

DATA STRUCTURES AND ALGORITHMS

DATA STRUCTURES:

- Organise and store data.
- Each has advantages as well as disadvantages.
- The best data structure depends on the data fed.

ALGORITHM:

- It is the step needed to perform a particular task.
- There can be more than 1 algorithm for a particular task.
 - Many methods of implementation for an algorithm is possible as well.

Big-O-Notation:

- The time complexity is the no. of steps taken by an algorithm to accomplish a task.
- The memory complexity is the amount of memory used by the algorithm for execution.
- Time complexity is the main constraint.
- Time complexity based on the scale of data fed to it.
- $O(1)$, $O(\log n)$, $O(n)$, $O(n \log n)$, $O(n^2)$ – Best to the worst algorithm.
- Big-O-Notation is hardware independent part.

ARRAYS:

- Indices start from 0(zero) and go upto $n-1$, where n is the size of the array.
- The highest valid index is $n-1$ and the index values can't go negative.
- Arrays stored as contiguous block in memory.
- The array can't be resized as the memory gets allocated in a contiguous block.
- Every element occupies the same amount of space in the memory based on the datatype of the array.
- An array objects are stored as the object references in the array, as a result maintaining the uniform size for each element in the array.
- The accessing is thus easier if we know the index.

Bubble Sort:

- As the algorithm progresses, the array gets partition into a sorted partition and an unsorted partition.
- Unsorted index starts from the end of the array. The other iteration variable 'l' goes to is increased as
 $l = \text{size of array} - 1$ – index used to traverse from left to right.
- The first iteration of outer loop fixes max. value

- Bubble sort is an in-place algorithm, and it is $O(n^2)$ time complexity{quadratic}. Algorithm degrades quickly.

Stable vs Unstable Sorts:

- In case of duplicate values, the unstable sort basically yields the position/ relative ordering of the same data is not preserved, thus considered unstable.
- Stable is vice versa case of unstable sort.
- Stable sort helps when dealing with large repository kind of data.
- Relative ordering of duplicate items should be preserved.

Selection Sort:

- Just like bubble sort.
- The largest elements are listed from the end in each iterations finally obtaining an ascending ordered array.
- Repetitive iteration to compare the values in the array. We get the value to be the largest value
- In place algorithm, And $O(n^2)$ algorithm.
- Doesn't require much swapping as bubble sort and is an unstable algorithm.

Insertion Sort:

- This also partitions the array.
- The sorted partition is from front of the array.
- It is actually assumed that 1st element is a sorted one.
- So the sorted partition builds up in forward manner in each iteration.
- Inserted value is compared to that of the already present values in the sorted partition.
- Sorted partition as a whole get the original sorted position based on the criteria satisfied.
- It is an in-place algorithm, is quadratic algorithm but is a stable algorithm.

Shell Sort:

- Variation of insertion sort to reduce runtime.
- Shell starts out using a larger gap value.
- As the algorithm progresses, the gap is reduced.
- By the time it obtains insertion sort, the array would have been partially sorted.
- Gap value chosen can influence the amount of steps taken to sort the algorithm
- Gap is calculated using **Knuth Sequence**: $\frac{3^k - 1}{2}$
- 'k' is based on the length of the array.
- 'k' is taken as $\text{array.length}/2$; which gets divided by 2 again and again to obtain a 'k' value of 1 after which we perform the insertion sort.
- The pre-sorting state takes place with some gap until gap reduces to 1.
- It is an in-place algorithm, Worst case is quadratic time.
- It is an unstable algorithm.

- Reduction in the shifting compared to the insertion sort.
- Also, a bubble sort can also implemented using a shell sort.

Recursive Algorithm:

- A function which calls itself again and again.
- Factorial computation is an example.

Merge Sort:

- Divide and conquer algorithm.
- Splitting is logical, without creating a new array. Indices take care of splitting.
- Recursive algorithm.
- Two phase – Split and merge.
- Splitting phase leads to faster sorting during merging phase.
- Splitting phase:
 - Start with unsorted array
 - Divide array into 2 arrays – the left and right array
 - The splitting goes on for the sub arrays until sorting reaches a 1 element array.
- Merge Phase:
 - Every left/right pair of sibling arrays into a sorted array.
 - From one element to a whole single array.
 - Temporary arrays used for merging.
- It is not an in-place algorithm
- Time complexity $O(n \log n)$ -base 2.
- Stable algorithm

Quick Sort:

- Chooses a pivot element.
- The left half has elements value less than the pivot element value and right is greater than pivot value.
- Recursive operation.
- Pivot is chosen again and again to sort the array.
- In-place algorithm
- Time complexity $O(n \log n)$ -base 2.
- It is an unstable algorithm.
- The worst possible case leads complexity to $O(n^2)$.

Counting Sort:

- Make assumptions about the data.
- No comparisons used.
- Count, no. of occurrences of each value.

- Non-negative values can only be used(integers).
- Values within a specific range.
- Not an in-place algorithm.
- $O(n)$
- Stability with increase of steps.

Radix Sort:

- The data has same radix(no of unique digits) and width.
- Sort based on individual digit or letter.
- Must use a stable sort algorithm at each stage.
- Start at rightmost point.
- Based on least significant digit.
- $O(n)$ is the time complexity.
- Use of stable counting sort algorithm for radix sort.