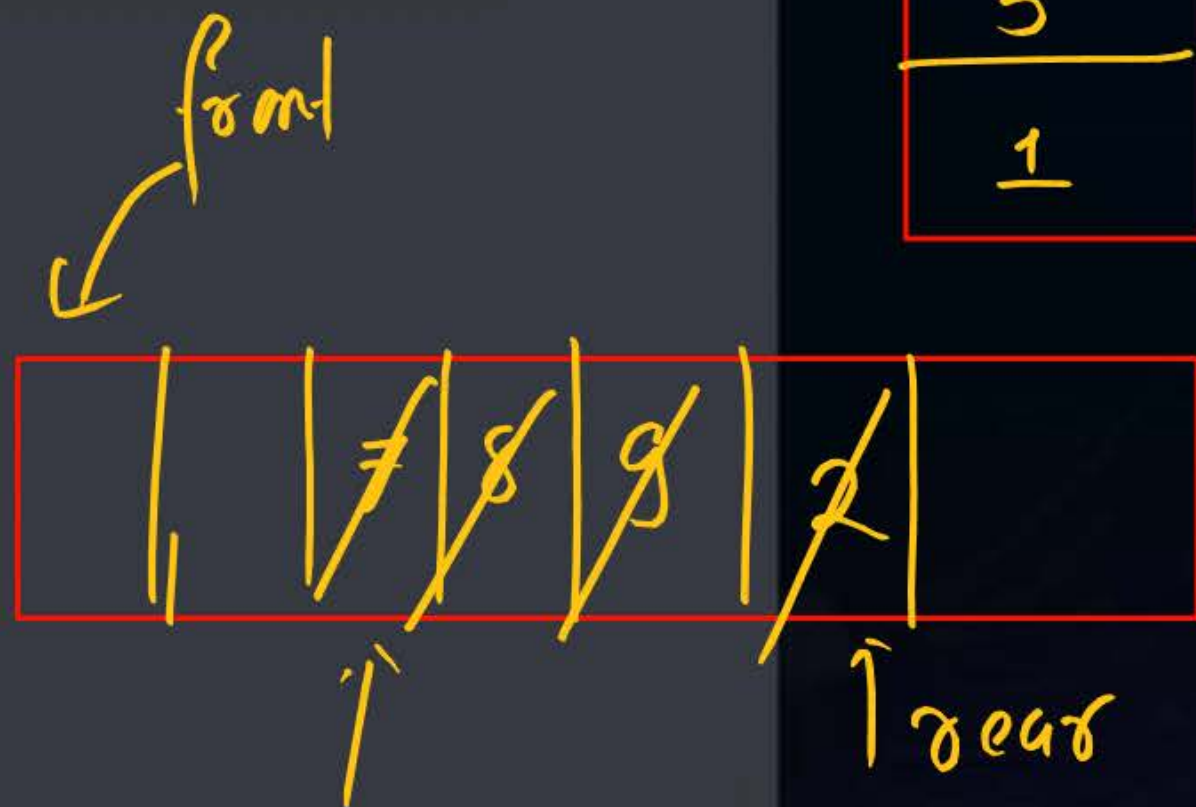


Consider a sequence a of elements $a_0 = 1, a_1 = 5, a_2 = 7, a_3 = 8, a_4 = 9$, and $a_5 = 2$. The following operations are performed on a stack S and a queue Q , both of which are initially empty.

- I. push the elements of a from a_0 to a_5 in that order into S . ✓
- II. enqueue the elements of a from a_0 to a_5 in that order into Q .
- III. pop an element from S . ✓
- IV. dequeue an element from Q . ✓
- V. pop an element from S . ✓
- VI. dequeue an element from Q . ✓
- VII. dequeue an element from Q and push the same element into S . ✓
- VIII. Repeat operation VII three times. ✓
- IX. pop an element from S .
- X. pop an element from S .

The top element of S after executing the above operations is 8.

2
9
8
7
8
7
5
1



Consider the following function

```
void f() {  
    int i;  
    if (!isEmpty()) {  
        i = dequeue();  
        f();  
        Enqueue(i);  
    }  
}
```

What operation performed by above function

- (A) Leave the queue unchanged
- ☒ (B) Reverse order of elements of Queue
- (C) Delete element from front of queue and insert in rear.
- (D) Empties the queue

Consider the following function

```
void f() {
```

```
    int i;
```

```
    if (!isEmpty()) {
```

```
        i = dequeue();
```

```
        f();
```

```
        Enqueue(i);
```

```
    }
```

Que
 $f(1 | 2 | 3)$

$l = 1;$

$f(2 | 3)$

$l = 1$
Enqueue(i)

$f(2 | 3)$

$l = 2$

$f(3)$

$l = 2$
Enqueue(i)

$f(3)$

$l = 3$

$f(\square)$

Enqueue(i) = 3

3 | 2 | 1



2 mins Summary



Topic

Expression

Topic

Evaluation of postfix prefix

Topic

Topic

Topic

THANK - YOU