

In [17]:

```
1 class Graph:
2     def __init__(self, vertices):
3         self.V = vertices
4         self.edges = []
5
6     def add_edge(self, u, v, weight):
7         self.edges.append((u, v, weight))
8
9     def find(self, parent, i):
10        if parent[i] == i:
11            return i
12        return self.find(parent, parent[i])
13
14    def union(self, parent, rank, x, y):
15        xroot = self.find(parent, x)
16        yroot = self.find(parent, y)
17
18        if rank[xroot] < rank[yroot]:
19            parent[xroot] = yroot
20        elif rank[xroot] > rank[yroot]:
21            parent[yroot] = xroot
22        else:
23            parent[yroot] = xroot
24            rank[xroot] += 1
25
26    def kruskal_mst(self):
27        result = []
28
29        # Sort all the edges in non-decreasing order of their weight
30        self.edges = sorted(self.edges, key=lambda edge: edge[2])
31
32        parent = [i for i in range(self.V)]
33        rank = [0] * self.V
34
35        i = 0 # Index used to pick next edge
36        e = 0 # Index used to count edges
37
38        while e < self.V - 1:
39            u, v, weight = self.edges[i]
40            i += 1
41            x = self.find(parent, u)
42            y = self.find(parent, v)
43
44            if x != y:
45                e += 1
46                result.append((u, v, weight))
47                self.union(parent, rank, x, y)
48
49        return result
50
51    # Example usage:
52    g = Graph(5)
53    g.add_edge(0, 1, 2)
54    g.add_edge(0, 3, 6)
55    g.add_edge(1, 2, 3)
56    g.add_edge(1, 3, 8)
57    g.add_edge(1, 4, 5)
```

```
58 g.add_edge(2, 4, 7)
59 g.add_edge(3, 4, 9)
60
61 mst = g.kruskal_mst()
62 print("Edges in the Minimum Spanning Tree:")
63 for u, v, weight in mst:
64     print(f"{u} - {v} : {weight}")
65
66
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73
74
```

Edges in the Minimum Spanning Tree:

0 - 1 : 2

1 - 2 : 3

1 - 4 : 5

0 - 3 : 6

In []:

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