

characteristics of an algm

unambiguity - instns should be clear & straightfwd

Finiteness - terminate after finite number of steps

Definiteness - steps defined precisely.

IP -

OP -

effectiveness - sufficient basic & infinite length of time

a) $n(n+1) \approx 2000n^2$
 $n^2 + n$ $2000n^2$

same order.

b) $100n^2 \approx 0.01n^3$
 $\underset{2}{1}$ $\underset{3}{1}$

$100n^2 < 0.01n^3$

$$3) \log_2 n \text{ \& } \ln n$$

$$\log_2 n = \frac{\log_e n}{\log_e 2}$$

$$= \frac{\ln n}{\log_e 2}$$

$$\text{i.e., } \ln n = \log_e 2 * \log_2 n$$

$$\text{so, } \ln n \approx \log_2 n$$

same order

$$4) \log_2^2 n \text{ \& } \log_2 n^2$$

$$\log_2 n * \log_2 n \quad 2 \log_2 n$$

$$\log_2 n * \log_2 n \gg 2 \log_2 n \text{ for very large value of } n$$

$$\boxed{\log_2^2 n \gg \log_2 n^2}$$

$$5) 2^{n-1} \text{ \& } 2^n$$

$$\frac{2^n}{2} \text{ \& } 2^n$$

$$\boxed{2^n \rightarrow 2^n} \text{ same}$$

$$6) (n-2)!$$

$$(n-2)!$$

$$5 \log (n+100)^{10}$$

$$\log n^{10}$$

$$2^{2n}$$

$$n^4$$

$$\log n^{10} < n^4 < 2^{2n} < (n-2)!$$

Circular Queue

define N 5

int queue[N]

int front = -1, rear = -1,

void enqueue(int x)

{
if (front == -1 && rear == -1)

{

front = rear = 0

queue[rear] = x,
}

else if ((rear + 1) % N == front)

{

queue is full.
}

else

{

rear = (rear + 1) % N

queue[rear] = x,

void dequeue(int x)

{

if (front == -1 && rear == -1)

{

queue is empty.
}

else if

front

0

front

0 1 2 3 4

2

front

$(rear + 1) \% N =$

$(0 + 1)$

$1 \% 5 =$

$2 = 2$

full

$rear = (0 + 1) \% 5$
 $1 = 0$

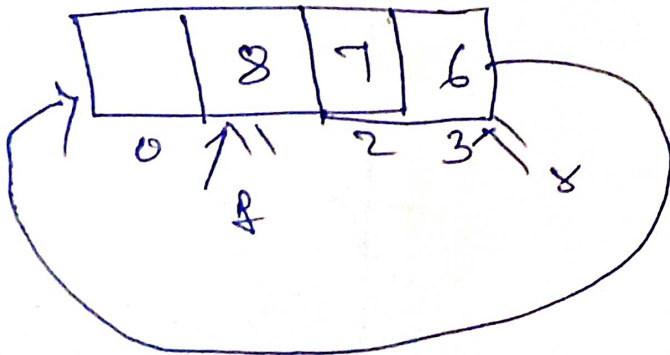
rear = 1

0 1 2 3 4
2 -1 5 6 7
front rear

EnQueue & DeQueue

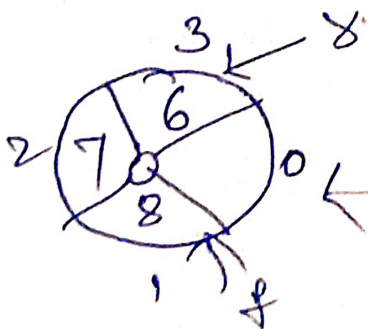
both insertions & deletion can happen in both end.

circular queue



wrap around the queue.

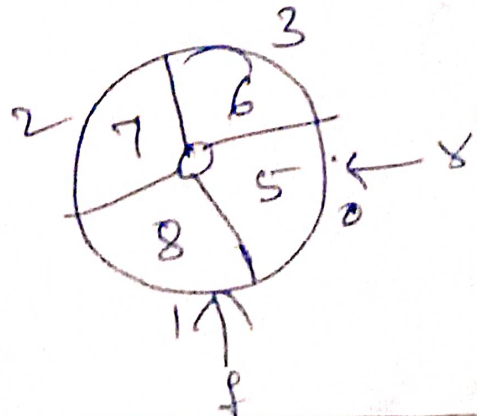
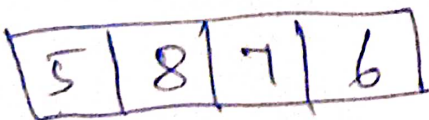
①



$f < r$

~~2007-5-11~~
 $(\text{rear} + 1) \% N$
 $(4 + 1) \% 5$
 $5 \% 5$
 $= 0$

②



$f > r$

algo queue-delete (queue[], front, rear, max, item)

if (front == 0)

{ Print underflow;

}

else { item Queue[front]

if (f == rear)

{ f = 0

}

else if (f == max)

{ f = 1

}

else {

f = f + 1

} exit }

Action	F	R	Queue
Empty	0	0	
insert A, B, C	1	3	
Delete A.	2	3	
insert D, E	2	5	
Delete B, C	4	5	
insert F	4	1	
insert G, H	4	3	
Delete D, E	1	3	
Insert I	1	4	
Delete f	2	4	

⑧ Dequeue

if is empty()

return

else if front == rear

front \leftarrow rear \leftarrow -1

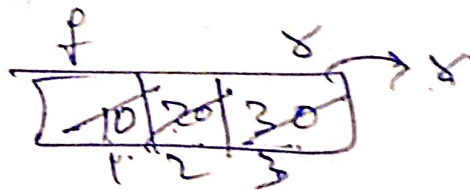
else

front \leftarrow front + 1

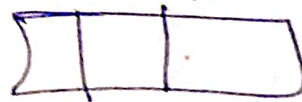
}

⑧

r = 4



f = 4



r = 4

r = 3

r = 4

Peek \rightarrow head of the queue

scullary dequeue

```
void dequeue()
{
```

```
if (f == -1 && r == -1)
{
```

Q is underflow

```
else if (f == r)
```

```
{
```

f = r = -1 // one element

```
else
```

$f = (f + 1) \% N$

$(0 + 1) \% 5$

$1 \% 5$

$=$

$(1 + 1) \% 5$

$2 \% 5$

$\Rightarrow \frac{5(2)}{4} \frac{1}{1.5}$

display

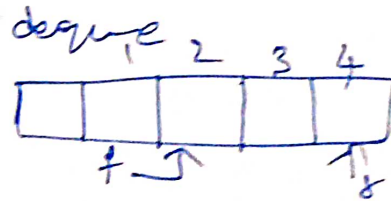
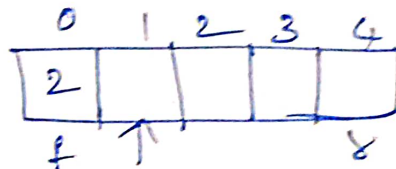
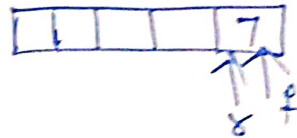
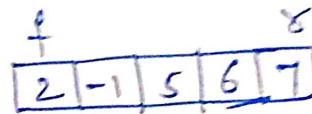
```
while (i != rear)
```

```
{
```

Print (" %d, %d)", i)

$i = (i + 1) \% N$

```
}
```



$$(x-5)!, 2\log(x+200)^{20}, 4^{2n}, 0.001x^4 + 5x^3 + 2$$

$$(x-5)!, \log x^{20}, 4^{2n}, x^4$$

$$\log x^{20} < x^4 < 4^{2n} < (n-2)!$$

$$\underline{\underline{2^n}}$$

if $(n=0)$ return 1

return $f(n-1) + f(n-1)$

$$f(n) = \begin{cases} 0 & \text{if } n=0 \\ 1 + 2f(n-1) & \text{otherwise.} \end{cases}$$

$$f(n) = 1 + 2f(n-1)$$

$$= 1 + 2(1 + 2f(n-2))$$

$$= 1 + 2 + 2^2 f(n-2)$$

$$= 1 + 2 + 2^2 (1 + 2f(n-3))$$

\vdots

$$= 1 + 2 + 2^2 + 2^3 + 2^4 \dots + 2^i f(n-i)$$

$$= 1 + 2 + 2^2 + 2^3 + 2^4 \dots 2^{n-1}$$

$$= \frac{a(x^n - 1)}{x - 1} = \frac{1(2^n - 1)}{2 - 1}$$

$$\boxed{2^n - 1}$$