

CS & IT ENGINEERING



Operating System

Virtual Memory

Lecture – 03

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Recap of Previous Lecture



Topic

Effective Memory Access Time

Topic

Page Replacement Algorithm

Topic

FIFO, Optimal Algorithms

Topics to be Covered



Topic

Page Replacement Algorithm

Topic

LRU, MRU Algorithms

Topic

LIFO, Frequency Based Algorithms



Topic : Least Recently Used (LRU)

Replace the page which has not been used since longest period of time.

Assume:

- Number of frames = 3 (All empty initially)
- Page reference sequence: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

1	1	1	4	4	4	5		3	3	3
	2	2	2	1	1	1		1	4	4
		3	3	3	2	2		2	2	5
✓	✓	✓	✓	✓	✓	✓	Hit Hit	✓	✓	✓

No. of p.f. = 10



Topic : Least Recently Used (LRU)

Advantages:

1. Efficient.
2. Doesn't suffer from Belady's Anomaly

Disadvantages:

1. Complex Implementation
2. Expensive
3. Requires hardware support



Topic : Question

- Number of frames = 4
- Pure demand paging used
- Page reference sequence: 5, 7, 0, 1, 7, 6, 7, 2, 1, 6, 7, 6, 1
- Number of page faults for FIFO, optimal and LRU policies? $7, 6, 6$

FIFO:-

5	5	5	5	6	6	6
	7	7	7	7	2	2
		0	0	0	0	7
			1	1	1	1
✓	✓	✓	✓	✓	✓	✓

no. of p. faults = 7

optimal:-

5	7	0	1	7	6	7	2	1	6	7	6	1
5	5	5	5		6		6					
	7	7	7		7		7					
		0	0		0		2					
			1		1		1					
✓	✓	✓	✓	✗	✓	✗	✓	✗	✗	✗	✗	✗

no. of P.F. = 6

LRU:-

5	7	0	1	7	6	7	2	1	6	7	6	1
5	5	5	5		6		6					
	7	7	7		7		7					
		0	0		0		2					
			1		1		1					
✓	✓	✓	✓	✗	✓	✗	✓	✗	✗	✗	✗	✗

P.f. = 6



Topic : Question

Consider the following page references:

2, 3, 4, 5, 6, 4, 5, 2, 7, 8, 9, 8, 9, 8, 9, 1, 6, 5, 6, 5, 3

Using optimal policy and 4 frames. Memory access time is 2ms without page fault and 40ms with page fault. The effective memory access time for servicing the above page requests is ____ ms?

2	2	2	2	2	7	7	9	9	9
	3	3	3	6	6	6	6	6	6
		4	4	4	4	8	8	1	1
			5	5	5	5	5	5	3

$$\text{no. of p.f.} = 10$$

$$\text{Page fault rate} = \frac{10}{21}$$

$$\begin{aligned} \text{EMAT} &= \frac{11}{21} * 2 + \frac{10}{21} * 40 = 20.095 \\ &= 20.1 \text{ ms} \end{aligned}$$



Topic : Last In First Out (LIFO)

replace [↓] the page which comes last in mem.

Assume:

- Number of frames = 3 (All empty initially)
- Page reference sequence: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

no. of page faults = 8

<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>	<u>1</u>
	2	2	2	2	2	2	2
		3	4	5	3	4	5
✓	✓	✓	✓	✓	✓	✓	✓



Topic : Most Recently Used (MRU)

replace the page which has been referred ^{most} recently.

Assume:

- Number of frames = 3 (All empty initially)
- Page reference sequence: ~~1~~, ~~2~~, ~~3~~, ~~4~~, 1, 2, 5, 1, 2, 3, 4, 5

1	1	1	1
	2	2	2
		3	4

1	2	3
5	5	5
4	4	4

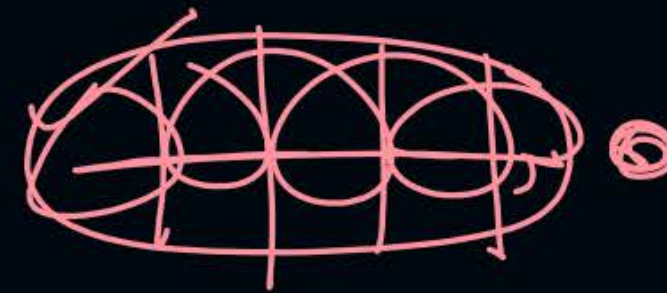
no. of p.f. = 7

✓ ✓ ✓ ✓ ✗ ✗ ✓ ✓ ✓



Topic : Counting Algorithms

- Counting algorithms look at the number of occurrences of a particular page and use this as the criterion for replacement.
- Such counting algorithms includes:
 - LFU (Least Frequently Used)
 - MFU (Most Frequently Used)





Topic : Least Frequently Used (LFU)

replace the page which has been referred min. no. of times

Assume:

- Number of frames = 3 (All empty initially)
- Page reference sequence: ~~1~~ ~~2~~ ~~0~~ ~~3~~ 0 ~~4~~ ~~2~~ ~~3~~ 0 3 2

Page	Frequency
1	1
2	1 2 3
0	1 2 3
3	1 2 3
4	1

1	1	1	3	3	2	2
	2	2	2	4	4	3
		0	0	0	0	0
✓	✓	✓	✓	×	✓	✓
				×	✓	✓
					×	×
						×

no. of p. faults = 7

→ Tie breaker ⇒ FIFO



Topic : Most Frequently Used (MFU)

replace the page which has been referred

Assume:

- Number of frames = 3 (All empty initially)

- Page reference sequence: ~~1~~~~2~~~~0~~~~3~~~~0~~~~4~~~~2~~~~3~~~~0~~~~3~~~~2~~

<u>1</u>	<u>1</u>	<u>1</u>	3	3		3		2
	2	2	2	2		0		0
		0	0	4		4		4
✓	✓	✓	✓	✗	✓	✗	✗	✓

no. of p.f. = 7

max. no. of times
↳ tie breaker = FIFO

Page	frequency
1	1
2	1 2 3
0	1 2 3
3	1 2 3
4	1

<u>optimal:-</u>		20 faults				<u>hits $\Rightarrow 9$</u>				<u>hit</u>			
		$a_1, a_2, \dots, a_{10}, a_{11}, a_{12}, \dots, a_{20}$				$a_1, a_2, \dots, a_9, a_{10}, a_{11}, \dots, a_{20}$							
P.f. = 30		a_1	a_1	a_1		a_1							
		a_2	a_2	}		\vdots							
		\vdots	\vdots			\vdots							
		a_9	a_9			a_9							
		a_{10}	a_{11}	a_{12}		a_{20}							a_{20}

$$\text{Difference} = 31 - 30 = 1$$



Topic : Question

H.W.

[GATE-2014]



- #Q. A main memory can hold 3 page frames and initially all of them are vacant. Consider the following stream of page requests :
2, 3, 2, 4, 6, 2, 5, 6, 1, 4, 6
If the stream uses FIFO replacement policy, the hit ratio h will be ?

- A** 11/3
- B** 1/11
- C** 3/11
- D** 2/11



Topic : Question

H. W.

#Q. A virtual memory system has only 2-page frames which are empty initially. Using demand paging the following sequence of page reference is passed through this system.

9, 8, 7, 8, 7, 9, 7, 9, 8, 9

Minimum possible number of page faults ?



Topic : Question

[GATE-2007]



#Q. The address sequence generated by tracing a particular program executing in a pure demand paging system with 100 bytes per page is
0100, 0200, 0430, 0499, 0510, 0530, 0560, 0120, 0220, 0240, 0260, 0320, 0410.

Suppose that the memory can store only one page and if X is the address which causes a page fault then the bytes from addresses x to $x + 99$ are loaded on to the memory.

How many page faults will occur?

A 0

B 4

C ✓ 7

D 8

Page in mm

~~0100 - 0199~~

~~0200 - 0299~~

~~0430 - 0529~~

~~0530 - 0629~~

~~0120 - 0219~~

~~0220 - 0319~~

0320 - 0419

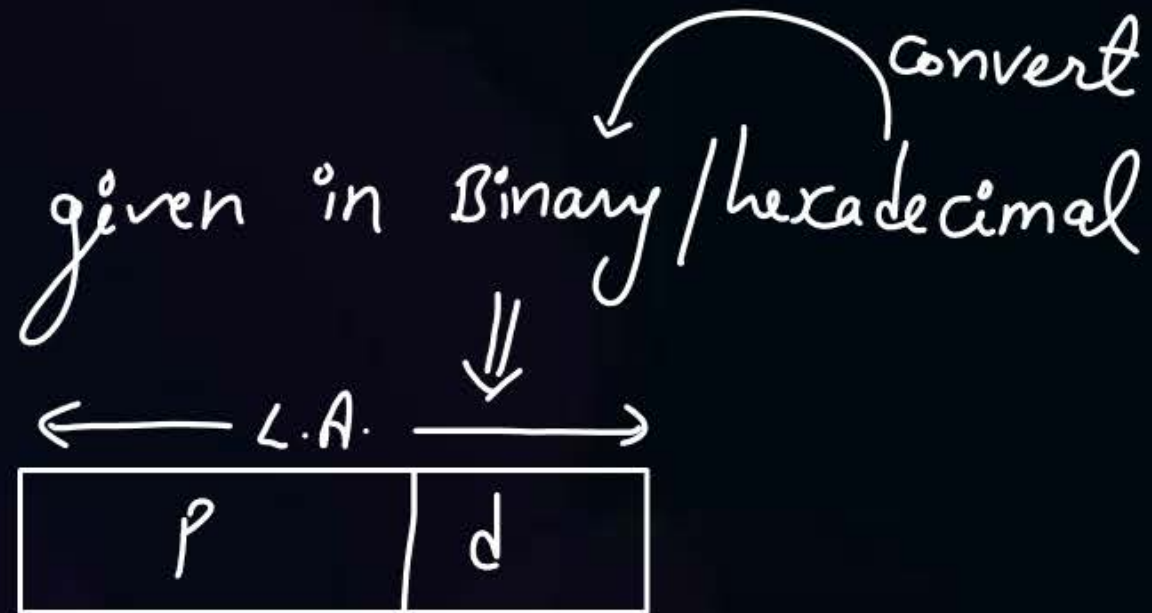


Topic : Making Page Reference Sequence

Logical add.
or
virtual add. $\} \longrightarrow$ Page no.

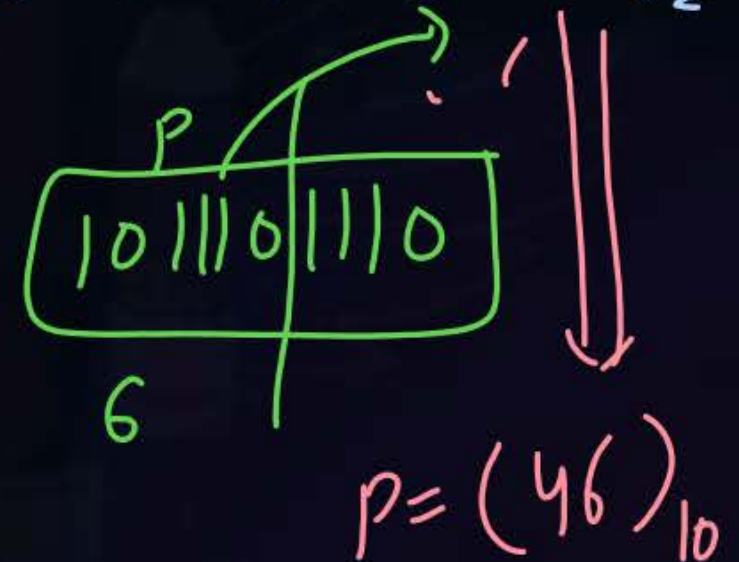
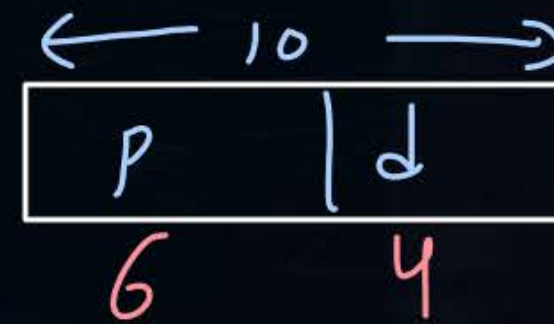
option 1:-

L.A. (V.A.)



example:- L.A. = 10 bits
Page size = 16 bytes = $2^4 = 16$

L.A. = 1011101110 \Rightarrow $P = (101110)_2$



option 2 :-
L.A. (V.A.) given in decimal

$$p = \left\lfloor \frac{\text{L.A.}}{\text{Page size}} \right\rfloor$$

$$d = \text{L.A.} \% \text{Page size}$$

ex:-

Page size = 4B

$$0/4 = 0^p$$

$$0 \% 4 = d = 0$$

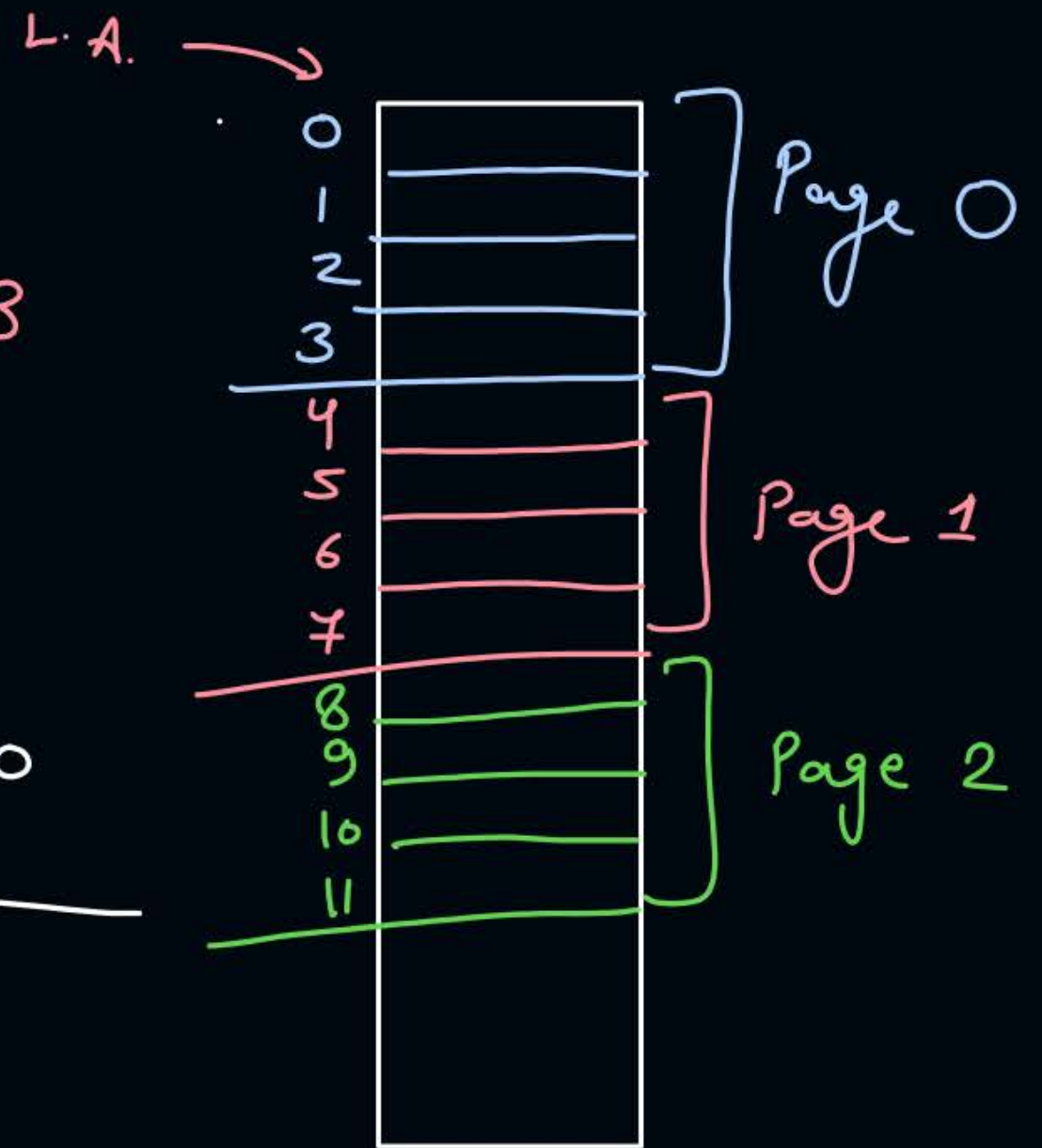
$$\text{Add} = 1$$

$$\lfloor 1/4 \rfloor = 0^p$$

$$1 \% 4 = 1^d$$

$$\lfloor 10/4 \rfloor \Rightarrow 2$$

$$10 \% 4 = 2$$



$$\begin{array}{r} 4 \overline{) 10} (2 \\ \underline{- 8} \\ 2 \end{array}$$

Ques)

H.W.

Page size = 2048 bytes

L.A.	p	d
5184		
2590		
2003		
1004		
9822		
15623		



2 mins Summary

Topic

Page Replacement Algorithm

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LRU, MRU Algorithms

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LIFO, Frequency Based Algorithms



Happy Learning

THANK - YOU