

# Electrical Engineering



## Electronics and Communication Engineering



**Digital Logic**

**Practice Sheet – 01**

**Discussion**

**Boolean Theorems and GATES**

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**Question****(MCQ)**

$f = (A + B)(A + C)(A + \bar{C})$  is equivalent to  $\rightarrow (A + C \cdot \bar{C})(\bar{A} + B)$   
 $A + (B \cdot C \cdot \bar{C}) = A$   $A \cdot \bar{A} + A \cdot B = \bar{A}B$

$$(A + B) \cdot (A + C) \cdot (A + \bar{C})$$

**A**  $A + BC$

**B**  $A + B\bar{C}$

**C** 0

**D**  $A$



A logic function is given as:

$$f(A, B, C) = \underline{B\bar{C}} \left[ A + \underline{B\bar{C}D} + \bar{B}CD + \bar{A}B\bar{C} + \bar{A}\bar{B}\bar{C} \right]$$

is equivalent to

$$(A + \bar{A}) \cdot (A + B\bar{C})$$

$$\checkmark (A + \underline{B\bar{C}} + \underline{B\bar{C}D} + \bar{B}CD + \bar{A}\bar{B}\bar{C})$$

$$B\bar{C} (A + B\bar{C} + \bar{B}CD + \bar{A}\bar{B}\bar{C})$$

$$= B\bar{C}$$

**A**  $A\bar{B}CD$

**B**  $B\bar{C}$

**C**  $A\bar{B} + B\bar{C} + CD$

**D**  $AB\bar{C}D$

If we have 4-variables in a logic function, the number of non-dual logical functions possible are\_\_\_\_\_.

$$n = 4 - \text{variables} \Rightarrow N = 2^4 = 16 \text{ terms} \rightarrow (2^{16}) \rightarrow \text{boolean function}$$
$$N = 2^n$$

$$2^{2^3} \rightarrow 2^8 \rightarrow \text{dual boolean function}$$

$$\rightarrow M = 2^{16} - 2^8 = 2^8(2^8 - 1)$$
$$= 256 \times 255$$

A logic function

$f(A, B, C) = (A + B)(\bar{B} + C)(A + C)$ , then  $\bar{f}$  will be equal to

**A**  $AB + \bar{B}C$

**B**  $\bar{A}\bar{B} + B\bar{C}$

**C**  $\bar{A}\bar{B} + \bar{A}\bar{C}$

**D**  $AB + AC$



Which of the following statement is true?

**A** Dual function  $f^D$  is always equals to  $f$ . ✗

**B** NAND is self dual in nature. ✗

**C** ✓ NOT is self dual in nature. ✓✓

**D** Number of self dual function with 3-variables is 8.

$$\begin{array}{ccc}
 \text{NAND} & \xleftrightarrow{\text{dual}} & \text{NOR} \\
 \frac{A \cdot B}{\overline{A \cdot B}} & & \frac{A + B}{\overline{A + B}} \\
 \overline{A} & \xleftrightarrow{\text{Dual}} & \overline{A}
 \end{array}$$

$$\begin{aligned}
 2^{2^2} &= 2^4 = 16 \rightarrow \text{self dual function} \\
 2^{2^3} &= 2^8 = 256 \rightarrow \text{total boolean function}
 \end{aligned}$$

Logical function  $f(A, B, C, D) = AB + \bar{A}CD + \bar{B}CD$  is equivalent to



**A**  $AB + \bar{B}C$

**B**  $AB + CD$

**C**  $\bar{A}C + \bar{B}C$

**D**  $AB + B\bar{C}$

A logical function is given as:

$$f(A, B, C) = \bar{A}\bar{B} + \bar{A}BC + \bar{A}B\bar{C}$$

then which of the following statement is true?

$$f(A, B, C) = \bar{A}\bar{B} + \bar{A}BC + \bar{A}B\bar{C} = \bar{A} [\bar{B} + BC + B\bar{C}]$$

$$= \bar{A} [\bar{B} + B(C + \bar{C})]$$

$$= \bar{A} [\bar{B} + B]$$

$$= \bar{A}$$

**A**  $f(A, B, C) = \bar{A}\bar{B} + B\bar{C}$  ✗

**B**  $f(A, B, C) = \bar{A} + \bar{C}$  ✗

**C**  $f(A, B, C)$  is a self dual function ✓

**D** None of the above

$$f(A, B, C) = \bar{A} \checkmark$$

$$f'(A, B, C) = \bar{A}$$



Which of the following is true?


**A**  $\overline{AB} + A\overline{B} = (\overline{A} + \overline{B})(A + B)$

**B**  $\overline{ABCD} = \overline{A} + \overline{B} + \overline{C} + \overline{D}$  ✓✓

**C**  $\overline{A\overline{B}.C} = (A + \overline{C})(\overline{B} + \overline{C})$

**D** None of these

Which of the following is true?

- A** We can use '1' as enable input for OR gate
- B** We can use '0' as enable input for AND gate 
- C** '0' as well as '1' can be used as enable input for XNOR gate
- D** None of the these

Which of the following relation is true?

**A**  $A \oplus \bar{B} = \bar{A} \odot B$

**B**  $\overline{A \oplus \bar{B}} = A \odot B$

**C**  $\overline{\bar{A} \odot \bar{B}} = A \oplus B$

**D**  $\overline{\bar{A} \oplus \bar{B}} = A \oplus B$





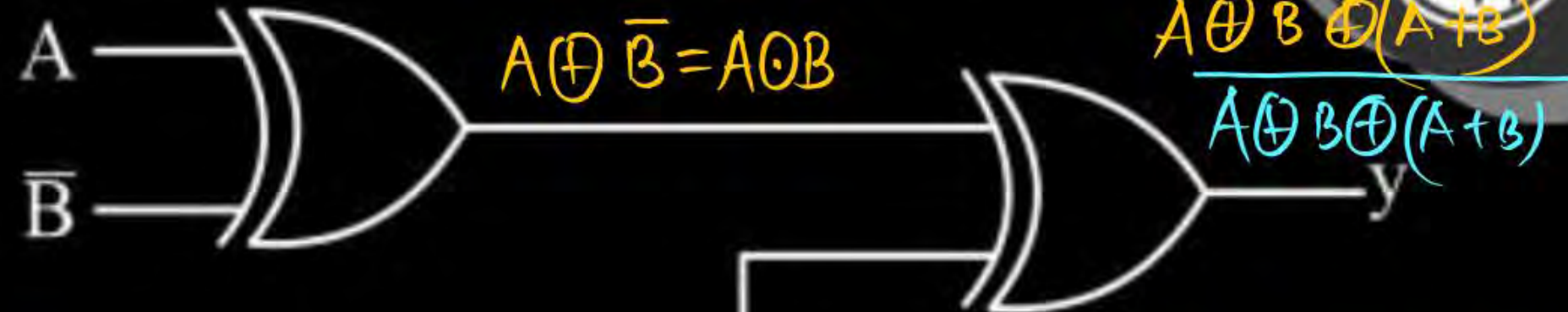
# Question

## (MCQ)



A logical circuit is as given below:

Output  $y$  will be



$$A \oplus B \oplus (A+B) = A \cdot B$$

$$A \oplus B \oplus A \cdot B = (A+B)$$



$$\frac{A \oplus B \oplus (A+B)}{A \oplus B \oplus (A+B)}$$

**A**  $\bar{A} + B$

**B**  $\bar{A} + \bar{B}$

**C**  $A\bar{B}$

**D**  $A + B$

$$A \oplus \bar{B} = A \cup B$$

$$\bar{A} \oplus B = A \cup B$$

$$\frac{A \oplus \bar{B} \oplus (\bar{A} + B)}{A \oplus B \oplus (\bar{A} + B)} = \frac{A \oplus B \oplus (\bar{A} + B)}{A \oplus B \oplus (\bar{A} + B)} = \frac{\bar{A} \cdot B}{\bar{A} + \bar{B}}$$



**Question****(MSQ)** (B, C)

A logic circuit has 4-input & 1-output line as shown:

$$A \oplus B \oplus C \oplus D$$

Output  $y$  is '1' wherever number of zeroes on input side are odd, then output  $y$  can be expressed as:

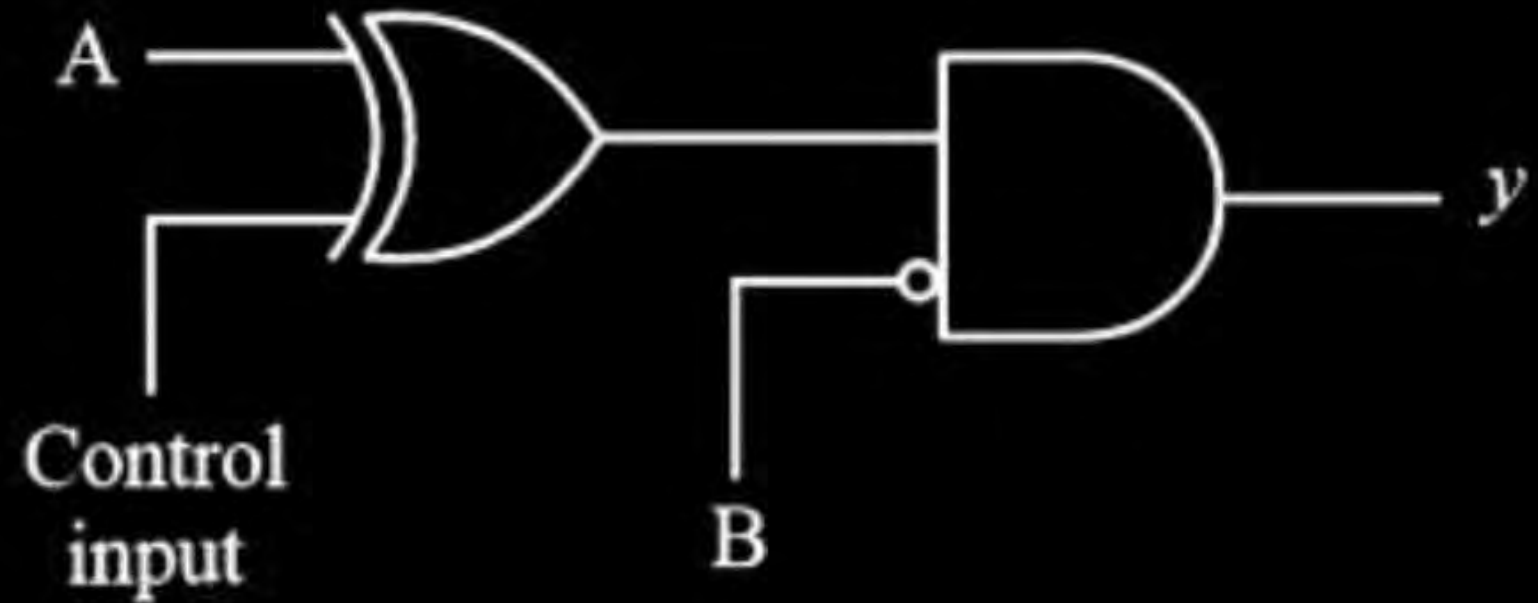
☒ **A**  $A \odot B \odot C \odot D$   
☒ **B**  $\overline{A \odot B \odot C \odot D}$   
☒ **C**  $\overline{A \oplus B \oplus C \oplus D}$   
☐ **D** None of these

Handwritten notes and diagram:
   
 1 zero + 3 - 1's  $\rightarrow 1$ 
  
 3-zeros + 1 - 1's  $\downarrow 1$ 
  
 Input D: 0, 1, 2, 3, 4
   
 $\downarrow (1, 3)$ 
  
 Logic circuit diagram: 4 inputs (A, B, C, D) enter a box labeled "Logic circuit". The output is  $y$ , which is labeled as  $A \oplus B \oplus C \oplus D$ .
   
 Handwritten derivation:
 
$$\overline{A \odot B \odot C \odot D} = A \oplus B \oplus C \oplus D$$

**Question****(MCQ)**

A logic circuit is as given below:

Which of the following is true?



- A** Output y is  $\bar{A}B$  if control input = 0 ✓
- B** Output y is  $\overline{A + B}$  if control input = 1
- C** Output y is  $\overline{A \cdot B}$  if control input = 0
- D** Output y is  $\overline{A \cdot B}$  if control input = 1



**Question****(MCQ)**

A logic circuit is as given below:

Which of the following is true?

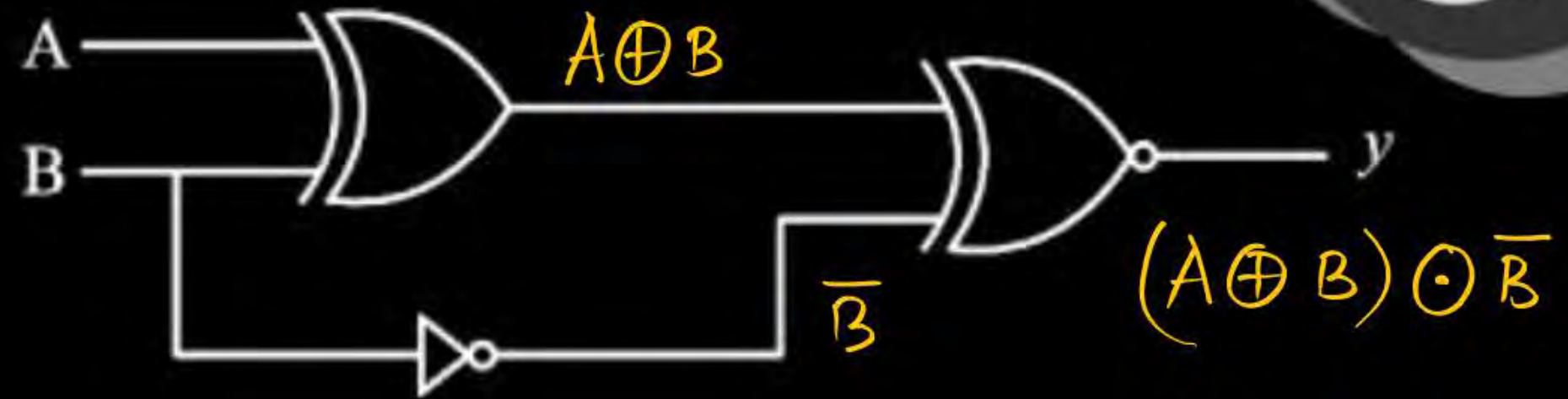


- A** Output is  $\bar{A}$  if  $n$  is even
- B** Output is  $A$  if  $n$  is even
- C** Output is  $\bar{A}$  if  $n$  is odd
- D** Output is  $A$  if  $n$  is odd

**Question****(MCQ)**

A logical circuit is as given below:

Output  $y$  is



$$A \oplus B \oplus \bar{B}$$

$$A \oplus 0$$

$$= A$$

☒ **A**  $A$

☐ **B**  $\bar{B}$

☐ **C**  $\bar{A}$

☐ **D**  $B$

A logical expression is given as:

$$f(A, B, C, D) = \bar{A} + AB[ABC + \bar{B}C + AB\bar{C} + C\bar{D}]$$

$$AB \cdot (AB + \bar{B}C + C\bar{D}) = AB$$

The minimum number of 2-input NAND gate required to implement above logic function will be 2.

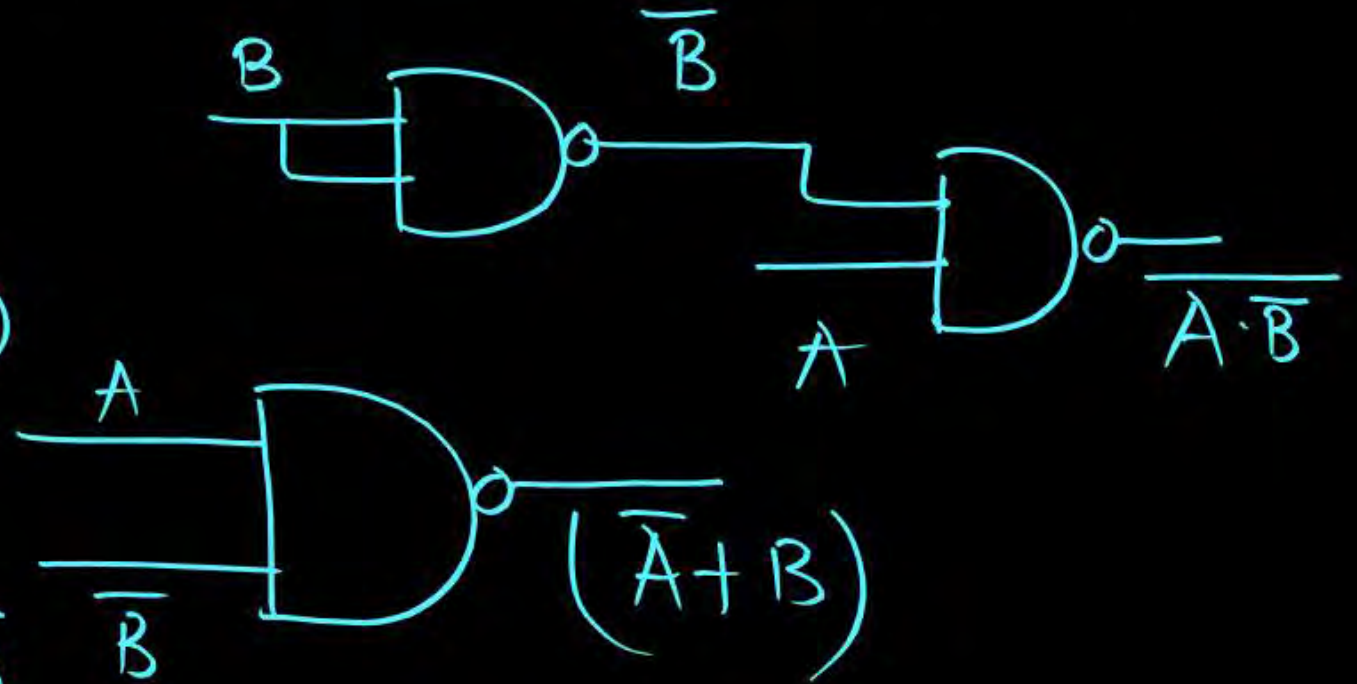
$$= \bar{A} + (AB)$$

$$= (\bar{A} + A)(\bar{A} + B)$$

$$f = \bar{A} + B$$

$$\bar{f} = \overline{\bar{A} + B} = A \cdot \bar{B}$$

$$f = \underline{\underline{A \cdot \bar{B}}} = \underline{\underline{A \cdot P}}$$





A logical expression is given as:

$f(A, B, C) = (\bar{A} + B)(A + \bar{B})$ , the minimum number of 2-input NAND gate required to implement above logical function is 5.

$$= A \odot B$$

$$(\bar{A} + \bar{B})(A + B) = A \oplus B$$

A logical expression is given as:

$f(A, B, C) = \bar{A} + A \cdot BC$  then minimum number of 2-input NAND gate required to implement above logical function is 2.

$$= (\bar{A} + A) \cdot (\bar{A} + BC)$$

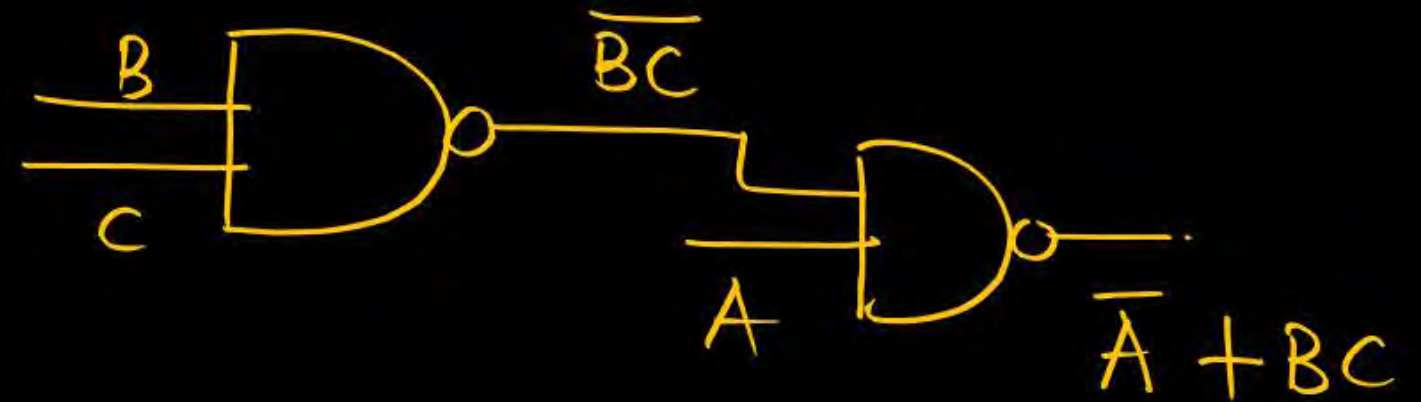
$$\quad \quad \quad \parallel$$

$$\quad \quad \quad (\bar{A} + B) (\bar{A} + C)$$

$$f = \bar{A} + BC$$

$$\bar{f} = A \cdot \overline{BC} = \underline{\underline{A \cdot P}} \Rightarrow 1 \text{ NAND}$$

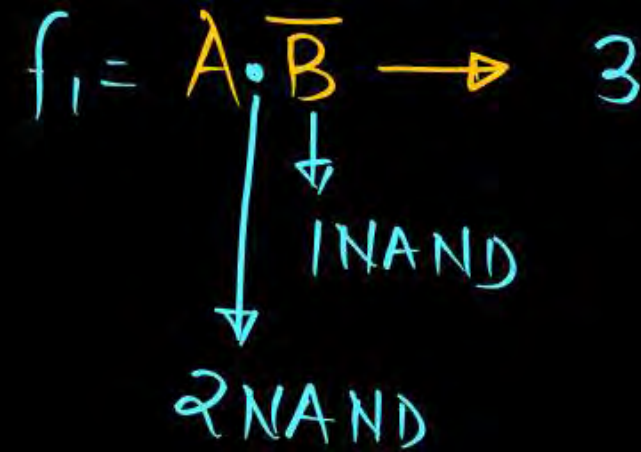
$$P = \overline{BC} \rightarrow 1 \text{ NAND}$$



A logical function is given as:

$f(A, B) = A \oplus (A \cdot \bar{B})$  If we implement this logical function using 2-input NAND gate, the minimum number of NAND gate required is 2.

$$\begin{aligned} & \neq (A \oplus A) \cdot (A \oplus \bar{B}) \\ &= \bar{A} A \bar{B} + A \overline{A \cdot \bar{B}} \\ &= 0 + A (\bar{A} + B) \\ &= A \cdot B \end{aligned}$$





**Thank you**

**GW**  
*Soldiers !*

