

Procedure for Testing of Hypothesis

Step 1: Set up null hypothesis H_0

$$H_0: \mu = \mu_0; H_0: \mu_1 > \mu_2; H_0: \sigma_1^2 \neq \sigma_2^2$$

Step 2: Set up Alternative hypothesis H_1 ,
(Decide one tailed or two-tailed)

$$\begin{array}{l} H_0: \mu = \mu_0; H_1: \mu \neq \mu_0 \\ \text{(one population)} \quad (\mu > \mu_0, \mu < \mu_0) \\ H_0: \mu_1 = \mu_2; H_1: \mu_1 \neq \mu_2 \\ \text{(two populations)} \end{array} \left. \begin{array}{l} \\ \\ \end{array} \right\} \begin{array}{l} \text{Two} \\ \text{-Tailed} \end{array}$$

$$\begin{array}{l} H_0: \mu \leq \mu_0 (\geq \mu_0); H_1: \mu > \mu_0 (< \mu_0) \\ \text{(one population)} \\ H_0: \mu_1 \leq \mu_2 (\mu_1 \geq \mu_2); H_1: \mu_1 > \mu_2 (< \mu_2) \\ \text{(two population)} \end{array} \rightarrow \text{one-tailed}$$

Step 3: Level of Significance
 α at 1% (or) 5%

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Step 4: Test statistic

$$\text{Test Statistic} = \frac{\text{Statistic - Value of the parameter under } H_0}{\text{Standard error of the statistic}}$$

For Normal:
(For Large Sample)

$$Z = \frac{t - E(t)}{SE(t)}$$

(OR)

$$|Z| = \frac{t - E(t)}{SE(t)}$$
$$= \frac{|\bar{x} - \mu|}{\frac{\sigma}{\sqrt{n}}}$$

(Statistic)

(χ^2, t, F)
distributions





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Step 5: CONCLUSION:

- If $Z_{cal} < Z_{\alpha}$ (or) $|Z| < Z_{\alpha}$
(Step 4) → Critical value @ α
(Cal)

We say that it is Not Significant

\therefore The Null hypothesis is Accepted.

- If $Z_{cal} > Z_{\alpha}$ (or) $|Z| > Z_{\alpha}$
(Cal)
- We say that it is significant

\therefore The Null hypothesis is Rejected

~o~



Given $\mu = \mu_0 = 200 \text{ ml}$
 $n = 100$
 $\bar{x} = 201.3 \text{ ml}$
 $\sigma = 5 \text{ ml}$

Null Hypothesis: H_0 : The Machine
is functioning
properly
(OR)

$$H_0: \mu = 200$$

Alternate $H_1: \mu \neq 200$ } (Two-tailed
Hypothesis Test)

Level of Significance: $\alpha = 5\%$

Test Statistic:
$$Z = \frac{|\bar{x} - \mu|}{\sigma / \sqrt{n}}$$
$$= \frac{|201.3 - 200|}{5 / \sqrt{100}}$$

$$\therefore Z_{\alpha_1} = 2.6$$

Also, @ $\alpha = 5\%$: $Z_{\alpha} = 1.96$

CONCLUSION:

$$Z_{\alpha_1} > Z_{\alpha}$$

$\Rightarrow H_0$ is REJECTED

\therefore The Machine is NOT Working Properly.

II Given $\mu = \mu_0 = 1.4 \Omega$

Soln: ↗

$$n = 64$$

$$\bar{x} = 1.39 \Omega$$

$$\sigma = 0.02 \Omega$$

H_0 : The mean Resistance of the resistor is 1.4Ω .

$$\Rightarrow H_0 : \mu = \mu_0 = 1.4$$

$$H_1 : \mu \neq \mu_0$$

Los: $\alpha = 5\%$

TEST STATISTIC: $Z = \frac{|\bar{x} - \mu|}{\sigma/\sqrt{n}}$

=

$$Z_{cal} = 4$$

CONCLUSION: $\sigma = 0.02 \Omega$

@ $\alpha = 5\%$ $Z_{\alpha} = 1.96$

$$\therefore \boxed{Z_{cal} > Z_{\alpha}}$$

$\Rightarrow H_0$ is Rejected

\therefore The mean resistance
of the resistor is Not 1.4.

