

# CROSSOVER OPERATORS

(1) Single point crossover  $\rightarrow$  X site (cross site)

Parent 1 ( $P_1$ )  $\rightarrow$  1101100

Parent 2 ( $P_2$ )  $\rightarrow$  10101011

Child 1  $\rightarrow C_1 \rightarrow$  11001011

Child 2  $\rightarrow C_2 \rightarrow$  10111100

(2) Two point crossover: (3) Three point crossover ( $N=3$ )

$P_1 \rightarrow$  11011100

$P_2 \rightarrow$  10101011

$C_1 \rightarrow$  11011100

$C_2 \rightarrow$  10011011

$P_1 \rightarrow$  1101110111010

$P_2 \rightarrow$  11001101101

$C_1 \rightarrow$  10001111101

$C_2 \rightarrow$  11110101010

(4) Uniform crossover (involves a Mask chromosome)

$P_1 \rightarrow$  10101101

$P_2 \rightarrow$  11011001

$M \rightarrow$  10110110

$C_1 \rightarrow$  11101101

$C_2 \rightarrow$  10011001

child 1's allele value is  $P_1$ 's if

Corresponding Mask " is 1 and } CHILD 1

$P_2$ 's if " " is 0.

for child 2: assign  $P_1$ 's value if Mask bit = 0

and  $P_2$ 's value if Mask bit = 1

(5) Three parent crossover

$P_1 \rightarrow$  11010110

$P_2 \rightarrow$  10101101

$P_3 \rightarrow$  11101010

child  $\rightarrow$  11101110

\* child =  $P_1$  if  $P_1$  and  $P_2$  are equal @

Corresponding bit position's allele value

\* otherwise assign  $P_3$ 's allele value

to child (offspring)

⑥ Precedence Preservative crossover - Generally applied with Permutation Encoding / representation.

Parent 1  $\rightarrow$  A B C D E F

Parent 2  $\rightarrow$  A C B E F D

select P<sub>id</sub>  $\rightarrow$  1 2 1 1 2 2

Offspring (child)  $\rightarrow$  A C B D E F

⑦ Partially Matched crossover

(P<sub>1</sub>) A = 9 8 4 | 5 6 7 | 1 3 2 10

(P<sub>2</sub>) B = 8 7 1 | 2 3 10 | 9 5 4 6

C<sub>1</sub> = 9 8 4 2 3 10 1 6 5 7

C<sub>2</sub> = 8 10 1 5 6 7 9 2 4 3

⑧ Ordered crossover:

P<sub>1</sub> = 9 8 4 | 5 6 7 | 1 3 2 10

P<sub>2</sub> = 8 7 1 | 2 3 10 | 9 5 4 6

P<sub>2</sub> = 8 H 1 | 2 3 10 | 9 H 4 H

(H  $\rightarrow$  Hole or mapping happens)

Holes filled by sliding next 2nd x site

P<sub>2</sub>  $\rightarrow$  2 3 10 | H H H | 9 4 8 1

child 2 = 2 3 10 5 6 7 9 4 8 1

mul P<sub>1</sub>  $\rightarrow$  9 8 4 | 5 6 7 | 1 H H H

$\rightarrow$  5 6 7 | H H H | 1 9 8 4

$\therefore$  C<sub>1</sub>  $\rightarrow$  5 6 7 | 2 3 10 | 1 9 8 4 //

~~Ordered~~ / ~~Crossover~~ :- cyclic crossover

$P_1 = 9 \ 8 \ 2 \ 1 \ 7 \ 4 \ 5 \ 10 \ 6 \ 3$

$P_2 = 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10$

$C_1 = [9 \ 2 \ 3 \ 1 \ 5 \ 4 \ 7 \ 8 \ 6 \ 10] \otimes$

~~$G_2 = 1 \ 2 \ 3 \ 4 \ 5 \ 6$~~

1 2 3 4 5 6 7 8 9 10

9 8 2 1 7 4 5 10 6 3

$C_2 = [1 \ 8 \ 2 \ 4 \ 7 \ 6 \ 5 \ 10 \ 9 \ 3] \otimes$

(Permutation Encoding)

~~(2 5) 4~~



Dominance, Diploidy, Abeyance

↳ diploidy - pair of chromosomes

dominance - genotype to phenotype mapping.

↳ Previous representations - haploid (cr) single stranded chromosome

Diploid - Genotype carries 'one (cr) more pairs' of

↳ Chromosomes (Homologous chromosomes), each containing information for the same function

↳ Issue of Redundancy / Duplication. Pairs of genes that decode to same fn. (values)?

↳ Consider following diploid structure:-

$\left\{ \begin{array}{l} ABCDE \\ abcde \end{array} \right.$

$A, a \rightarrow$  different characteristics

$\left\{ \begin{array}{l} ABCDE \\ abcde \end{array} \right.$

↳ could be "Eye color" -  $A \rightarrow$  Blue;  $a \rightarrow$  Brown, etc.

But both are not possible @ any time.

↳ Conflict resolved by operator - Dominance.

↳ An allele is dominant if expressed in phenotype.  
assuming 'Caps' are all dominant

dominant  $\leftarrow (A)BCDE$   $\rightarrow ABCDE$   
allele  
recessive  $\leftarrow (a)BCDE$

Dominance/ Rules  
Recessive

$\left\{ \begin{array}{l} Aa \rightarrow A \\ AA \rightarrow A \\ aa \rightarrow a \end{array} \right.$  heterozygous  
homo "

$\therefore$  Dominance is a genotype  $\rightarrow$  phenotype map. fn.

Diploidy  $\rightarrow$  Way for remembering alleles/ combinations

Previously

Dominance  $\rightarrow$  Protect Shield such alleles from harmful selection.

$\hookrightarrow$  Diploidy allows multiple solns (to same problem) to be carried along, however only one soln is expressed.

Hollstein study :- Diploidy + Evolving Dominance

Each binary gene  $\rightarrow$  described by two genes (values)  $\rightarrow$  Modifier and Functional gene.

Functional Gene  $\rightarrow$  0/1 values  $\rightarrow$  decodes to a normal parameter.

Modifier Gene  $\rightarrow$  M/m

Dominance  $\rightarrow$  of 0 if atleast one 'M' allele is present.

$\hookrightarrow$  Two locus scheme evolved to a simpler 1 locus  
- third allele @ each locus

	OM	Om	IM	Im
OM	0	0	0	0
Om	0	0	0	1
IM	0	0	1	1
Im	0	1	1	1

Two locus Dominance Map

Allele values from  $\{0,1,2\}$  set.

2  $\rightarrow$  dominant

1  $\rightarrow$  Recessive

Rules: 2 and 1  $\rightarrow$  1

2 dom 0  
0 dom **1**

	0	1	2
0	0	0	1 <sup>(2)</sup>
1	0	1	1
2	1 <sup>(2)</sup>	1 <sup>1/2</sup>	1 <sup>(2)</sup>

## Selection Schemes

16-3-10

①

↳ Objective of evolving selection methods that reduce stochastic errors of Roulette wheel selection.

↳ few in literature

- ✓ (a) Deterministic Sampling
- (b) Remainder Stochastic Sampling w/o replacement
- ✓ (c) Stochastic <sup>ⓑ</sup> Sampling w/o replacement
- (d) <sup>ⓑ</sup> with replacement
- ✓ (e) <sup>ⓐ</sup> with replacement
- (f) Stochastic tournament (Ranking scheme)

e  $\Leftrightarrow$  Roulette wheel method

c  $\Leftrightarrow$  Expected value model (R3 plan)

(a)  $\rightarrow$  Prob. of selection =  $f_i / \sum f_i$

Ex. No. of Individuals for a string;  $e_i$

$$e_i = p_{\text{select}} \cdot n$$

↳ Each string is allocated copies = integer part of  $e_i$

↳ Population sorted on "fractional part"

↳ Remainders of strings to make population — top of the sorted list.

\* (b) and (d) start similarly to Deterministic Sampling

↳ (Integer part) No. of copies

In (d) — fractional parts of  $e_i$  — determine weights for roulette wheel to fill up the rest of the population.



In (b) - fractional parts - probabilities

Thus if  $e_i = 0.5$

1 sure copy and another with prob 0.5.

(b) Stochastic Tournament - Tournament selection

↳ one of two competing (drawn @ random) or  $\Phi$  is declared winner and inserted in new population  
→ Successive pairs of individuals are drawn using r/w selection.

↳ Gen. observation of good perfo. by  $\Phi$  in most applications

+

critical Events of Interest — not only start soln of  
previous but also those that yield a improved  
objective fn values (local to optimum)



Meta heuristic  $\rightarrow$  Method for solving class of  
Computational problems by combining user given  
heuristics — in the hope of finding an  
(heuristics) efficient / robust procedure.