

CS & IT ENGINEERING



THEORY OF COMPUTATION

Grammar

Lecture - 01



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Recap of Previous Lecture



Topic

Mealy machine

????? &

Moore Machine



Topics to be Covered



Topic

Grammar

Topic

??

Topic

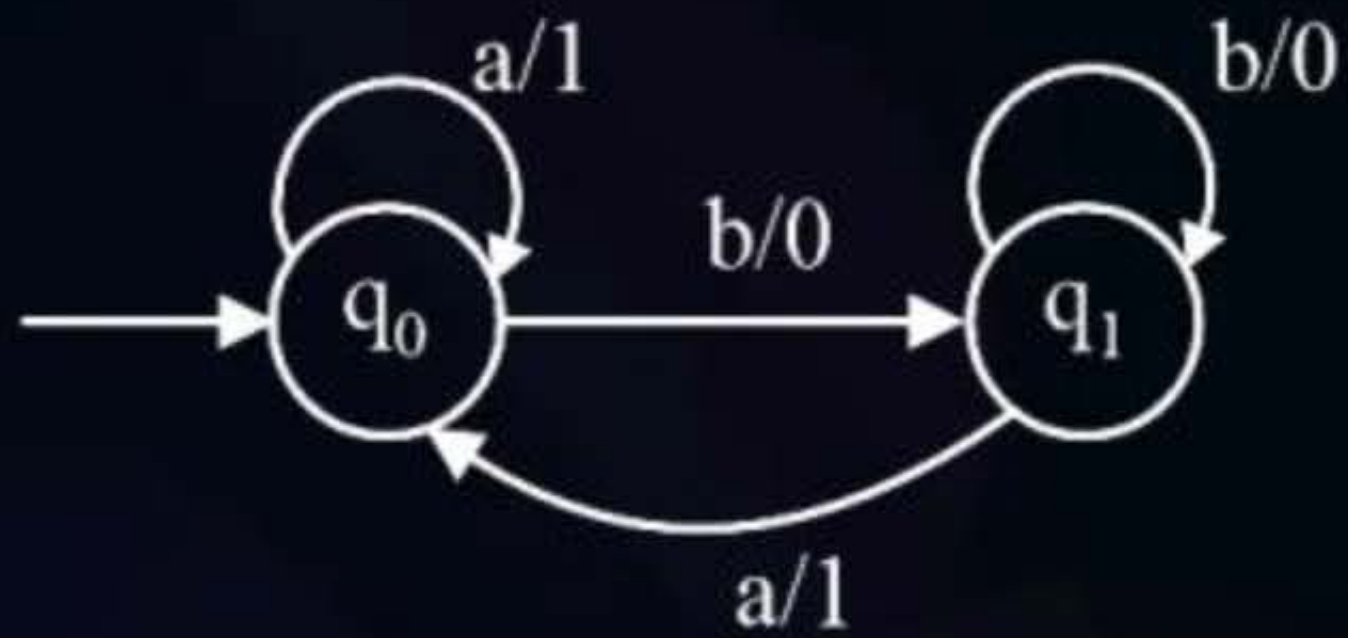
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Topic

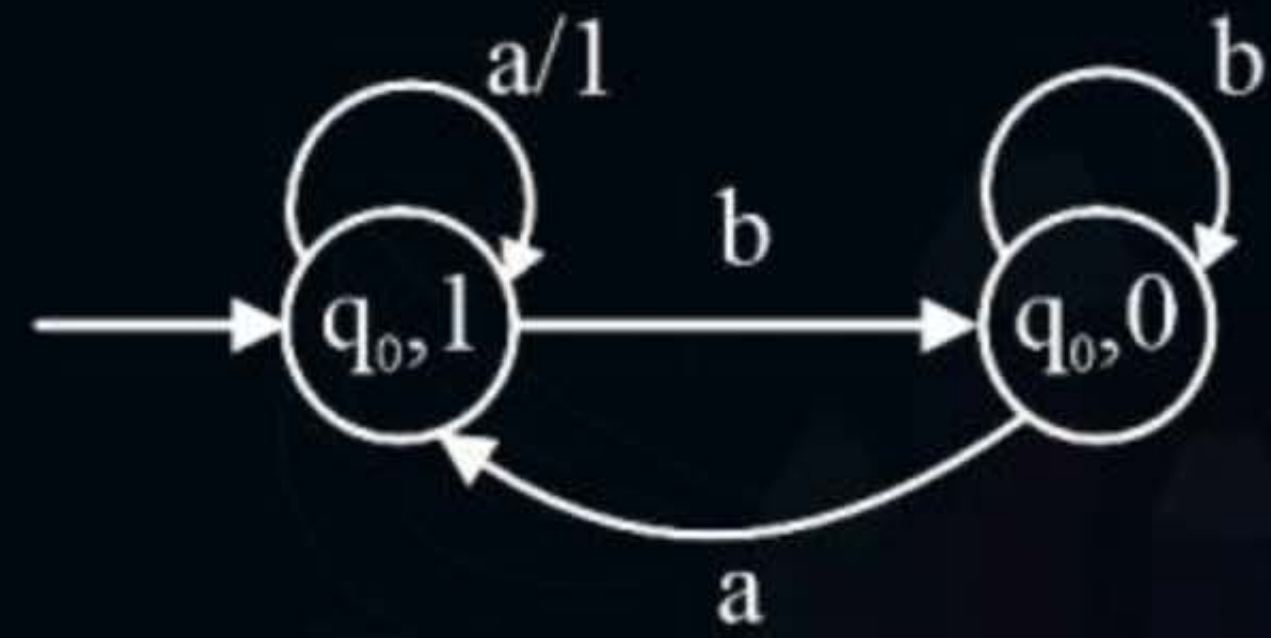
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F.A with output

Mealy Machine



Moore Machine



- Mealy Machine:
- It is a mathematical model in which output is associated
- with transition.

- Moore Machine:
- It is a mathematical model in which output is associated
- with state.

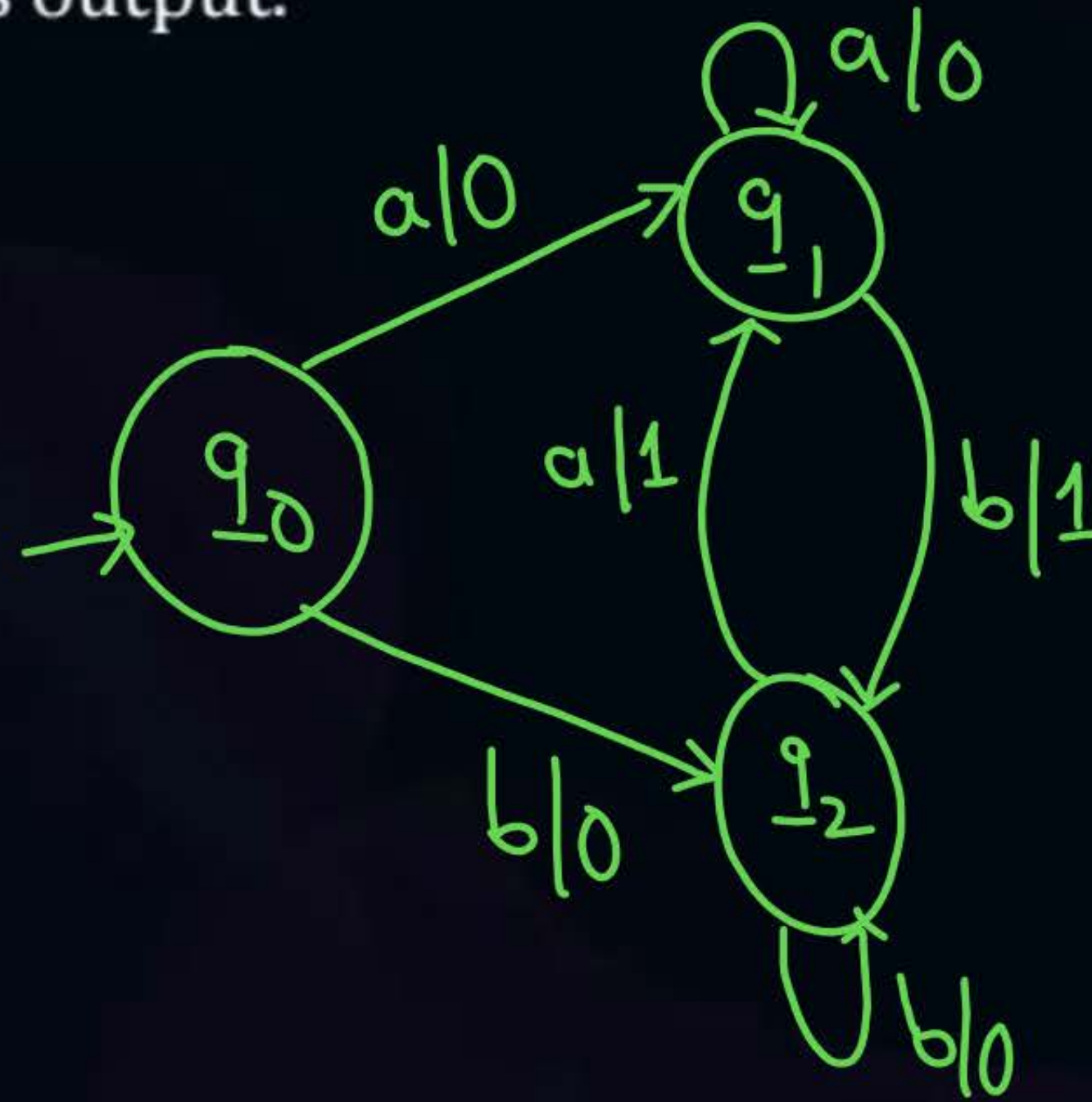
- #Q. Construct mealy machine that takes all strings of a's and b's as input and produces 1 as output if last two symbols in the input are same otherwise produces 0 as output.

[NAT]

$$\Sigma = \{a, b\}$$

$$\Delta = \{0, 1\}$$

#Q. Construct mealy machine that takes all strings of a's and b's as input and produces 1 as output if last two symbols in the input are different otherwise produces 0 as output.



$ab \rightarrow 1$

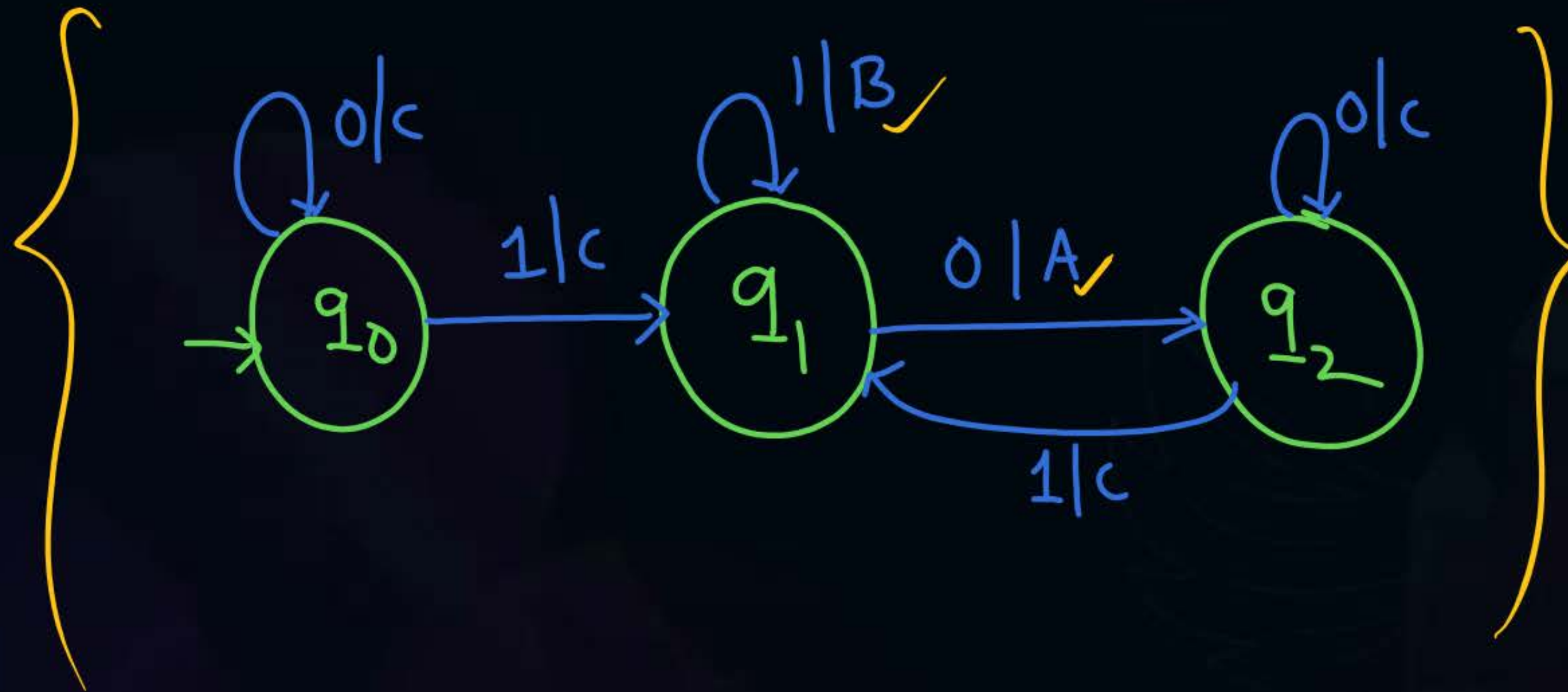
$\left. \begin{array}{l} a \\ b \\ a \\ b \end{array} \right\} 0$

[NAT]

No final State

''''''

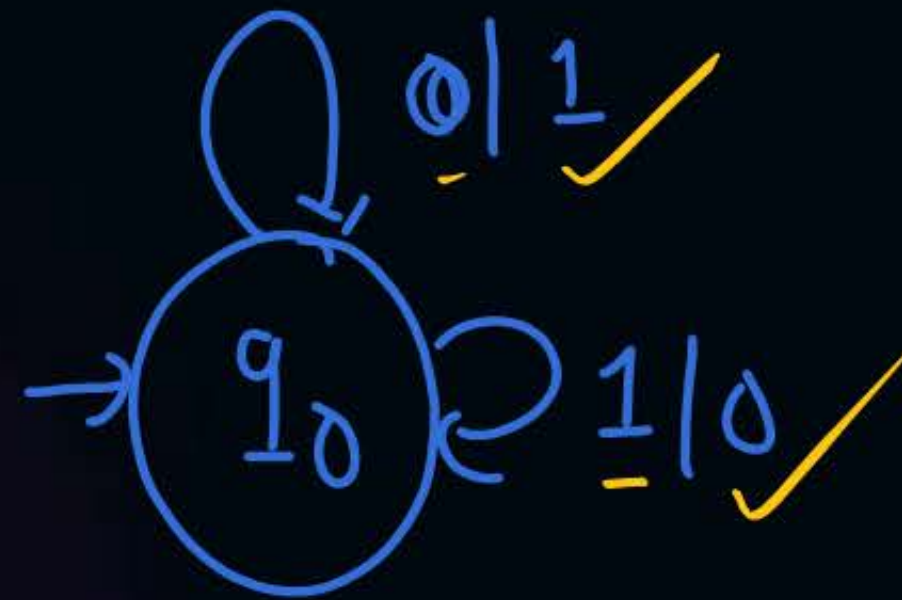
#Q. Construct mealy machine that takes all strings of 0's and 1's as input and produces A as output if input ending with 10 or produces B as output if input ending with 11 otherwise produces output C.



10 → A
 11 → B
 other → C

[NAT]

#Q. Construct mealy machine that produces 1's complement of given binary number as output.



0101
1010

#Q. Construct mealy machine that produces 2's complement of given binary number as output.(assume we are reading string from LSB to MSB)

[NAT]

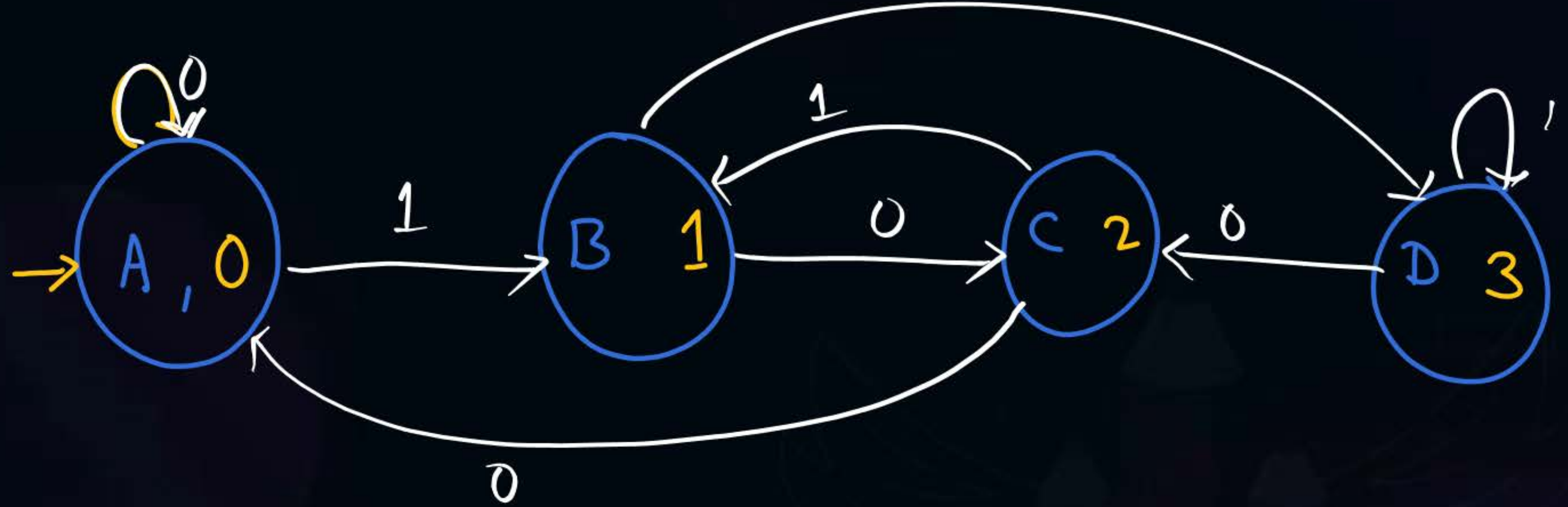


$$\Delta = \{0, 1, 2, 3\}$$

$$\begin{array}{r} 000 \rightarrow 0 \\ 001 \rightarrow 1 \end{array}$$

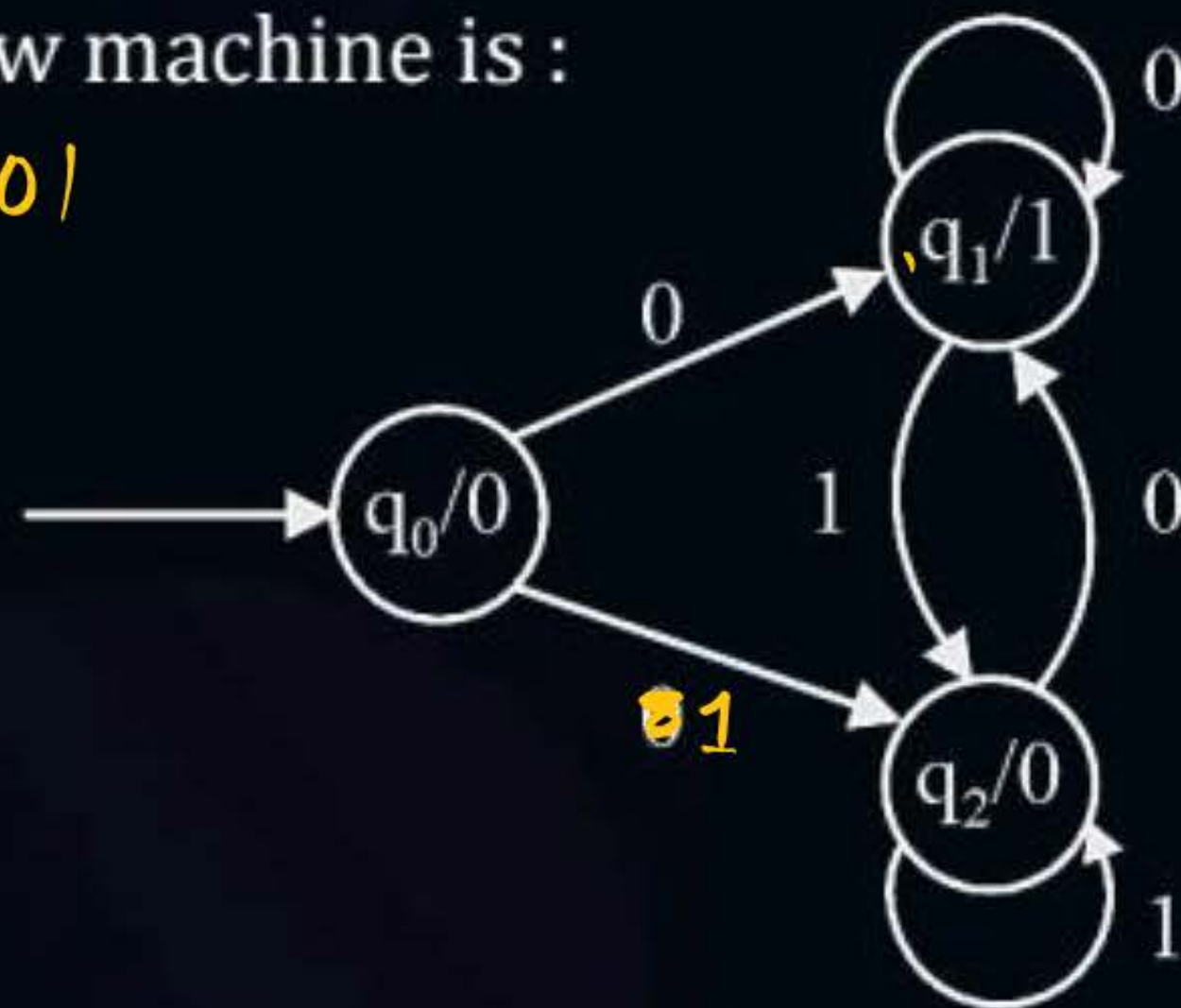
#Q. Construct Moore machine that takes all binary strings as input and produces Residue modulo 4 as output.

	0	1
A	A	B
B	C	D
C	A	B ✓
D	C	D



#Q. The below machine is :

0101



0101
1010

1's Complement

- A A Mealy machine to find 2's complement of a number
- B A Moore machine to find 2's complement of a number
- C A Mealy machine to find 1's complement of a number
- ☒ D A Moore machine to find 1's complement of a number

#Q. A finite state machine with the following state table has a single input x and a single output z .

	Present state $x = 1$	Next state, z $x = 0$
A	D, 0	B, 0
B	B, 1	C, 1
C	B, 2	D, 1
D	B, 1	C, 0

If the initial state is unknown, then the shortest input sequence to reach the final state C is :

A

0 1

B

1 0

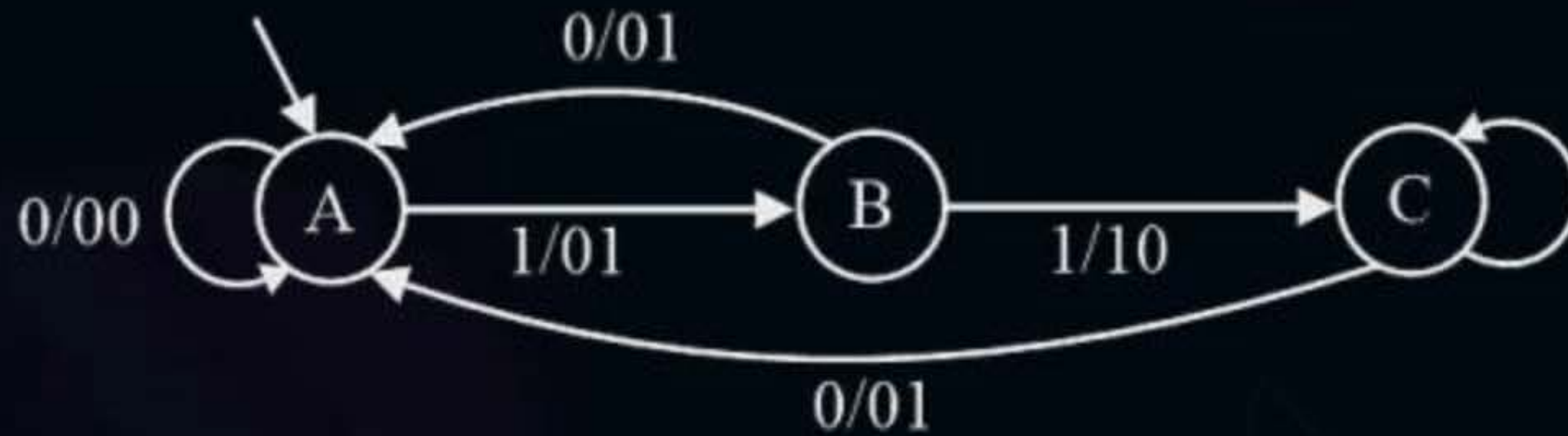
C

1 0 1

D

1 1 0

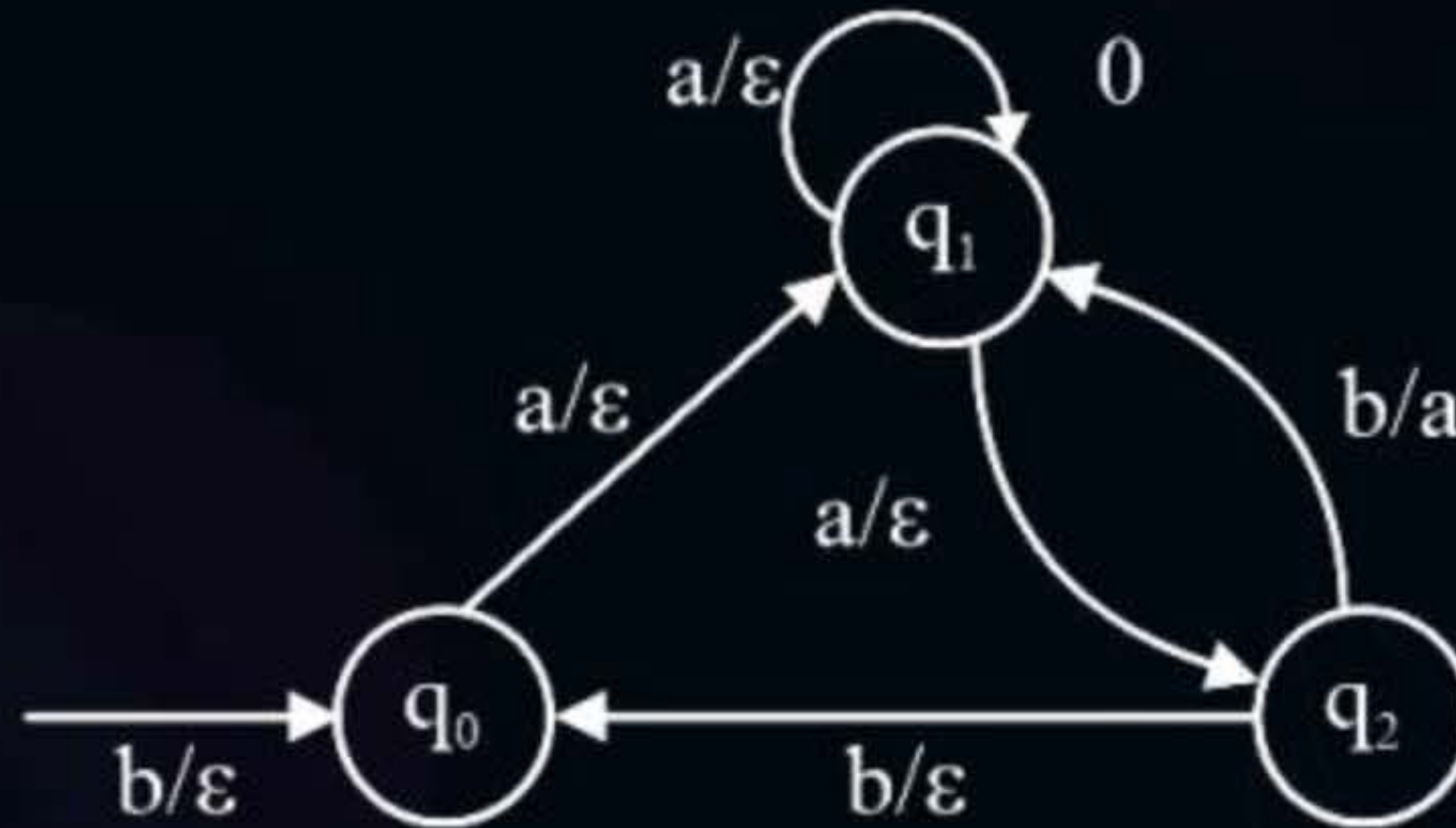
#Q. The Finite state machine described by the following state diagram with A as starting state, where an arc label is x/y and x stands for 1-bit input and y stands for 2-bit output.



- A** Outputs the sum of the present and the previous bits of the input
- B** Outputs a "01" whenever the input sequence contain "11"
- C** Outputs a "00" whenever the input sequence contains "10"
- D** None of the above

[MCQ]

#Q. Consider the following finite state transducer where the label on an edge x/t denotes if the input is x , follow the arrow and emit t



For the input, aabbbaaabbabbabaabb the output is :

A

aaaa

B

aaaaaaaaaa

C

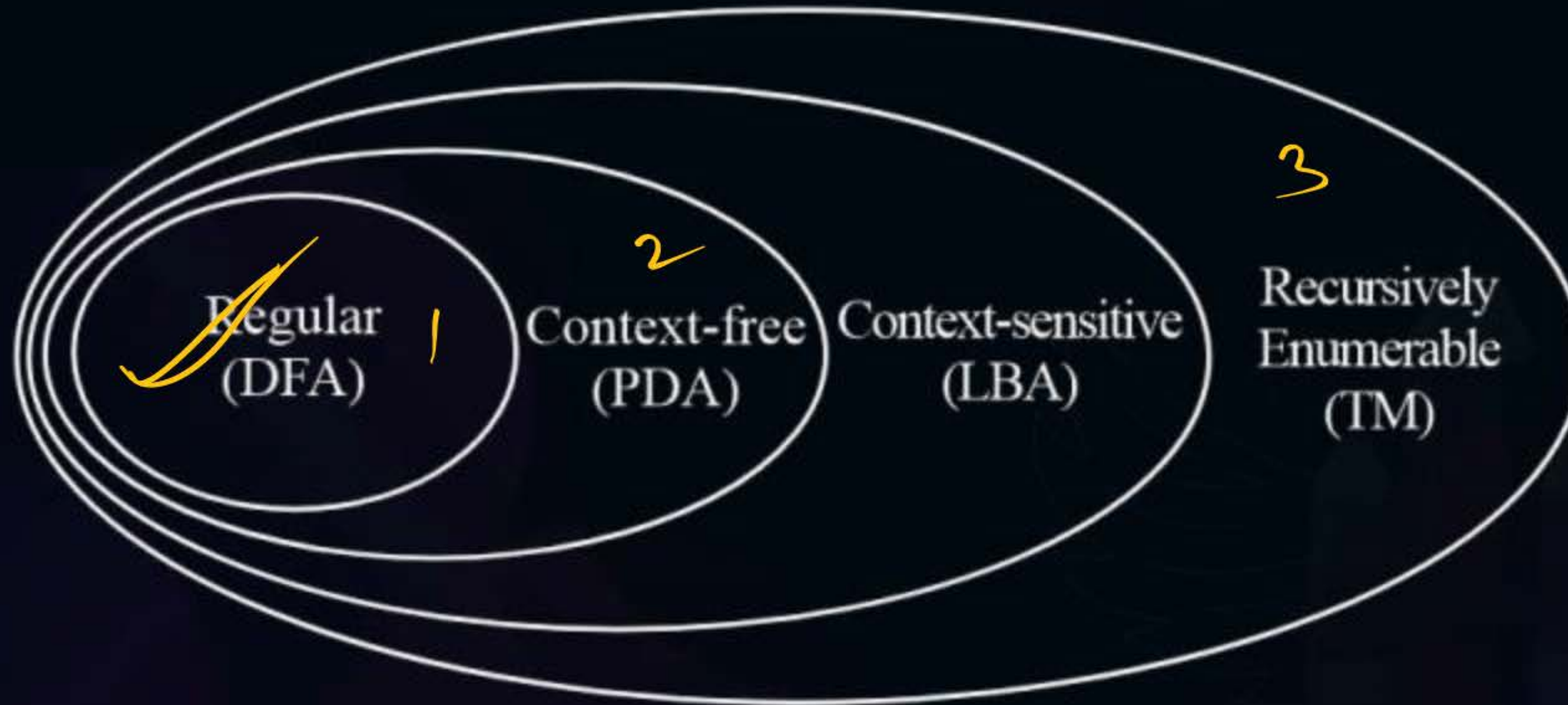
ab ab ab ab

D

abbbabbbbababb



Topic : Regular expression



DFA

NFA

E-NFA

Regular Expressions

Regular Language Detection

closure properties

F.A With o/p

50%



Topic : Grammar

C \rightarrow

java \rightarrow

- Set of rules used to describe strings of a language is known as grammar.
- Formal definition of grammar is

$G = (N, T, P, S)$ $\{S, A, B, C\}$

- **N** :- non terminals (or) variables
- **T** :- Terminals $\rightarrow \{a, d, b\}$
- **P** :- no. of productions $\rightarrow 4$.
- **S** :- Starting symbol

$S \rightarrow ABC - 1$
 $A \rightarrow a|e - 2$
 $B \rightarrow d|a - 2$
 $C \rightarrow b|c - 2$

$\alpha \rightarrow \beta$

$X \rightarrow Y$

7

DF A = Language = Reg Expression

Grammar = Language



Topic : Grammar

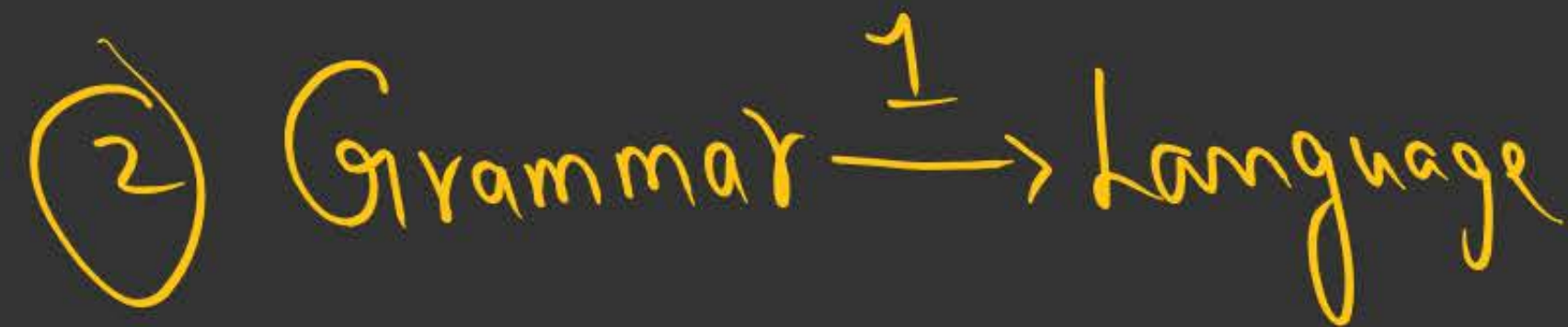
- For every language grammar exists & every grammar generates one language.
- All grammars are of a form $\alpha \rightarrow \beta$, where β is replacement of α

$$L = \{a^n b^n\} \text{ — Grammar}$$

$$\alpha \rightarrow \beta$$

$\alpha = \beta$

For a given language many no. of grammars can be constructed.





Topic : Derivation

- The process of deriving strings from the given grammar known as derivation.
- The derivation can be either left most derivation or right most derivation
- **Left most derivation:**
It is the derivation in which left most non terminal is replaced by its R.H.S part at every step.
- **Right most derivation:**
It is a derivation in which right most non terminal is replaced by its R.H.S part at every step.

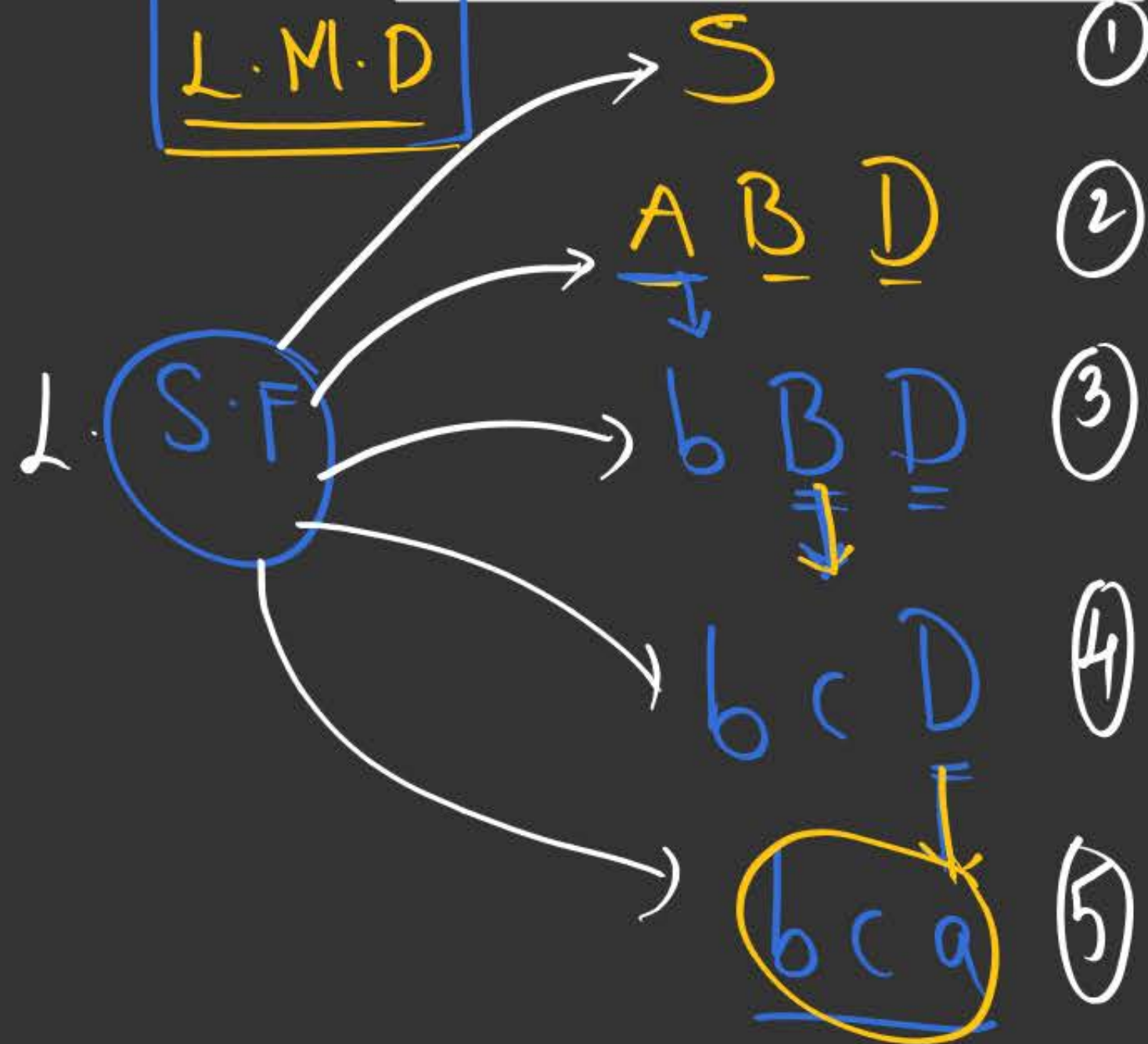
$S \rightarrow ABD$

$A \rightarrow b$

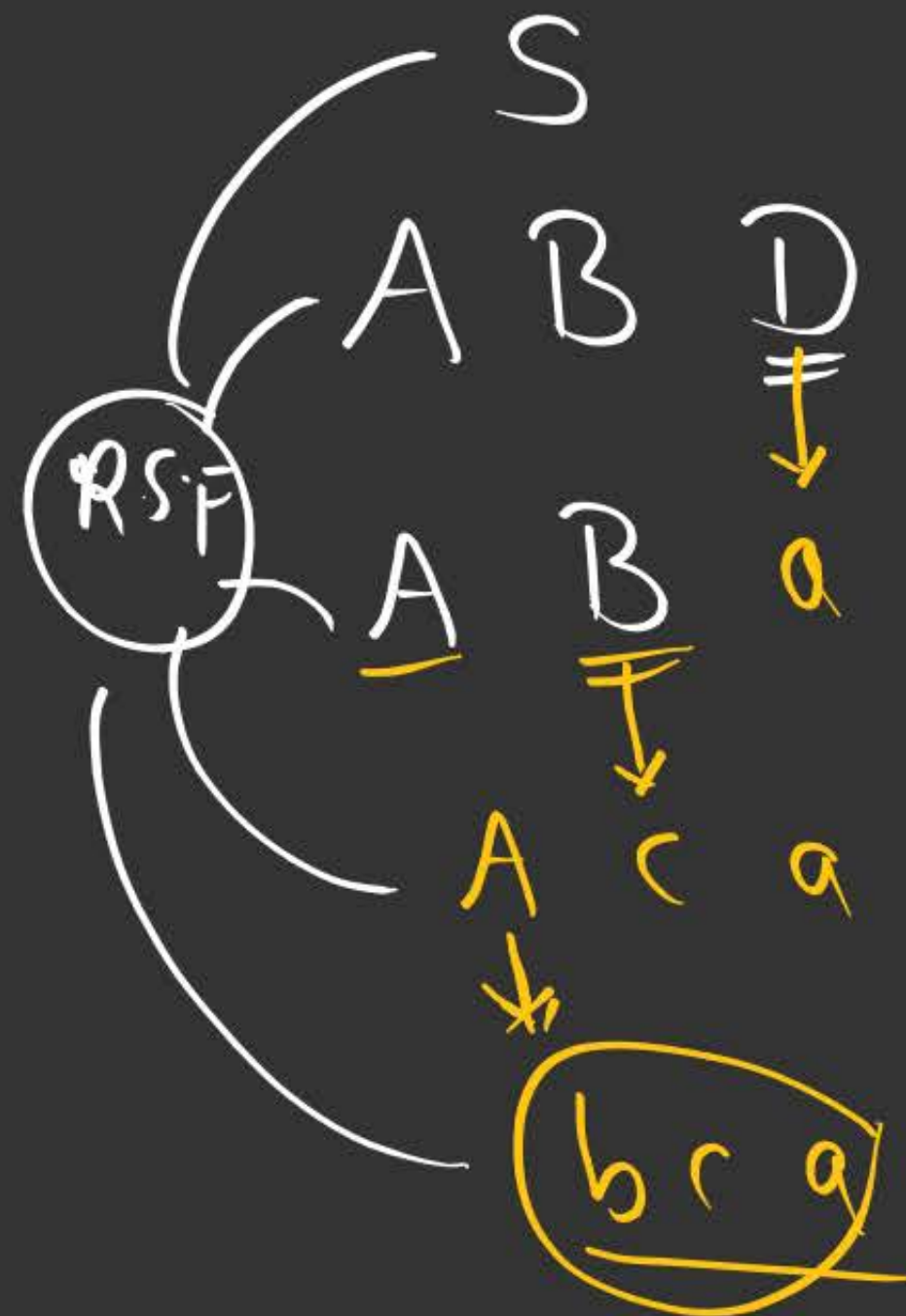
$B \rightarrow c$

$D \rightarrow a$

L.M.D



R.M.D



Parse tree



Derivation Tree (or) Parse Tree

- Tree representation of the derivation is known as derivation tree.
- All leaf node of the parse tree is known as yield of parse tree .
- while reading yield from left to right sentence of the grammar can be generate.

Sentential form

- Each step in the derivation is one sentential form.
- Hence sentential form is combination of terminals & non terminals (sentence also can be included)
- If the derivation is left most then sentential form is left sentential form.
- If the derivation is right most then sentential is right sentential form
- Every grammar represents only one language but for one language more than one grammar may exist.
- For regular languages there exist a grammar known as regular grammar.

- Context free language there exist a grammar known as context free grammar.
- Context sensitive language there exist a grammar known as context sensitive grammar.
- For recursive enumerable language there exist a grammar known as unrestricted grammar.

#Q.

Identify language generated by following grammar.

①

recursive

$$S \rightarrow aS \mid a = \{a, a^2, a^3, \dots\} = a^+$$

$$\begin{array}{c} S \\ | \\ a \end{array}$$
$$\begin{array}{cc} S & \\ / \quad \backslash & \\ a & S \\ & | \\ & a \end{array}$$
$$\begin{array}{ccc} S & & \\ / \quad \backslash & & \\ a & S & \\ & / \quad \backslash & \\ & a & S \\ & & | \\ & & a \end{array}$$

②



= language?

$$\{\epsilon, a, a^2, a^3, \dots\} = a^*$$

S
|
ε

S
/ \
a S
|
ε

③

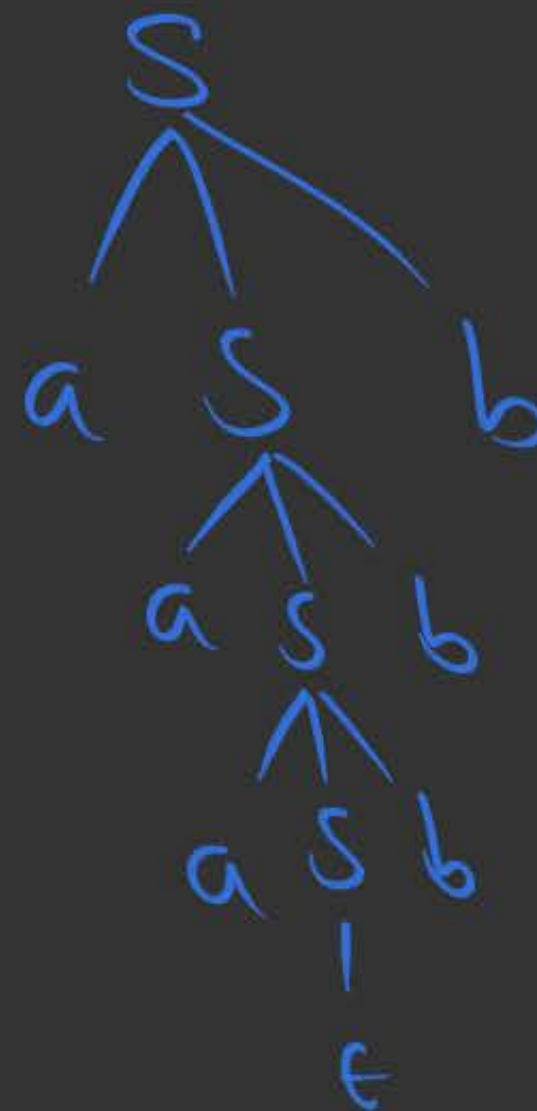
$S \rightarrow aS/bS/\epsilon$ = language? = $(a+b)^*$ ✓

$\{ \epsilon, a, b, a^2, a^3, \dots, a^2 b b, b^2, b^3, \dots, b^2 a^2, \dots \}$



Complete language ✓

④ $S \rightarrow aSb \mid \epsilon$ = language? $\{ \epsilon, ab, a^2b^2, a^3b^3, \dots \}$
 $\{a^n b^n\}$ ✓



⑤ $S \rightarrow AB$ $\left. \begin{array}{l} A \rightarrow aA \mid \epsilon \\ B \rightarrow bB \mid \epsilon \end{array} \right\} \text{Language?}$

$A \rightarrow aA \mid \epsilon \rightarrow a^*$

$B \rightarrow bB \mid \epsilon \rightarrow b^*$

$S = a^*b^*$

⑥ $S \rightarrow a \underline{A} b / b A a \rightarrow \underline{\text{language}} ?$

$A \rightarrow a A / b A / \epsilon \rightarrow (a+b)^*$

$$S = a(a+b)^*b + b(a+b)^*a$$

Starting and ending with different
Symbol.

⑧

$$S \rightarrow aSa / bSb / a / b$$

Language = ?

L = odd length Palindrome

$$\Sigma = \{a, b\}$$

$$L = \left\{ W X W^R \mid \begin{array}{l} W \in (a+b)^* \\ X \in (a+b) \end{array} \right\}$$

⑨

$S \rightarrow AB$

$A \rightarrow \underline{a} \underline{A} \underline{b} \mid \underline{ab}$

$B \rightarrow bB \mid b$

$\{a^n b^n\}$

Language = ?

b^+

$S = a^n b^n b^+$

Non Regular

$L = \{a^n b^m \mid n < m, n, m \geq 1\}$

10

$$S \rightarrow a S d \mid a \boxed{A} d$$

$$A \rightarrow b A c \mid b c = \{ \underline{b^n c^n} \}$$

language ??

$$\underline{a^m d^m b^n c^n}$$

$$L = \{ a^m b^n c^n d^m \mid n, m \geq 1 \}$$

#Q. Construct grammar for the following languages.

$$\textcircled{1} \quad L = a^*$$

$$S \rightarrow \underline{a}S \mid \epsilon$$

2 production

②

$$L = \underline{a}^* \underline{b}^*$$

Grammar = ?

5 productions

$$S \rightarrow AB$$

$$A \rightarrow aA \mid \epsilon$$

$$B \rightarrow bB \mid \epsilon$$

$$\textcircled{3} L = \underline{(a+b)^*}b$$

$$S \rightarrow aS / bS / b$$

$$S \rightarrow Ab$$

$$A \rightarrow aA / bA / \epsilon$$

$$(a+b)^*$$

④

$$L = \{a^n b^m \mid (n+m) \text{ is even}\}$$

$$\underline{(aa)^*} \underline{(bb)^*} + a(aa)^* b(bb)^*$$

10 am

$$\begin{aligned} S &\rightarrow AB \mid aAbB \\ A &\rightarrow aaA \mid \epsilon \\ B &\rightarrow bbB \mid \epsilon \end{aligned}$$

not Regular

$(aa)^*$

$(bb)^*$

Home Work

$$(5) \quad L = \{a^n b^m \mid (n+m) \text{ is odd}\}$$

$$a(aa)^*(bb)^* + (aa)^*b(bb)^*$$

⑥ $L = \{a^n b^{2n} \mid n \geq 1\}$

$$S \rightarrow a S b b \mid a b b$$

$L = \{a^n b^n \mid n \geq 1\}$

$$S \rightarrow a S b \mid a b$$

$$\textcircled{7} \quad L = \{ \underbrace{a^n}_{\cup} \underbrace{b^n}_{\cup} \underbrace{c^m}_{\checkmark} \mid n, m \geq 1 \}$$

$$S \rightarrow AB$$

$$A \rightarrow aAb \mid ab$$

$$B \rightarrow cB \mid c$$

$$\textcircled{N.T} = \{ \underline{S, A, B} \}$$

$$\textcircled{a^n b^n}$$

$$\textcircled{c^m}$$

$$\textcircled{8} \quad L = \{ a^{n+m} b^m c^n \mid n, m \geq 1 \}$$

$$\overline{a^n} a^m b^m c^n$$

$$S \rightarrow aSc \mid aAc$$

$$A \rightarrow aAb \mid ab$$

⑨ $L = \{a^n b^m c^m d^n / n, m \geq 1\}$

$S \rightarrow a S d / a A d$
 $A \rightarrow b A c / b c$

$$(10) \quad L = a(a+b)^* a + b(a+b)^* b + a + b$$

Home Work

Types of Grammar

Type	Language (Grammers)	From of Productions	Accepting Dived
3	Regular	$A \rightarrow aB, A \rightarrow A$	Finite Automaton
2	Context -free	$A \rightarrow \alpha$	Pushdown Automaton
1	Context sensitive	$A \rightarrow \beta$ With $ \alpha \geq \beta $	LBA
0	Unrestricted	$\alpha \rightarrow \beta$	Turing machine

Unrestricted grammar.

Type 0 - Recursively enumerable
grammar ✓

Type 1 - Context -sensitive
grammar ✓

Type 2 - Context-free
grammar (or) grammar ✓

Type 3 - Regular
Grammar/ grammar ✓

① Grammar \rightarrow Language

② Language \rightarrow Grammar Construction.



2 mins Summary



Topic

One

Topic

Two

Topic

Three

Topic

Four

Topic

Five

10 am

THANK - YOU