

Computer Science & IT

Database Management System



Relational Model & Normal Forms

Lecture No. 13



By- Vishal Sir

Recap of Previous Lecture



✓ **Topic** Normal forms { 1NF, 2NF, 3NF, BCNF, 4NF }

✓ **Topic** First normal form (1NF) { No multi-valued attributes }
 { By default normal form of relation is 1NF }

✓ **Topic** Redundancy in relation because of FD

→ If $X \rightarrow Y$ is a non-trivial FD & X is a S.K., then no redundancy w.r.t. $X \rightarrow Y$

→ If $X \rightarrow Y$ is a non trivial FD & X is not a S.K., then redundancy is possible w.r.t. $X \rightarrow Y$.



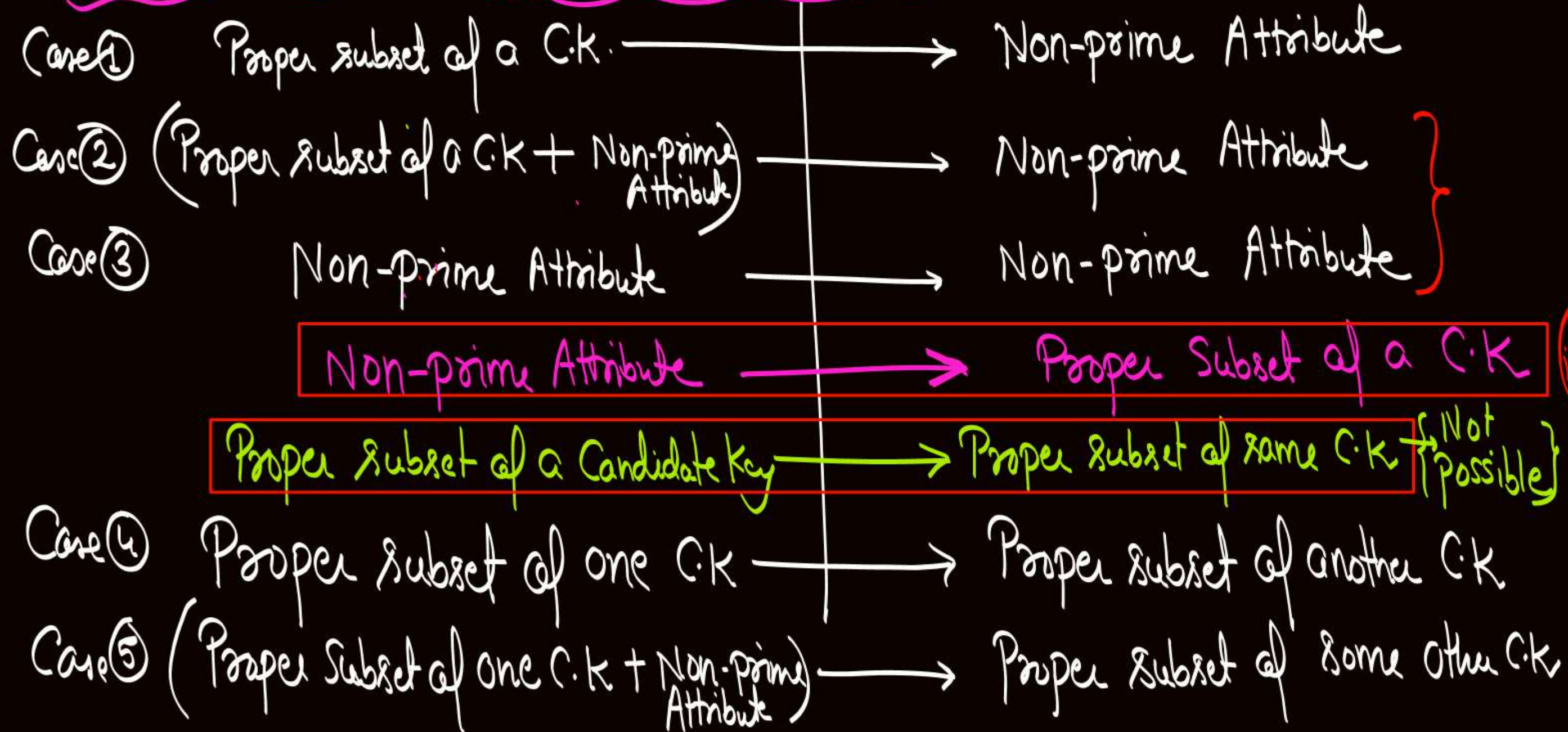


Topics to be Covered



- ✓ Topic Redundancy in relation because of FD
- ✓ Topic Second normal form (2NF)
- ✓ Topic Third normal form (3NF)
- ✓ Topic Boyce codd normal form (BCNF)
- ✓ Topic Decomposition of relation

Possible non-trivial FDs " $X \rightarrow Y$ " that may cause redundancy in the relation are,



(Not possible)
if $X \rightarrow$ Prime Attribute,
then that Prime
Attribute can be
replaced by X,
and X will also
become part of
C.K. (i.e. Prime Attribute)



Topic : Redundancy in relation because of FD

Normal Form \ Case	Case 1	Case 2	Case 3	Case 4	Case 5
1 NF	✓	✓	✓	✓	✓
2 NF	✗ Not allowed	✓	✓	✓	✓
3 NF	✗	✗	✗	✓	✓
BCNF	✗	✗	✗	✗	✗

For 2NF,
functional dependency
Similar to Case ①
are not allowed.
All other functional
dependencies are
allowed.

→ All types of functional dep. are allowed in 1 NF

→ W.r.t. 3NF
Case ① Case ② & Case ③ type of FDs are not allowed.
But Case ④ & Case ⑤ type FDs may be present.

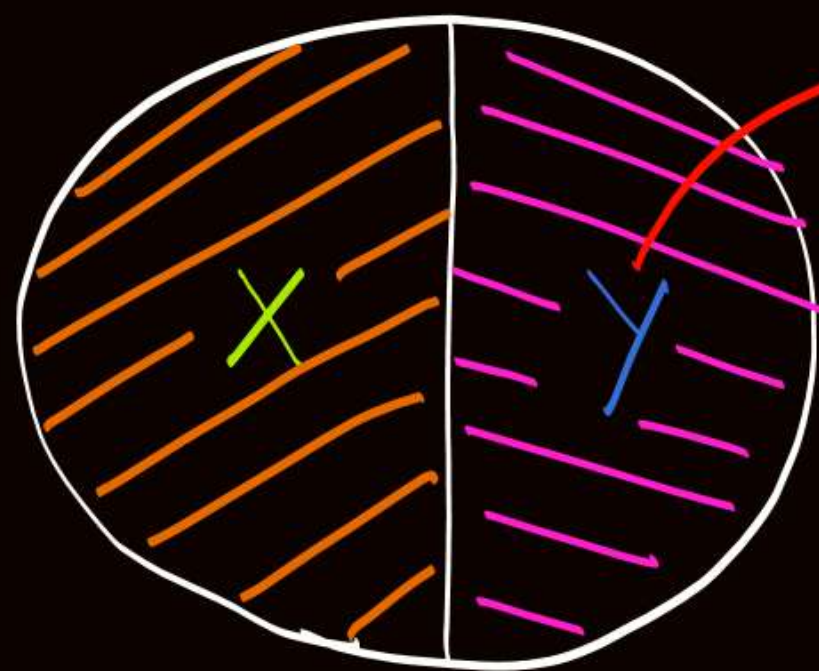
All 5 types of FDs are not allowed for BCNF.



Topic : Second normal form (2NF)

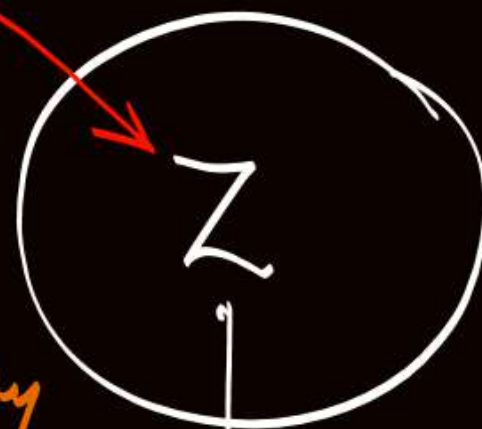
- A relation R is in 2NF only if,
 - (i) Relation is in 1NF.
 - (ii) Relation must not contain any partial dependency

Partial Functional Dependency :-



Let Y can determine Z
i.e. $Y \rightarrow Z$

then we say that
Partial dependency
exists in the
relation.



Non-prime
Attribute

X & Y are two set of attributes
& (XY) together is Candidate Key
of the relation

{ X & Y becomes some
Proper subsets of C.K }

Note: Let "XY" is Candidate key
& Z is non-prime attribute

① if 'Z' is fully dependent
on "XY" { i.e. No proper subset
of XY can determine Z }, then

$XY \rightarrow Z$ is a
Full functional dependency

② If a Proper subset of
Candidate key "XY" can
determine 'Z', then

$XY \rightarrow Z$ is called
a Partial functional dependency.



Topic : Third normal form (3NF)

A relation R is in 3NF only if,

Every non-trivial functional dependency $X \rightarrow Y$ is with

(i) X as a Super Key { in $X \rightarrow Y$ if 'X' is a Super Key.
then there will be no redundancy
wrt. $X \rightarrow Y$, hence $X \rightarrow Y$ will be
in BCNF, and hence in 3NF as well.

(or)

(ii) Y as a prime attribute

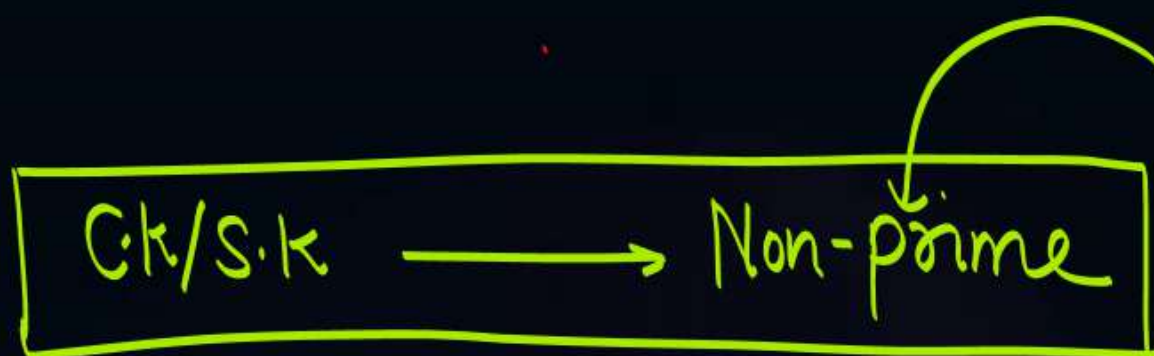
ie, Case (1), Case (2) & Case (3) are not allowed.



Topic : Third normal form (3NF)

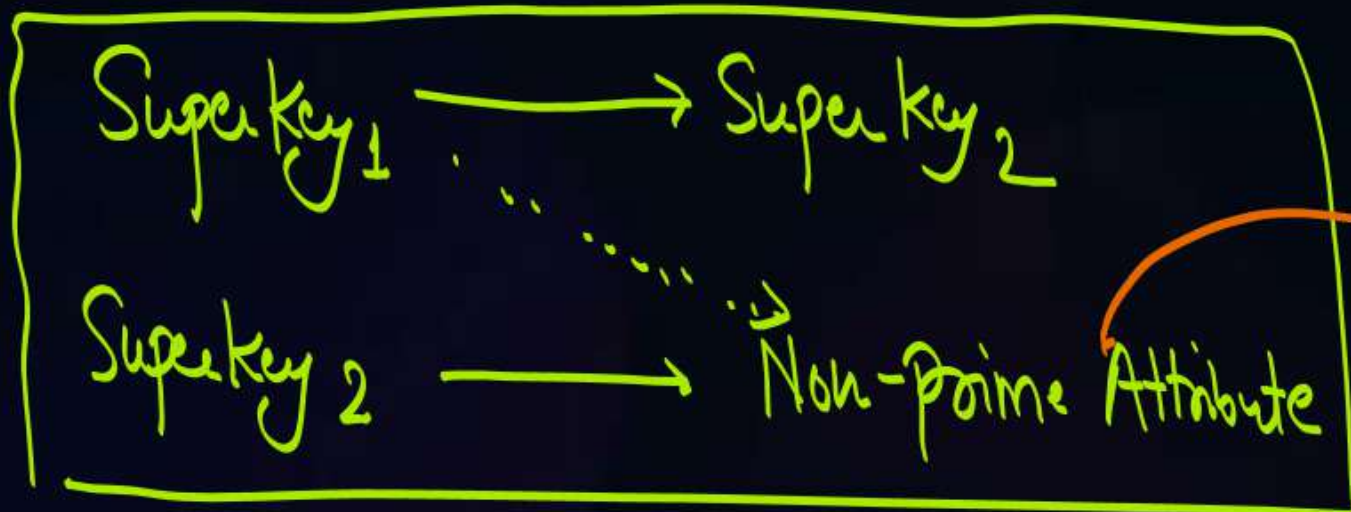
- A relation R is in 3NF only if.

Relation R does not contain any transitive dependency.



In this case non-prime attribute is directly dependent on Ck/Sk , ∴ No transitive dependency

A functional dependency is called transitive dependency if "Non-prime" attribute is transitively dependent on Superkey/ Ck . { i.e. Not directly dependent on Sk or Ck }



In this case also non-prime attribute is directly dependent on Sk_2

Super key \rightarrow N.P.A.₁

N.P.A.₁ \rightarrow N.P.A.₂

NPA₁ is directly dependent on Super key

\therefore Super key \rightarrow NPA₁ is allowed in 3NF

But NPA₂ is not directly dependent on S.K.

\therefore $\{ \text{NPA}_1 \rightarrow \text{NPA}_2 \text{ is not allowed in 3NF} \}$

i.e. Case (3) type of FDs are not allowed

it is not a SK

(P.S.C.K + Non-prime Attribute)

\rightarrow Non-prime Attribute

This non-prime attribute is not directly dependent on a Super key

i.e. Case (2) type of FDs are not allowed



Topic : Boyce codd normal form (BCNF)

A relation R is in BCNF only if
Every non-trivial functional dependency
 $X \rightarrow Y$ must be with
"X" as a super key of relation R

For a relation to be in BCNF there must be no redundancy because of functional dependency

∴ All 5 types of FDs are not allowed in BCNF

#e.g.

Given $R(ABCDEF)$ and

$F = \{AB \rightarrow CD, \underline{D} \rightarrow A, C \rightarrow E, B \rightarrow F\}$

Find the normal form of the relation.

$AB \rightarrow CD$ {BCNF}

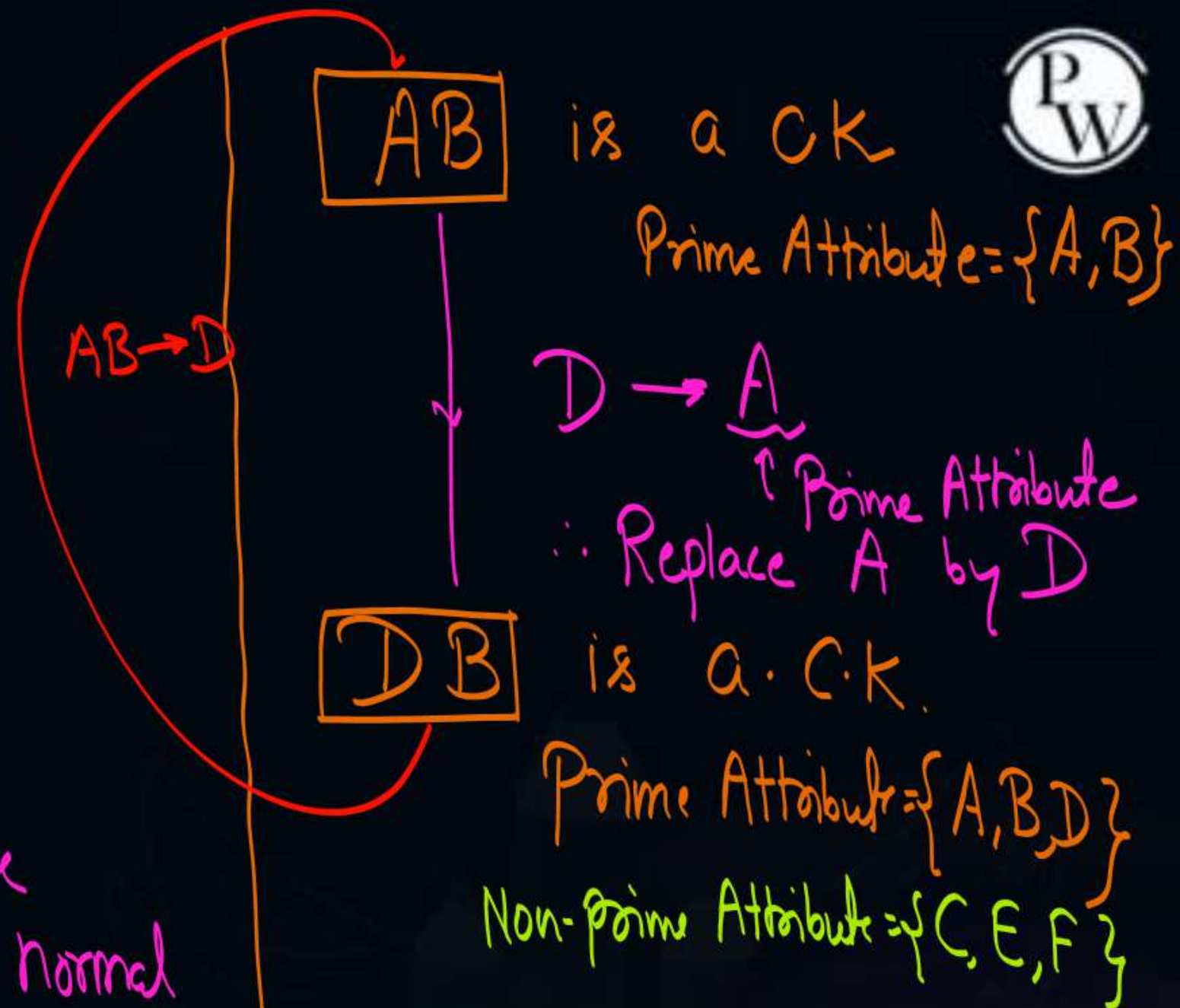
$D \rightarrow A$ {3NF}

$C \rightarrow E$ {2NF}

$B \rightarrow F$ {1NF}

Normal form
of the relation
will be the
least of the normal
forms of all the
FDs

Hence Normal form of Relation is **1NF**



C.K. = (AB)

(D B) ① AB \rightarrow CD
S.K. \rightarrow \therefore Allowed upto BCNF

② D \rightarrow A
Proper Subset of one C.K. \rightarrow Proper Subset of another C.K. \rightarrow Case ④ \rightarrow Allowed upto 3NF
But not allowed in BCNF

③ C \rightarrow E
N.P.A. \rightarrow N.P.A. \rightarrow Case ③ \rightarrow Allowed upto 2NF
not allowed in 3NF

④ B \rightarrow F
P.S.C.K. \rightarrow N.P.A. \rightarrow Case ① \rightarrow Allowed in 1NF
not allowed in 2NF

Decomposition of Relation
into
Sub-relations

#e.g.

Given $R(ABCDE)$ and $F=\{AB \rightarrow \check{C}, C \rightarrow \check{D}, B \rightarrow \check{E}\}$

$(AB)^+ = \{A, B, C, D, E\}$
all attributes
 $\therefore \boxed{AB}$ is a C.K.



Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.

P.A = $\{A, B\}$
N.P.A = $\{C, D, E\}$

$\underbrace{AB}_{S.K} \rightarrow C \{BCNF\}$

Case ③ $\underbrace{C}_{N.P.A} \rightarrow \underbrace{D}_{N.P.A} \{2NF\}$

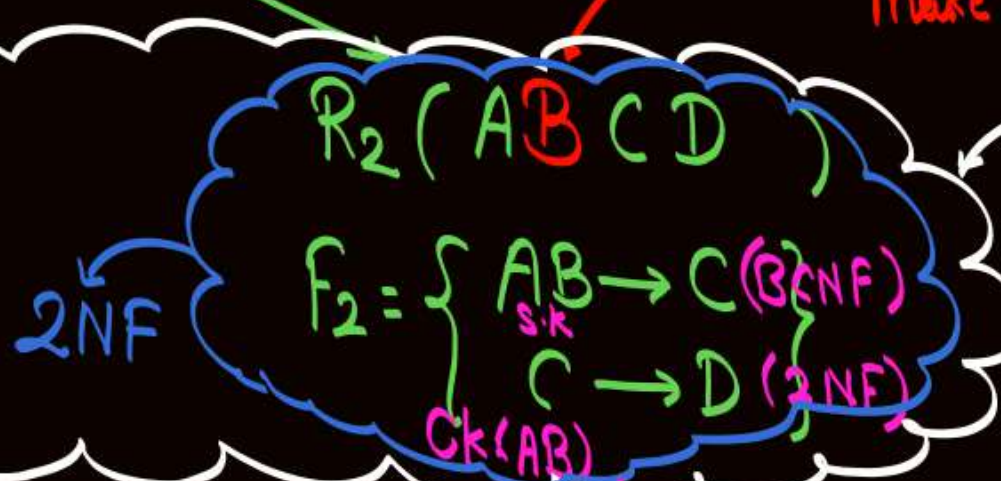
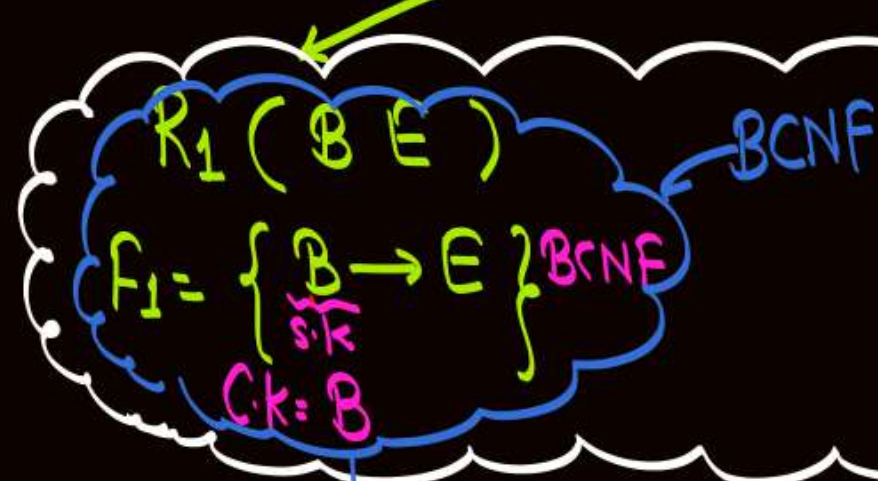
Case ① $\underbrace{B}_{P.S.C.K} \rightarrow \underbrace{E}_{N.P.A} \{1NF\}$

Normal form of Relation
is 1NF

$$F = \left\{ \begin{array}{l} AB \rightarrow C \\ C \rightarrow D \\ B \rightarrow E \end{array} \right\}$$

✓ R(ABCDE) is in 1NF
 Not in 2NF because of FD "B → E"
 ∴ Decompose w.r.t. B → E

$$(BE)^+ = \{B, E\}$$

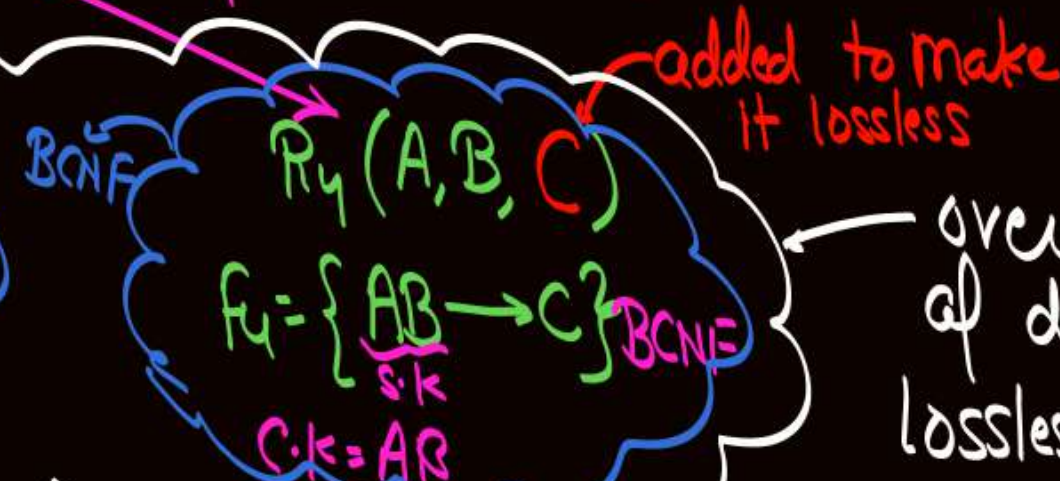
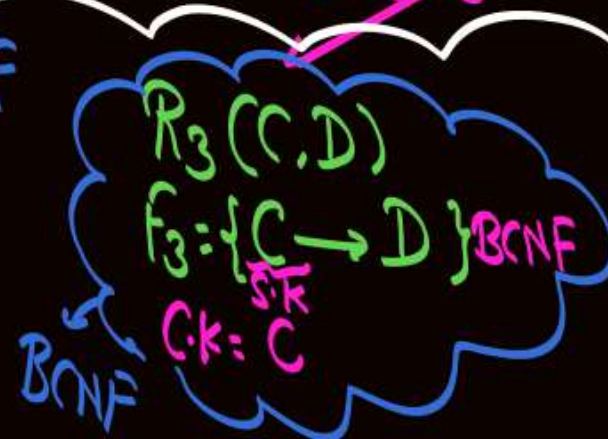
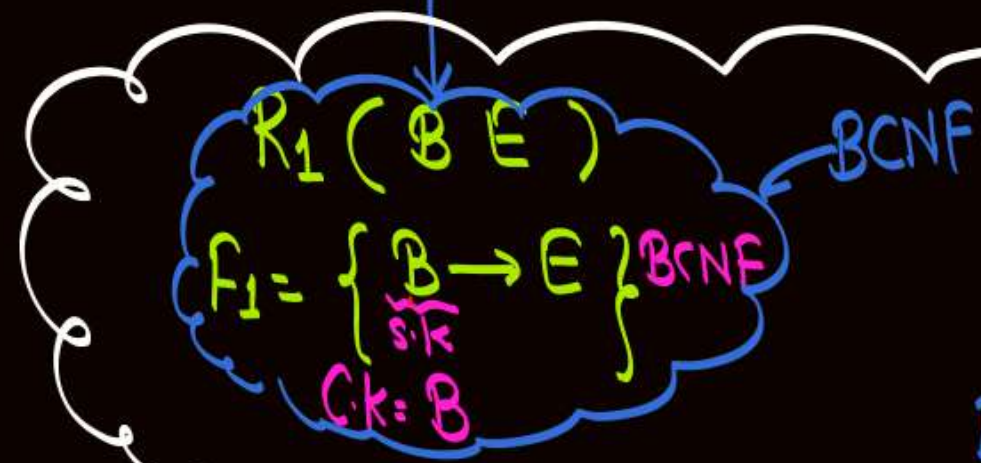


SK. of another relation is added to make it lossless

overall normal form of database is 2NF
 + lossless join decomposition
 + Dep. preserving decomposition

↓ R₂(ABCD) is not in 3NF because of C → D
 ∴ Decompose w.r.t. C → D

$$(CD)^+ = \{C, D\}$$



added to make it lossless

overall Normal form of database is BCNF
 + lossless join decomposition
 + Dep. preserving decomposition.

H.W.



#e.g.

Given $R(ABCDEF)$ and $F=\{A \rightarrow BCDEF, BC \rightarrow ADEF, D \rightarrow E, E \rightarrow F\}$

Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.

H.W.

#e.g.

Given $R(ABCD)$ and $F=\{AB \rightarrow C, BC \rightarrow D\}$



Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.

H.W.



#e.g.

Given $R(ABCDEFGH IJ)$ and $F=\{AB \rightarrow C, A \rightarrow DE, B \rightarrow F, F \rightarrow GH, D \rightarrow IJ\}$

Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.

H.W.
#e.g.



Given $R(ABDLPT)$ and $F=\{B \rightarrow PT, T \rightarrow L, A \rightarrow D\}$

Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.

H.W.

#e.g.

Given $R(ABCDE)$ and $F:\{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$



Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.

HW.

#e.g.



Given $R(ABCD)$ and $F=\{AB \rightarrow CD, D \rightarrow A\}$

Find the normal form of the relation, and if relation is not already in BCNF then decompose the relation up to BCNF.



2 mins Summary



Topic

Redundancy in relation because of FD

Topic

Second normal form (2NF)

Topic

Third normal form (3NF)

Topic

Boyce codd normal form (BCNF)

Topic

Decomposition of relation

THANK - YOU