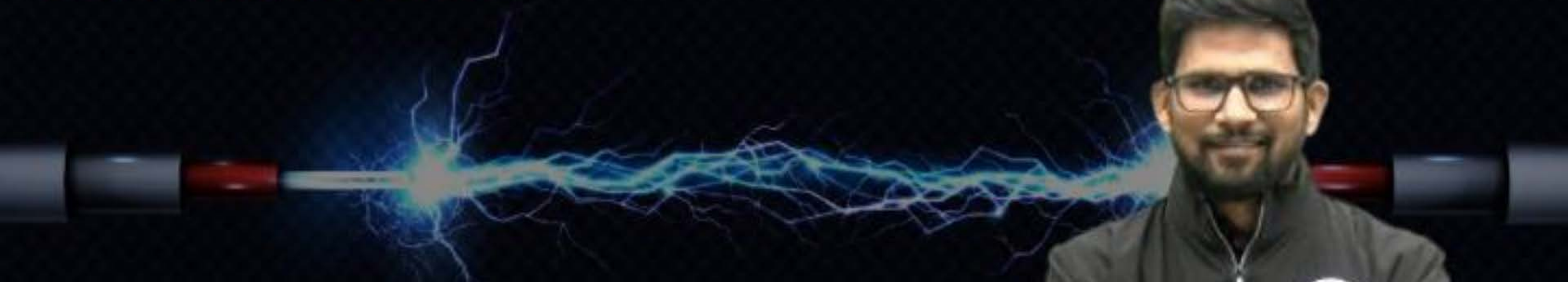




COMPUTER SCIENCE & IT

DIGITAL LOGIC




Lecture No. 04

Combinational Circuit



By- Chandan Gupta Sir



Recap of Previous Lecture

Look ahead carry adder

H.S. , F.S.



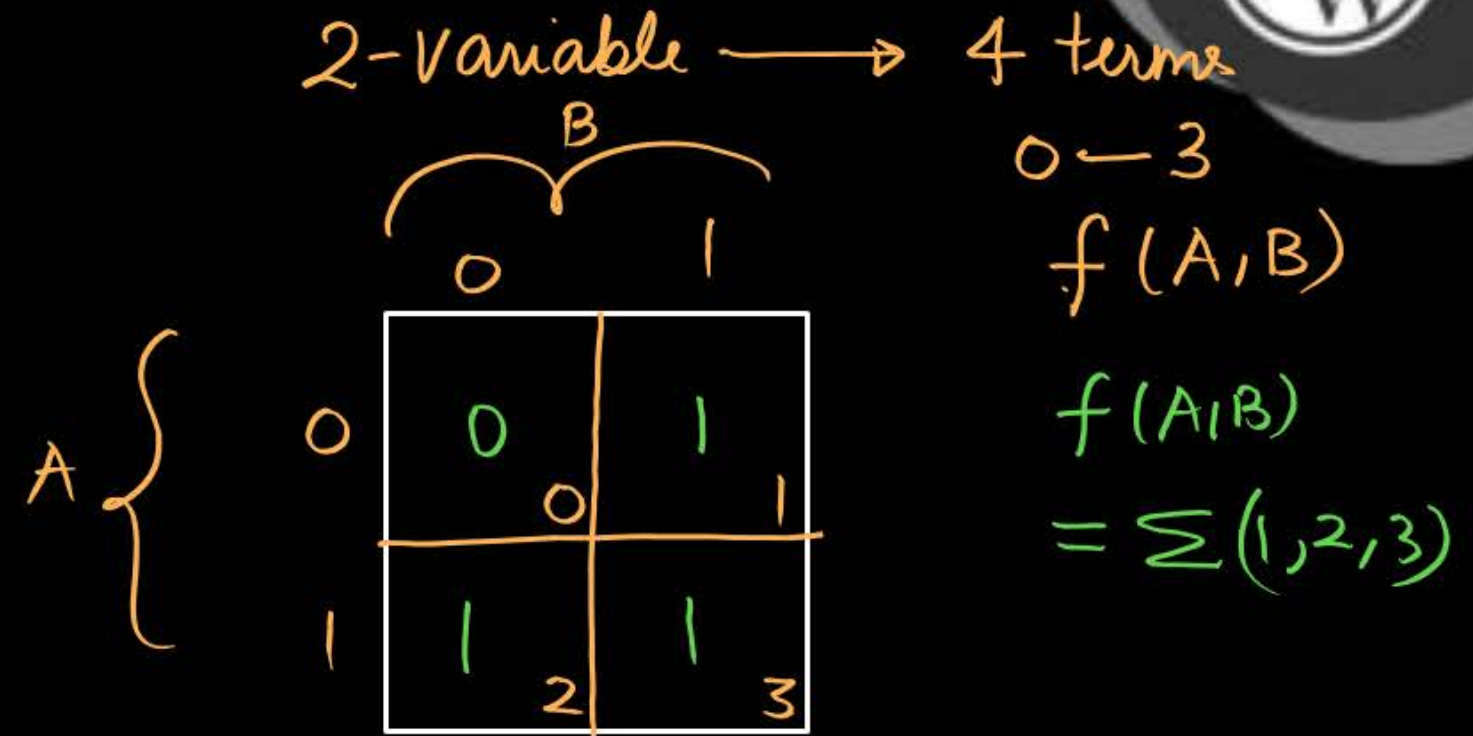
Topics to be Covered

K-Map

[K-Map]

Used for Entries :

- '0'
- '1'
- X \rightarrow don't care
- Variable



What is don't care 'X' →

	A	B	C	y
0	0	0	0	X
	0	0	1	0
2	0	1	0	X
	0	1	1	0
4	1	0	0	X
	1	0	1	1
6	1	1	0	X
	1	1	1	1

$$y(A, B, C) = \sum(5, 7) + d\sum(0, 2, 4, 6)$$

$$ABC > 3$$



0-9
↓

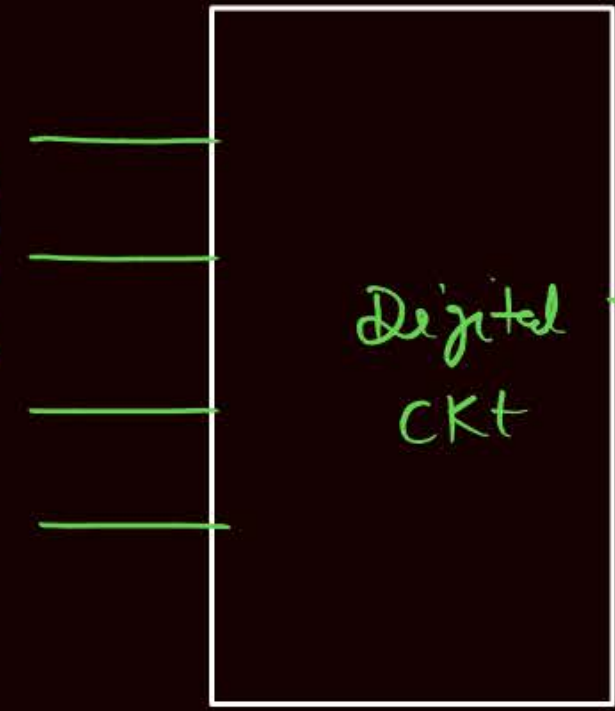
$$(126)_{10} = (1111110)_2 = (0001\ 0010\ 0110)_{BCD}$$

	8	4	2	1
	2^3	2^2	2^1	2^0
0 —	0	0	0	0
1 —	0	0	0	1
2 →	0	0	1	0
3 →	0	0	1	1
4 →	0	1	0	0
5 →	0	1	0	1
6 →	0	1	1	0
7 →	0	1	1	1

8 —	1	0	0	0
9 —	1	0	0	1

1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

Invalid BCD Codes



O/P is '1' when i/p is divisible by '2'.

$$(25)_{10} = (11001)_2 = (0010\ 0101)_{BCD}$$

2-variable, 3-variable and 4-variable K-maps



		B	
		0	1
A	0	0	1
	1	2	3

ABC
✓✓

		BC			
		00	01	11	10
A	0	0	1	3	2
	1	4	5	7	6

		\bar{B}	B
\bar{A}			1
A	1		1

$$f(A,B) = \sum(1, 2, 3)$$

$$\begin{aligned}
 &= (A + B) \\
 &= \bar{A}B + A\bar{B} + AB \\
 &= B(\bar{A} + A) + A(\bar{B} + B) \\
 &= B + A
 \end{aligned}$$

		A	
		0	1
BC	00	0	4
	01		5
	11	3	7
	10	2	6

AB

		C	
		0	1
AB	00	0	1
	01	2	3
	11	6	7
	10	4	5

ABCD

AB {

	00	01	11	10
00	0	1	3	2
01	4	5	7	6
11	12	13	15	14
10	8	9	11	10

\Leftrightarrow

$\overline{A}\overline{B}$
 $\overline{A}B$
 AB
 $A\overline{B}$

	$\overline{C}\overline{D}$	$\overline{C}D$	CD	$C\overline{D}$
$\overline{A}\overline{B}$	0	1	3	2
$\overline{A}B$	4	5	7	6
AB	12	13	15	14
$A\overline{B}$	8	9	11	10



- Why gray code is used in case of K-map?

		00 $\overline{B}\overline{C}$	01 $\overline{B}C$	11 BC	10 $B\overline{C}$
0 \overline{A}			1	1	
1 A					

$$\begin{aligned}
 &\overline{A}\overline{B}C \\
 &+ \overline{A}BC \\
 &= \overline{A}C(\overline{B}+B) \\
 &= \overline{A}C
 \end{aligned}$$

$\overline{A}C$

binary	gray
0111	→ 0100
1000	→ 1100

	binary	Gray
0	→ 00	→ 00
1	→ 01	→ 01
2	→ 10	→ 11
3	→ 11	→ 10

binary	Gray
1001	→ 1101
1010	→ 1111

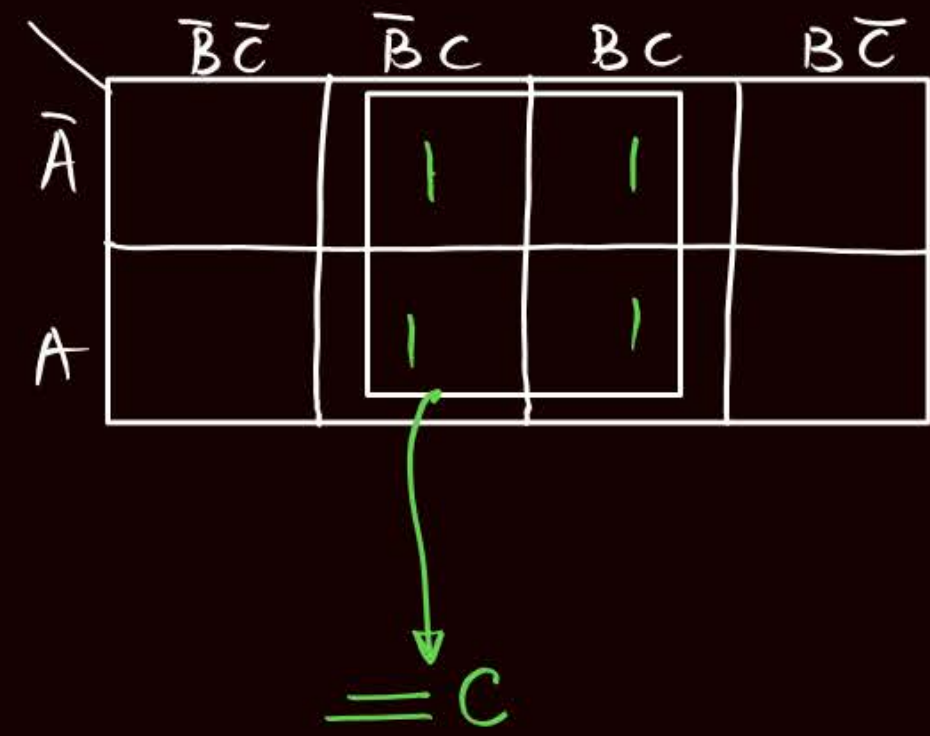
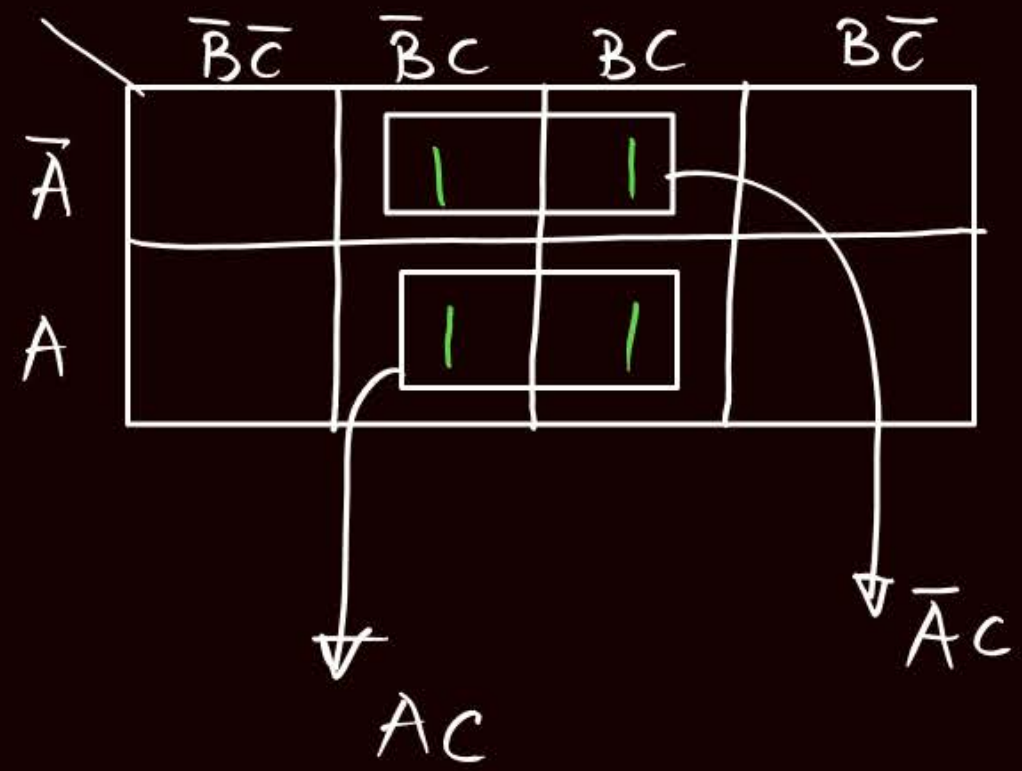
	$\overline{B}\overline{C}$	$\overline{B}C$	$B\overline{C}$	BC
\overline{A}		1	1	
A				

→ binary codes are used.

$$\overline{A}\overline{B}C + \overline{A}B\overline{C}$$

$$\overline{A}[\overline{B}C + B\overline{C}]$$

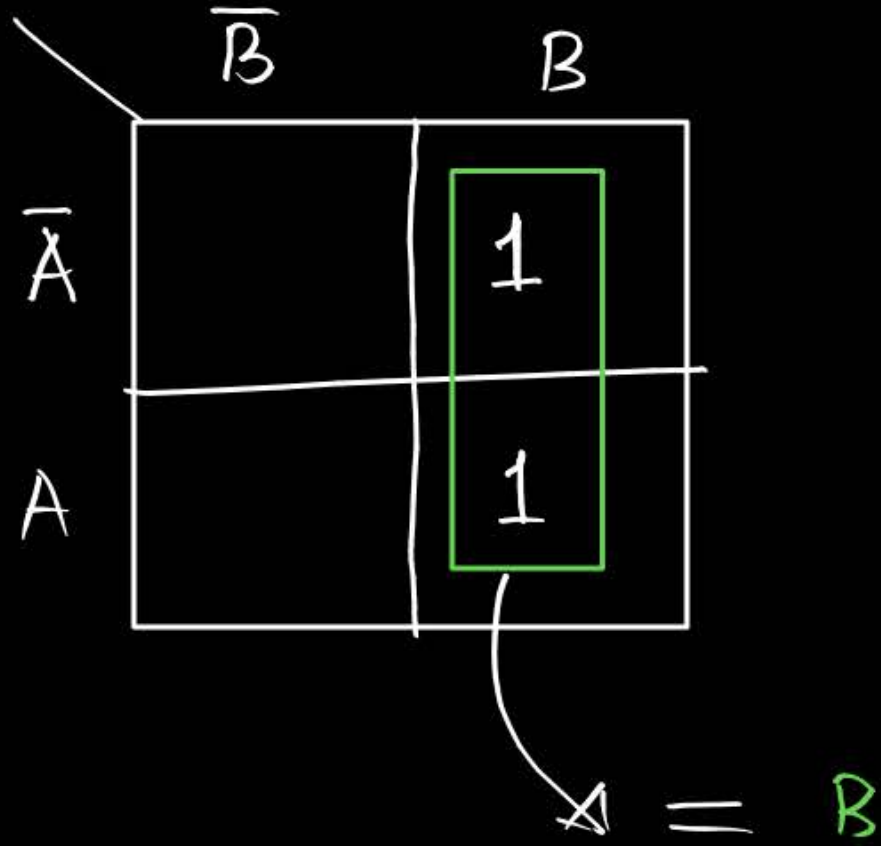
→ no simplification possible



$$\begin{aligned}
 &= \bar{A}C + AC \\
 &= C(\bar{A} + A) \\
 &= C
 \end{aligned}$$

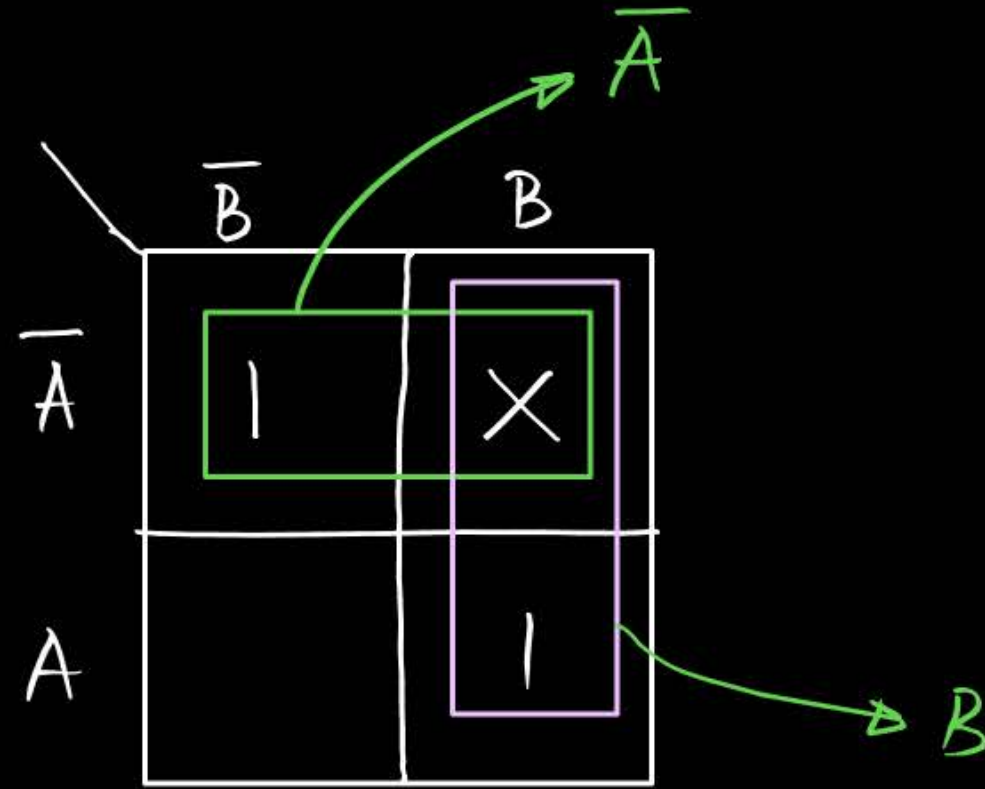
[Question]

$$f(A, B) = \Sigma(1, 3)$$
$$= B$$



[Question]

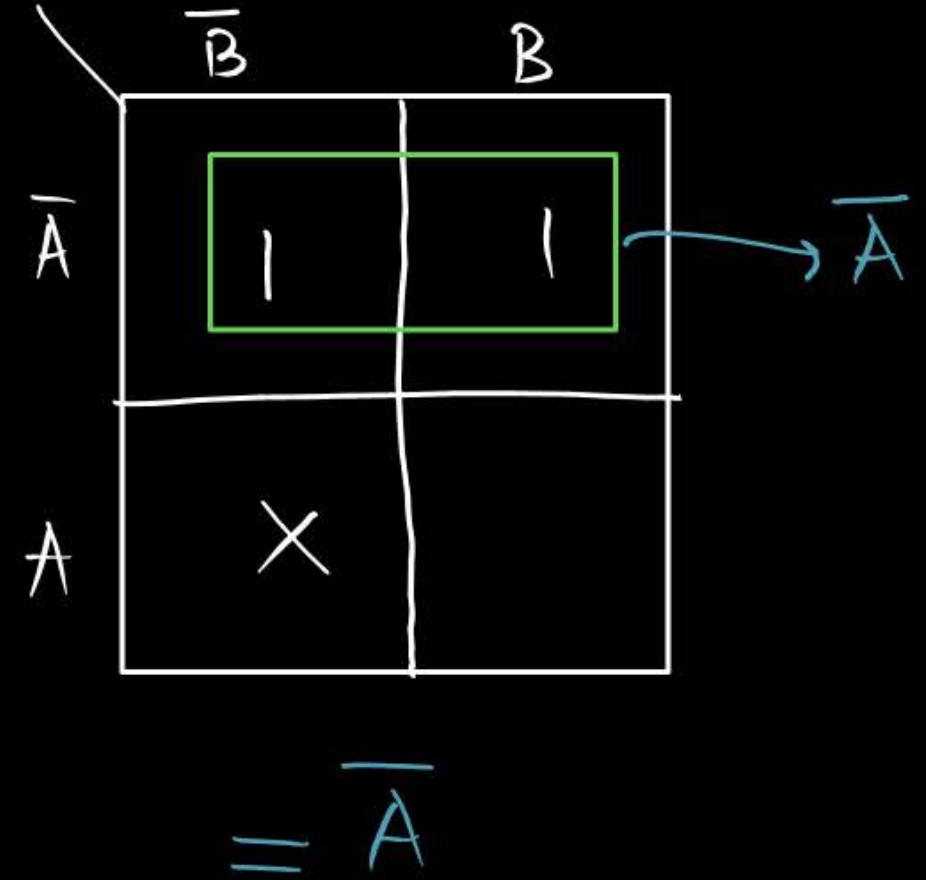
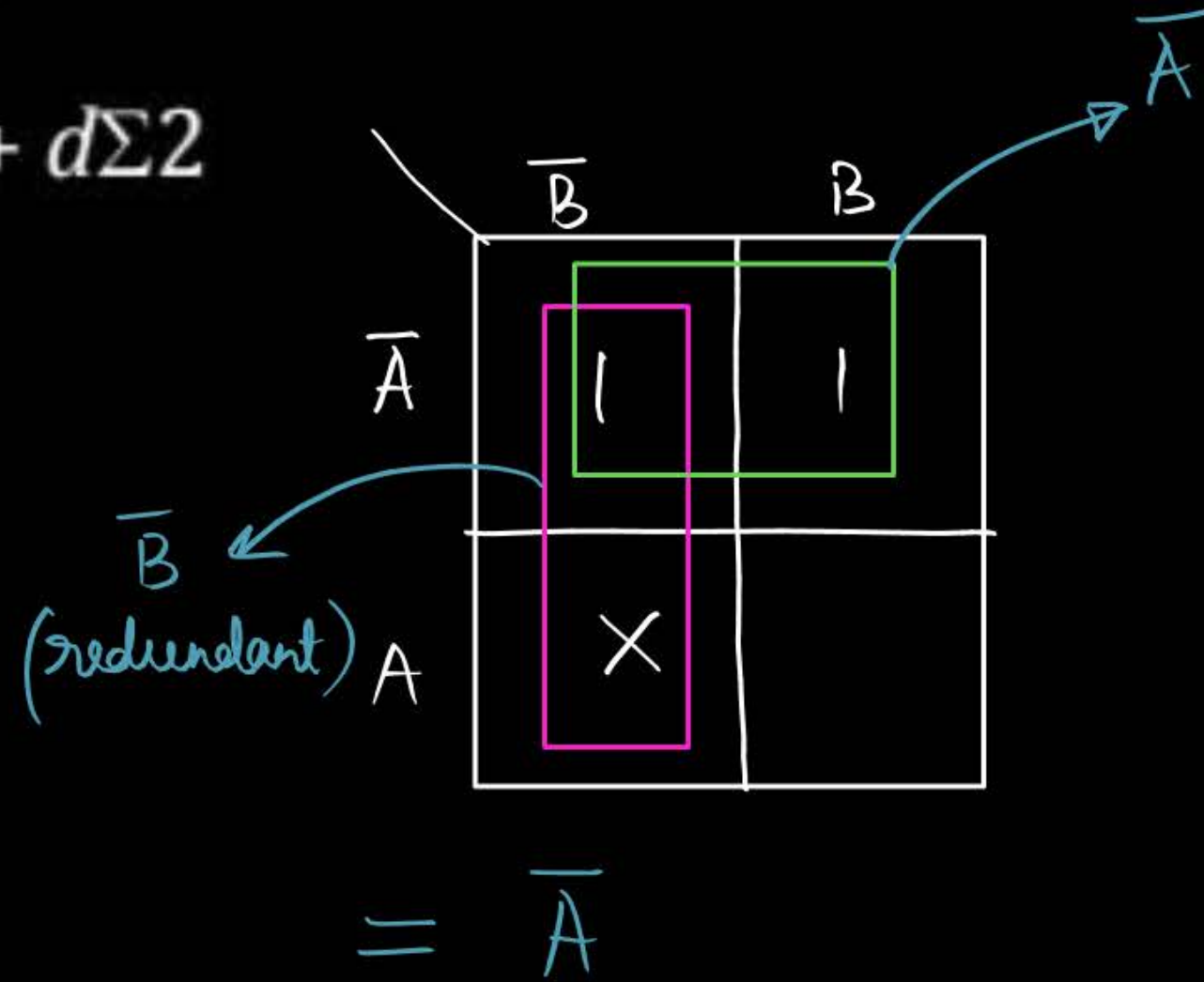
$$f(A, B) = \Sigma(0, 3) + d\Sigma(1)$$



$$= \bar{A} + B$$

[Question]

$$f(A, B) = \Sigma(0, 1) + d\Sigma 2$$





2 Minute Summary



K-Map

Thank you

GW
Soldiers !

