

Presentation

Data Logic Design

Group Members

- Shahban Iqbal 1421-116033
- Raja Faizan Ali 1421-116032
- Raja Usman 1421-116036
- Usama Hameed 1421-116028

Content:

- Sum of product (SOP)
- Product of sum (POS)
- Standard SOP and POS Forms
- Convert SOP to standard SOP
- Convert POS to Standard POS
- Minterms and Maxterms

Sum of Product

- The sum-of-products (**SOP**) form is a method (or form) of simplifying the Boolean expressions of logic gates.
- Sum and product derived from the symbolic representations of the OR and AND functions.
- OR (+) , AND (.) , addition and multiplication.

$$f(A,B,C) = ABC + A'BC'$$

Sum

Product terms

Product of Sum

- When two or more sum terms are multiplied by a Boolean OR operation.
- Sum terms are defined by using OR operation and the product term is defined by using AND operation.

$$f(A,B,C) = (A' + B) \cdot (B + C')$$

Sum terms

Product

Standard SOP and POS Forms

- The canonical forms are the special cases of SOP and POS forms.
- These are also known as standard SOP and POS forms.

Canonical Form

- In SOP or POS form, all individual terms do not involve all literals.
- For example $AB + A'BC$ the first product term do not contain literal C.
- If each term in SOP or POS contain all literals then the expression is known as standard or canonical form.

Canonical Form

- Each individual term in the POS form is called **Maxterm**.
- Each individual term in the SOP form is called **Minterm**.
- In Minterm, we look for the functions where the output results is “1”.
- while in Maxterm we look for function where the output results is “0”.
- We perform **Sum of minterm** also known as Sum of products (SOP) .
- We perform **Product of Maxterm** also known as Product of sum (POS).

Convert SOP to standard SOP form

Step 1: Find the missing literal in each product term if any.

Step 2: And each product term having missing literals with terms form by ORing the literal and its complement.

Step 3: Expands the term by applying, distributive law and reorder the literals.

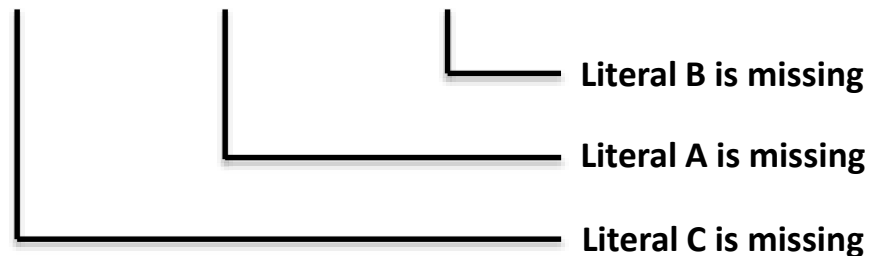
Step 4: Reduce the repeated product terms. Because $A + A = A$ (Theorem 1a).

Example:

$$f(A,B,C) = AB + BC + AC$$

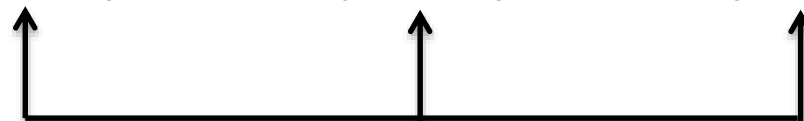
Step 1: Find the missing literals in each product term.

$$f(A,B,C) = AB + BC + AC$$



Step 2: AND the product term with missing literal + its complement.

$$f(A,B,C) = AB \cdot (C+C') + BC \cdot (A+A') + AC \cdot (B+B')$$



Missing literals and their complements


Step 3: Expands the term and reorder the literals.

$$f(A,B,C) = AB \cdot (C+C') + BC \cdot (A+A') + AC \cdot (B+B')$$

Expand & Reorder:

$$ABC + ABC' + ABC + A'BC + ABC + AB'C$$

Step 4: Omit repeated product terms.



A diagram consisting of a horizontal line with two vertical lines extending downwards from its ends, each ending in an arrowhead pointing to the third and fifth terms of the expression below.

$$f(A,B,C)=ABC + ABC' + ABC + A'BC + ABC + AB'C$$

$$f(A,B,C)= ABC + ABC' + A'BC + AB'C$$

Convert POS to standard POS form

Step 1: Find the missing literal in each sum term if any.

Step 2: OR each sum term having missing literals with terms form by ANDing the literal and its complement.

Step 3: Expands the term by applying, distributive law and reorder the literals.

Step 4: Reduce the repeated product terms. Because $A + A = A$ (Theorem 1a).

Example:

$$f(A,B,C) = (A + B) \cdot (B + C) \cdot (A + C)$$

Step 1: Find the missing literals in each sum term.

$$f(A,B,C) = (A + B) \cdot (B + C) \cdot (A + C)$$

Literal B is missing

Literal A is missing

Literal C is missing

Step 2: OR the sum term with missing literal . its complement.

$$f(A,B,C) = (A + B) + (C \cdot C') + (B + C) + (A \cdot A') + (A + C) + (B \cdot B')$$

Missing literals and their complements


Step 3: Expands the term and reorder the literals.

$$f(A,B,C) = (A + B) + (C.C') + (B + C) + (A.A') + (A + C) + (B.B')$$

Expand & Reorder:

$$f(A,B,C) = (A+B+C).(A+B+C').(A+B+C).(A'+B+C).(A+B+C).(A+B'+C)$$

Step 4: Omit repeated sum terms.


$$f(A,B,C) = (A+B+C).(A+B+C').(A+B+C).(A'+B+C).(A+B+C).(A+B'+C)$$
$$f(A,B,C) = (A+B+C).(A+B+C').(A'+B+C).(A+B'+C)$$

Minterms

- Minterms are AND terms with every variable present in either true or complemented form.
- Given that each binary variable may appear normal (e.g., x) or complemented (e.g., x'), there are 2^n m
- Example: Two variables (X and Y) produce $2 \times 2 = 4$ combinations:

XY (both normal)

XY' (X normal, Y complemented)

$X'Y$ (X complemented, Y normal)

$X'Y'$ (both complemented)

Thus there are four minterms of two variables.

Maxterms

- Maxterms are OR terms with every variable in true or complemented form.
- Given that each binary variable may appear normal (e.g., x) or complemented (e.g. x'), there are 2^n maxterms for n variables.
- Example: Two variables (X and Y) produce $2 \times 2 = 4$ combinations:
 - $X+Y$ (both normal)
 - $X+Y'$ (x normal, y complemented)
 - $X'+Y$ (x complemented, y normal)
 - $X'+Y'$ (both complemented)

A	B	C	Minterms	Maxterms
0	0	0	$A'B'C' = m_0$	$A+B+C = M_0$
0	0	1	$A'B'C = m_1$	$A+B+C' = M_1$
0	1	0	$A'BC' = m_2$	$A+B'+C = M_2$
0	1	1	$A'BC = m_3$	$A+B'+C' = M_3$
1	0	0	$AB'C' = m_4$	$A'+B+C = M_4$
1	0	1	$AB'C = m_5$	$A'+B+C' = M_5$
1	1	0	$ABC' = m_6$	$A'+B'+C = M_6$
1	1	1	$ABC = m_7$	$A'+B'+C' = M_7$

Minterms:

$$1. \quad f(A,B,C) = A'B'C' + A'BC' + A'BC + ABC$$

$$= m_0 + m_2 + m_3 + m_7$$

$$= \Sigma m(0,2,3,7)$$

$$2. \quad f(A,B,C) = A'B'C + A'BC + AB'C + ABC$$

$$= m_1 + m_3 + m_5 + m_7$$

$$= \Sigma m(1,3,5,7)$$

$$3. \quad f(A,B,C) = A'B'C' + A'BC' + A'BC + ABC'$$

$$= m_0 + m_2 + m_3 + m_6$$

$$= \Sigma m(0,2,3,6)$$

Maxterms:

$$1. \quad f(A,B,C) = (A+B+C).(A+B'+C).(A+B'+C')+(A'+B'+C')$$

$$= M_0 + M_2 + M_3 + M_7$$

$$= \prod M(0,2,3,7)$$

$$2. \quad f(A,B,C) = (A+B+C').(A+B'+C').(A+B'+C').(A'+B'+C')$$

$$= M_1 + M_3 + M_5 + M_7$$

$$= \prod M(1,3,5,7)$$

$$3. \quad f(A,B,C) = (A+B+C).(A+B'+C).(A+B'+C').(A'+B'+C)$$

$$= M_0 + M_2 + M_3 + M_6$$

$$= \prod M(0,2,3,6)$$