

* Discrete Mathematics (DM) - Assignment Number - 3

Name:- Kaustubh Shrikant Kabra

Class:- Second Year Engineering

Div:- A

Roll Number:-

Batch:-

Department:- Computer Department

College:- AISSMS's IOIT.

Q-1. The company has 10 members on its board of directors. In how many ways can they elect a president, a vice president, a secretary and a treasurer?

→ One person cannot hold more than 1 position, so, there are 10 member eligible for president, similarly 9 member eligible for vice president, 8 member eligible for secretary and 7

We have to choose 4 member out of 10,

$$\therefore \text{Total number of ways} = {}^{10}P_4 = \frac{10!}{4!} = 10 \times 9 \times 8 \times 7 = \boxed{5040}$$

\therefore There are total 5040 ways in which one can elect a president, a vice president, a secretary, and a treasurer.

Q-2. A box contains 6 white and 5 black balls. Find number of ways 4 balls can be drawn from the box if: i) Two must be white. ii) All of them have same colour.

→ Given:- 6 white ball and 5 black balls
 \therefore Total 11 balls in box.

i) 2 out of 4 must be white.

\therefore Numbers of ways 2 white ball can be drawn from 6 white balls $= {}^6C_2$.

Now 2 white are drawn, 9 balls are remaining in box.

\therefore Number of ways to select 2 remaining balls are $= {}^9C_2$.

\therefore Total number of ways to draw at least 2 white balls $= {}^6C_2 \cdot {}^9C_2$
 $= \frac{6!}{4! \cdot 2!} \cdot \frac{9!}{7! \cdot 2!}$

$$= 15 \times 36$$

$$= \boxed{540}$$

\therefore There are total 540 ways of selecting 4 balls such that 2 must be white.

ii) All 4 have same colour.

There are 2 cases:- 1) All 4 black balls
 2) All 4 white balls.

Number of ways for selecting 4 black balls from 5 $= {}^5C_4 = 5$

Number of ways for selecting 4 white balls from 6 $= {}^6C_4 = 15$.

\therefore $\text{Total number of ways} = 15 + 5 = 20$

There are total 20 ways of selecting 4 balls such that all have same colour.