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import random
import numpy as np
import matplotlib.pyplot as plt
import math
from random import shuffle

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#Number of points in two layers
N = 300

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class Net:

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    def __init__(self):
        self.X = self.findPoints(0, 1, N)
        self.V = self.findPoints(-1 / 10, 1 / 10, N)
        self.D = self.getActualOutput(self.X, self.V)

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    #following funtion is to initialize the weights

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    def findWeights(self,rows,column):
        if ( type(rows) is int and type(column) is int):
            W = np.empty((0, (column)))
            for i in range(rows):
                w = self.findPoints(-15, 15, column)
                W = np.vstack((W, w))
            return W
        else:
            print("Provide feasible values for input and output layers' nodes")

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    def findPoints(self,a,b,n): #this function gets the random points

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        x = list()
        for i in range(n):
            temp = random.uniform(a,b)
            x.append(temp)
        return x

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    def getActualOutput(self,X,V): # this fuction will calculate the required output

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        D= list()
        for x,v in zip(X,V):
            d = math.sin(20 * x) + 3 * x + v
            D.append(d)
        return D

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    def Output(self,x,W,A): # this function will calculate the local field and output

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        l= [] # induced local field
        Z = [] # output field
        x = np.array(np.insert(x,0,1)).reshape(1,-1)
        for idx,(a,w) in enumerate(zip(A,W)):
            if (idx is 0):
                u = np.dot(w,x.T)
            else:

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        u = np.insert(u,0,1)
        u = np.dot(w,u.T)
        l.append(np.array(u))
        u = np.array(self.findActivation(a,u))
        Z.append(u)
    return (l,Z)

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def findUpdate(self,x,d,W,no_of_layers,A,rate): # this function will perform the back propogation
    L = no_of_layers
    l, Z = self.Output(x, W, A)
    Delta = 0
    for i in reversed(range(L)):
        if i is (L-1):
            Delta = np.multiply((d - Z[i]), self.findDerivativeActivation(A[i],l[i]))[0] #
        else:
            W_n = np.delete(W[i+1],0,1)
            Delta = np.multiply(np.dot(W_n.T, Delta) , self.findDerivativeActivation(A[i],l[i]))
        if i is 0:
            Z_n = np.insert(np.array([x]), 0, 1).reshape(1,-1)
            Delta = Delta.reshape(1,-1)
            W[i] = W[i] + (rate) * np.dot((Delta).T, (Z_n))
        else:
            Z_n = np.insert(Z[i - 1], 0, 1)
            W[i] = W[i] + (rate) * np.dot((Delta), (Z_n))
    return (W)

```

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def findActivation(self, a, X):# this function will return the activation value
    tanh = np.vectorize(lambda x:math.tanh(x))
    relu = np.vectorize(lambda x:x)
    step = np.vectorize(lambda x:1 if x>=0 else 0)
    sigmoid = np.vectorize(lambda x: (math.exp(x)/ (1 + math.exp(x))))
    if a is 'tanh':
        y = tanh(X)
    elif a is 'relu':
        y = relu(X)
    elif a is 'step':
        y = step(X)
    elif a is 'softmax':
        y = self.softmax(X)
    elif a is 'sigmoid':
        y = sigmoid(X)
    return y

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def softmax_grad(self,s):
    jacobian_m = np.diag(s)
    for i in range(len(jacobian_m)):
        for j in range(len(jacobian_m)):
            if i == j:
                jacobian_m[i][j] = s[i] * (1 - s[i])

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        else:
            jacobian_m[i][j] = -s[i] * s[j]
    return jacobian_m

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def findDerivativeActivation(self,a,Y):# this computes derivative activation
    der_tanh = np.vectorize(lambda x:(1-math.tanh(x)**2))
    der_relu = np.vectorize(lambda x:1)
    sigmoid = np.vectorize(lambda x: (math.exp(x) / (1 + math.exp(x))))
    if a is 'tanh':
        q = der_tanh(Y)
    elif a is 'relu':
        q = der_relu(Y)
    elif a is 'softmax':
        q = self.softmax_grad(Y)
    elif a is 'sigmoid':
        q = (sigmoid(Y) * (1-(sigmoid(Y)**2)))
    return q

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def softmax(self,X):
    return (np.exp(X)/np.sum(np.exp(X)))

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def findOutputVec(self,W,X,A): # this will calculate the output vector
    Y = []
    for x in X:
        _y = self.Output(x,W,A)
        Y.append(y[1])
    return Y

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```

def error(self,D,Y): #This calculates the Mean Squared Error
    MSE = 0
    for d,y in zip(D,Y):
        MSE += (d - y)**2
    return MSE/len(D)

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```

def plot(self,X,D,Y_out): #This will plot the graphs.
    plt.scatter(X, D, color='b',marker='o')
    plt.scatter(X,Y_out,color='r',marker='x')
    plt.xlabel('x cordinate')
    plt.ylabel('y cordinate')
    plt.show()

```

# Following is the main function

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if __name__ == '__main__':
    obj = Net()
    D = obj.D
    X = obj.X
    W_final = []
    # propogating to next layers using forward propogation
    no_of_nodes_hidden = 24

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W1 = obj.findWeights(no_of_nodes_hidden, 2)
W2 = obj.findWeights(1, (no_of_nodes_hidden + 1)) # Ouput layer has one neuron with bias and preceeding
layer has N inputs
W_final.append(W1)
W_final.append(W2)
A = ['tanh','relu']
MSE = [] # to store mean sqaured error
Y = obj.findOutputVec(W_final, X, A)    #Calculating the required output
e = 0.015
epoch = 0
#Following perform back propogation
while True:
    for x,d in zip(X,D):
        W_final = obj.findUpdate(x,d,W_final,no_of_layers=2,A=A, rate=0.01)
    Y = obj.findOutputVec(W_final,X,A)
    mse = obj.error(D,Y)
    print("This is the mean Squared Error",mse," at epoch ", epoch)
    MSE.append(mse)
    epoch += 1
    if ((MSE[epoch - 1] <= e) or (epoch>100)):    #Stop if MSE is less than e
        break
range_epoch = [i for i in range(epoch)] #plots a graph of MSE with respect to the number of epochs.
plt.plot(range_epoch,MSE)
plt.show()
Y = obj.findOutputVec(W_final, X, A)
obj.plot(X,D,Y)
plt.show()

```

THE OUTPUT IS AS FOLLOWS: