

Computer Science & IT

Database Management System



Relational Model & Normal Forms

Lecture No. 08



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Recap of Previous Lecture



Topic

Identification of candidate key w.r.t. FD set

Topic

Membership test

Topic

Relation between two FD sets

Topic

FD set of a sub-relation



Topics to be Covered



Topic

FD set of a sub-relation

Topic

Minimal cover or Canonical cover

H.W.



#Q. Consider a relational schema $R(A, B, C, D, E, F)$ with FD set

$F = \{AB \rightarrow C, B \rightarrow D, BC \rightarrow A, D \rightarrow EF\}$

Find the FD set F_1 for sub-relation $R_1(A, B, C, D)$ of $R(A, B, C, D, E, F)$.

Also find candidate keys for the sub-relation $R_1(A, B, C, D)$.

A	AB	ABC
B	AC	ABD
C	AD	ACD
D	BC	BCD
	BD	
	CD	

$(A)^+ = \{A\}$

$(B)^+ = \{B, D, E, F\}$ $B \rightarrow D$

$(C)^+ = \{C\}$

$(D)^+ = \{D, E, F\}$

$(AB)^+ = \{A, B, C, D, E, F\}$ $AB \rightarrow CD$

$(AC)^+ = \{A, C\}$

$(AD)^+ = \{A, D, E, F\}$

$(BC)^+ = \{B, C, A, D, E, F\}$ $BC \rightarrow AD$

$(BD)^+ = \{B, D, E, F\}$

$(CD)^+ = \{C, D, E, F\}$

$(ACD)^+ = \{A, C, D, E, F\}$

$ABC \rightarrow D$

$ABD \rightarrow C$

$BCD \rightarrow A$

$R_1(A, B, C, D)$

FD set $F_1 = \left\{ \begin{array}{l} B \rightarrow D \\ AB \rightarrow CD \\ BC \rightarrow AD \\ ABC \rightarrow D \\ ABD \rightarrow C \\ BCD \rightarrow A \end{array} \right.$

$(AB)^+ = \{A, B, C, D\}$
all attributes of R_1

$(A)^+ = \{A\}$
 $(B)^+ = \{B, D\}$ } No proper subset is a S.K.

$\therefore \boxed{AB}$ is a C.K.
P.A. = $\{A, B\}$
 \downarrow $BC \rightarrow A$
 \therefore Replace A by BC
BC is S.K. $(B)^+ = \{B, D\}$
 $\therefore \boxed{BC}$ is a C.K. $(C)^+ = \{C\}$
P.A. = $\{A, B, C\}$

$AB \rightarrow C$
 \therefore Replace C by AB




Topic : Minimal cover (Canonical cover)

"irreducible"

- Minimal cover of canonical cover of FD set F is a set of functional dependencies (F_m) such that,
 - $F_m = F$ and
 - F_m does not contain any redundant FD, and
 F_m must not contain any extraneous
attribute at either side of any of its FD

eg. $F = \{ A \rightarrow B, B \rightarrow C, A \rightarrow C \}$



As long as $A \rightarrow B$ & $B \rightarrow C$ are present in FD set F , we don't need to mention " $A \rightarrow C$ " explicitly in the FD set F .

∴ if $A \rightarrow B$ & $B \rightarrow C$ are present then $A \rightarrow C$ is a redundant FD

∴ Minimal Cover of $F = F_{\min} = \{ A \rightarrow B, B \rightarrow C \}$

eg. Let $F = \{ \underline{A} \rightarrow B, AB \rightarrow C \}$

In $AB \rightarrow C$

we know $A \rightarrow B$

i.e. A can determine B ,

\therefore if ' A ' is present, then we don't need B ,

Hence $AB \rightarrow C$

' B ' is L.H.S. of FD is extraneous.

$\therefore AB \rightarrow C$ after removal of extraneous attribute becomes " $A \rightarrow C$ "

Minimal Cover of $F = F_m = \{ A \rightarrow B, A \rightarrow C \}$

$$\alpha \rightarrow \beta$$

$$\alpha = A \cup (\alpha - A)$$

$$F = \left\{ \begin{array}{l} fd_1 \\ fd_2 \\ fd_3 \\ \alpha \rightarrow \beta \\ fd_4 \end{array} \right\} \left\{ \begin{array}{l} \text{if } A \in (\alpha - A)^+ \text{ wrt. } (F - (\alpha \rightarrow \beta)), \text{ then } A \text{ is extra} \\ \text{otherwise } A \text{ is not extraneous.} \end{array} \right.$$



Topic : Testing if an Attribute is Extraneous

To check
extraneous
attribute in LHS
of FD.

Consider a set F of functional dependencies and functional dependency $\alpha \rightarrow \beta$ in F .

Set of attributes

Set of attributes

To test if attribute $A \in \alpha$ is extraneous in α (i.e., Any extraneous attribute in LHS of FD)

1. compute $(\{\alpha\} - \{A\})^+$ using the dependencies in F . Except $\alpha \rightarrow \beta$
2. check if $(\{\alpha\} - A)^+$ contains A ; if it does then, A is extraneous.

Otherwise A is not extraneous.

We can
skip it
&
check for
redundant FDs

To test if attribute $B \in \beta$ is extraneous in β (i.e., Any extraneous attribute in RHS of FD)

1. compute α^+ using only the dependencies in F' , $F' = (F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - B)\}$.
2. check that α^+ contains B ; if it does then, B is extraneous

#e.g., Consider the FD set

$$F = \{A \rightarrow BC, B \rightarrow C\}$$

In $A \rightarrow BC$

(i) check if B is extraneous

$$(A)^+ \text{ wrt } \left\{ \begin{array}{l} B \rightarrow C \equiv F - (A \rightarrow BC) \\ A \rightarrow C \equiv A \rightarrow (BC - B) \end{array} \right\} = \{A, C\}$$

$B \notin (A)^+ \text{ wrt } (F - (A \rightarrow BC)) \cup (A \rightarrow (BC - B)) \therefore B \text{ is not extraneous}$

(ii) Check if 'C' is extraneous.

$$(A)^+ \text{ wrt } \left\{ \begin{array}{l} B \rightarrow C \equiv F - (A \rightarrow BC) \\ A \rightarrow B \equiv A \rightarrow (BC - C) \end{array} \right\} = \{A, B, C\}$$

$C \in (A)^+ \therefore C \text{ is extraneous}$

$$F = \left\{ \begin{array}{l} A \rightarrow B \\ A \rightarrow C \\ B \rightarrow C \end{array} \right\} \leftarrow \text{simplified } A \rightarrow BC$$

Check if $A \rightarrow B$ is redundant
Not redundant

Check if $A \rightarrow C$ is redundant

$$(A)^+ \text{ wrt } F - \{A \rightarrow C\} = \{A, B, C\}$$

\therefore Redundant



Topic : Procedure to obtain minimal cover of FD set

- ✓ 1. Simplify RHS of all FDs (i.e., split the FDs such that RHS contain exactly one attribute)
- ✓ 2. For all FDs find redundant (extraneous) attribute in LHS and remove them *as soon as identified.*
- ✓ 3. Eliminate all redundant FDs
4. Apply Union if needed
5. The result is minimal Cover

#e.g., Consider the following FD set

$F = \{AC \rightarrow G$

$D \rightarrow EG$

$BC \rightarrow D$

$CG \rightarrow BD$

$ACD \rightarrow B$

$CE \rightarrow AG$

$\}$

Find minimal cover of F .

Step 1: Simplify RHS of all FDs

F =

$AC \rightarrow G$

$D \rightarrow E$

$D \rightarrow G$

$BC \rightarrow D$

$CG \rightarrow B$

$CG \rightarrow D$

$ACD \rightarrow B$

$CE \rightarrow A$

$CE \rightarrow G$

check if A is extra

$(C)^+ = \{C\}$ $A \notin (C)^+ \therefore$ Not extra

check if C is extra

$(A)^+ = \{A\}$ $C \notin (A)^+ \therefore$ Not extra

check with B, (C)⁺ = {C}, B \notin (C)⁺

check with C (B)⁺ = {B}, C \notin (B)⁺

is extra

$(C)^+ = \{C\}$

$(G)^+ = \{G\}$

$(A)^+ = \{A\}$ 'CD' together is not extra with A

$(AC)^+ = \{A, C, G, B, D, E\}$ $D \in (AC)^+$

$(C)^+ = \{C\}$ \therefore D is extra if 'ASC' are present

$(E)^+ = \{E\}$

FDs after removal of Extraneous attribute in LHS

~~$AC \rightarrow G$~~ X

$D \rightarrow E$

$D \rightarrow G$

$BC \rightarrow D$

~~$CG \rightarrow B$~~

$CG \rightarrow D$

$AC \rightarrow B$

$CE \rightarrow A$

~~$CE \rightarrow G$~~

Identify Redundant FDs

$(AC)^+ = \{A, C, B, D, E, G\}$

$\therefore AC \rightarrow G$ is Redundant

Remove it

$(D)^+ = \{D, G\}$ E not present

$(D)^+ = \{D, E\}$ G is not present

$(BC)^+ = \{B, C\}$ D not present

$(CG)^+ = \{C, G, D, E, A, B, \dots\}$

$(CG)^+ = \{C, G\}$ B is present

D is not present $\therefore CG \rightarrow B$ is redundant

Present

$(AC)^+ = \{A, C\}$ B is not present

$(CE)^+ = \{C, E, G, D\}$ A is not present

$(CE)^+ = \{C, E, A, B, D, G\}$

G is present

$(CD)^+ = \{C, D, E, G, A\}$
 $A \in (CD)^+$
 is: if we consider 'CD' in LHS, then A will be extraneous in LHS.

If (AC) is present, then D is extraneous

& if (CD) is present, then A is extraneous

We choose any one of the possible options.

Our final minimal Cover may vary with our choice.

\therefore More than one minimal Cover are possible with given FD set.

#e.g., Consider the following FD set

$F = \{AC \rightarrow G$

$D \rightarrow EG$

$BC \rightarrow D$

$CG \rightarrow BD$

$ACD \rightarrow B$

$CE \rightarrow AG$

$\}$

Minimal Cover of F

$D \rightarrow EG$

$BC \rightarrow D$

$CG \rightarrow D$

$AC \rightarrow B$

$CE \rightarrow A$

from previous slide.

Find minimal cover of F.

#e.g., Consider the following FD set

H.W.

$F = \{A \rightarrow BC$

$CD \rightarrow E$

$E \rightarrow C$

$D \rightarrow AEH$

$ABH \rightarrow BD$

$DH \rightarrow BC$

$\}$

Find minimal cover of F.



Topic : NOTE



Minimal cover of FD set F need not be unique, but all minimal cover are logically equivalent.

i.e., if F_{m_1} & F_{m_2} are two minimal covers of FD set F

then we know $F_{m_1} \equiv F$ & $F_{m_2} \equiv F$

$$\therefore \underline{F_{m_1} \equiv F_{m_2}}$$

#e.g., Consider the FD set

$F = \{AB \rightarrow C, B \rightarrow A, A \rightarrow B\}$

Find all minimal covers of F .



2 mins Summary



Topic

FD set of a sub-relation

Topic

Minimal cover or Canonical cover

THANK - YOU