

Fermat's little theorem: to test given number is prime or not

$$a^{p-1} \equiv 1 \pmod{p}$$

p is the given number

a is an integer < p

ex: Check whether number 5 is prime or not using Fermat's little theorem

p=5

a= 1,2,3,4

apply these numbers to equation

$$1^4 \equiv 1 \pmod{5} \text{ True}$$

$$2^4 \equiv 1 \pmod{5} \text{ True}$$

$$16 \equiv 1 \pmod{5} \text{ True}$$

$$3^4 \equiv 1 \pmod{5} \text{ true}$$

$$4^4 \equiv 1 \pmod{5} \text{ true}$$

The equation of Fermat's little theorem satisfies for all the values of a from (1 to p-1)

Therefore given number 5 is prime

Example 2:

Check the number 6 is prime or not using Fermat's little theorem

Soln:

p=6

a = 1,2,3,4,5

$$a^{p-1} \equiv 1 \pmod{p}$$

$$1^5 \equiv 1 \pmod{6} \text{ True}$$

$$2^5 \equiv 1 \pmod{6} \text{ False} \text{ Therefore given number 6 is not prime}$$

$$3^5 \equiv 1 \pmod{6}$$

$$4^5 \equiv 1 \pmod{6}$$

$$5^5 \equiv 1 \pmod{6}$$