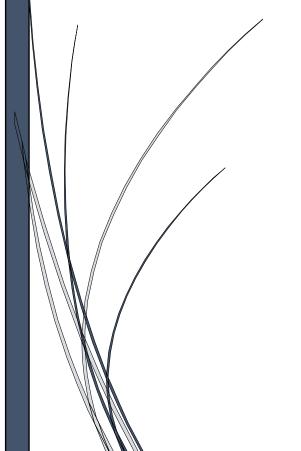
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Individual Assignment: Portfolio Optimization Using Python

BBFE 31382- Computing for Finance



FE/2021/047 - Gamalath K.H.



University of Kelaniya

Faculty of Commerce and Management Studies

Department of Finance

BBFE 31382- Computing for Finance

Individual Assignment: Portfolio Optimization Using Python



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Lecturer/(s): Mr. A.J.P. Samarawickrama

Ms. P. Kethmi

Assignment Topic: Individual Assignment: Portfolio Optimization

Using Python

Student Number and Name:

Student Number	Student Name
FE/2021/047	Gamalath K.H.

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EXECUTIVE SUMMARY

This project implements Modern Portfolio Theory (MPT) to construct an optimized investment portfolio using Python, focusing on risk-adjusted return maximization through Sharpe Ratio analysis. Historical adjusted closing prices for five diversified S&P 500 constituents—JPM, JNJ, DIS, BA, and XOM—were sourced via the yfinance API over a 5-year period. Preprocessing included daily return computation, outlier handling, and exploratory data analysis to establish statistical foundations. Annualized expected returns and the covariance matrix were derived to evaluate inter-asset dependencies and risk dynamics. A single simulated portfolio established baseline metrics for portfolio return and volatility, serving as a precursor to broader stochastic analysis.

A Monte Carlo simulation generated 10,000 random portfolios to construct the efficient frontier, facilitating the identification of both the maximum Sharpe Ratio and minimum volatility portfolios. Subsequently, constrained optimization using Sequential Least Squares Programming (SLSQP) via scipy.optimize was used to refine asset weights under real-world constraints (no short-selling, full capital allocation). The optimized Sharpe-maximizing portfolio delivered an expected annual return of 26.53% with a volatility of 24.72%, while the minimum variance portfolio achieved a lower return of 8.93% at 15.10% volatility. These results demonstrate the robustness of quantitative techniques in portfolio construction and reinforce the trade-off between return-seeking strategies and volatility minimization for different investor risk profiles.

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1 INTRODUCTION

The objective of this project was to apply Modern Portfolio Theory (MPT) using Python [1] to construct an optimal investment portfolio. By analyzing historical data, calculating risk-return metrics, and leveraging optimization techniques, we aimed to identify the best portfolio allocations for different investor profiles.

2 PORTFOLIO CONSTRUCTION OVERVIEW

Five diverse stocks were selected from the S&P 500 index: **JPM**, **JNJ**, **DIS**, **BA**, and **XOM**, representing finance, healthcare, entertainment, aerospace(industrials), and energy sectors respectively. Historical adjusted close prices from May 2020 to May 2025 were collected using the yfinance library, and daily returns were calculated using the .pct_change() [2] method.

3 KEY INSIGHTS FROM MONTE CARLO SIMULATION

A Monte Carlo simulation [3] of 10,000 portfolios was performed, varying the asset weights randomly under the constraint that weights sum to 1. For each portfolio, expected return, volatility, and Sharpe ratio (with a 2% risk-free rate) were calculated. The efficient frontier was visualized, clearly highlighting the trade-off between risk and return.

4 <u>OPTIMIZED PORTFOLIO COMPARISON AND EXPLAIN THE</u> <u>CHARACTERISTICS</u>

Using scipy.optimize [4], two optimized portfolios were derived based on Modern Portfolio Theory principles:

- Maximum Sharpe Ratio Portfolio: Focused on maximizing risk-adjusted return.
- Minimum Variance Portfolio: Aimed to minimize total portfolio risk.

4.1.1 **Summary of Results:**

Portfolio	Expected Return	Volatility (Risk)	Sharpe Ratio
Max Sharpe Ratio	26.53%	24.72%	0.99
Minimum Variance	8.93%	15.10%	0.46

4.1.2 Portfolio Weights:

Stock	Max Sharpe Ratio	Min Variance
JPM	0.00%	0.00%
JNJ	0.00%	10.00%
DIS	0.00%	71.43%
BA	56.95%	9.52%
XOM	43.05%	9.05%

The **Maximum Sharpe Ratio Portfolio** is characterized by its objective to achieve the highest possible risk-adjusted return. It does this by allocating the majority of its capital to highperforming but volatile assets like BA (Boeing) and XOM (ExxonMobil). This results in a higher expected return (26.53%) with higher volatility (24.72%), making it a more aggressive strategy.

The **Minimum Variance Portfolio** seeks to minimize overall portfolio risk regardless of return. It allocates the largest portion of its weight to DIS (Disney), a relatively stable stock, resulting in a much lower volatility (15.10%) and moderate return (8.93%). This strategy reflects a conservative investment approach, prioritizing stability over growth.

5 SUITABILITY FOR INVESTOR TYPES

Each portfolio suits a different investor profile:

- Max Sharpe Ratio Portfolio o Suitable for aggressive investors seeking
 maximum return even at the cost of higher volatility. These investors are willing
 to take on more risk for potentially higher reward, and are likely to have a longer
 investment horizon.
- Minimum Variance Portfolio o Ideal for conservative investors who prioritize capital preservation and lower volatility.
 - This is a good fit for risk-averse individuals or those approaching retirement who value stability and predictable performance.

6 CHALLENGES ENCOUNTERED

Missing or inconsistent data

Used .dropna() to clean the dataset and ensure accurate return calculations.

Understanding annualization formulas

Reviewed lecture slides and used mean * 252 and cov * 252 for annual returns and risk.

Sharpe ratio optimization logic was confusing

Broke it into small functions and referred to documentation for scipy.optimize.

Efficient Frontier plot looked too crowded

Added color gradients and alpha transparency to improve visualization clarity.

Constraint setup in optimization was tricky

Used a lambda function with 'type': 'eq' [5] to ensure weights sum to 1.

7 <u>KEY LEARNINGS</u>

- Learned how to collect and clean real-world financial data using yfinance.
- Understood how to calculate and interpret returns, volatility, and the Sharpe ratio.
- Discovered how optimization can improve investment decisions significantly.
- Gained practical experience in using scipy.optimize for financial problems.
- Realized the importance of diversification and risk management in portfolios.

8 CONCLUSION

Through systematic data analysis, simulation, and optimization, an efficient portfolio was constructed. The practical exposure to tools like yfinance, numpy, pandas, matplotlib [6], and scipy.optimize has enhanced my understanding of portfolio theory and financial computation, preparing me for real-world financial modeling.

9 REFERENCES

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- [4] "Optimization and root finding," The SciPy community, [Online]. Available: https://docs.scipy.org/doc/scipy/reference/optimize.html. [Accessed 17 5 2025].
- [5] "How to Use Python Lambda Functions," DevCademy Media Inc. DBA Real Python, [Online]. Available: https://realpython.com/python-lambda/. [Accessed 17 5 2025].
- [6] "Matplotlib Tutorial," W3Schools, [Online]. Available: https://www.w3schools.com/python/matplotlib_intro.asp. [Accessed 12 5 2025].

10 APPENDIX

10.1 Stock Tickers Used

- **JPM** JPMorgan Chase & Co. (Finance)
- **JNJ** Johnson & Johnson (Healthcare)
- **DIS** Walt Disney Company (Entertainment)
- **BA** Boeing Company (Industrials)
- **XOM** ExxonMobil Corporation (Energy)

10.2 Key Python Libraries Used

- yfinance For downloading historical stock data.
- pandas For data manipulation and analysis.
- numpy For numerical calculations and portfolio metrics.
- matplotlib.pyplot For plotting visualizations.
- scipy.optimize For portfolio optimization using constraints.

10.3 Assumptions

- Trading Days Per Year: 252
- **Risk-Free Rate**: 2% (0.02)
- **Investment Horizon**: 5 years (2020-05-01 to 2025-04-30)
- Short Selling: Not allowed (weights constrained to [0, 1])

10.4 Portfolio Optimization Constraints

- All weights sum to 1: sum(weights) == 1
- No short-selling: weights >= 0 and weights <= 1

10.5 Efficient Frontier Plot Highlights

- Red Dot: Portfolio with maximum Sharpe ratio
- Blue Dot: Portfolio with minimum volatility
- Scatter Points: 10,000 simulated portfolios via Monte Carlo

10.6 Codes

10.6.1 Task 01 # -----# # Task 1: Data Collection & Preprocessing # -----# # Import necessary libraries import yfinance as yf import pandas as pd import numpy as np # Step 1: Select 5 diverse stocks from major stock market index # JPMorgan Chase (JPM)- Financial Sector # Johnson & Johnson (JNJ)- Healthcare Sector # The Walt Disney Company (DIS)- Entertainment Sector # Boeing (BA)- Aerospace Sector # Exxon Mobil (XOM)- Energy Sector tickers = ['JPM', 'JNJ', 'DIS', 'BA', 'XOM'] # Step 2: Download historical stock data (5 years) with auto_adjust=True try: data = yf.download(tickers, start="2020-05-01", end="2025-05-01", auto_adjust=True) except Exception as e:

```
print("Error fetching data:", e)
raise
# Step 3:Directly extract 'Close' prices (already adjusted due to auto_adjust=True)
adj_close = data['Close']
# Step 4: Calculate Daily Returns and drop the first NaN
returns = adj_close.pct_change().dropna()
# Step 5: Display Outputs Nicely print("\n---
Adjusted Close Prices (Last 5 Rows) ---")
display(adj_close.tail())
print("\n--- Daily Returns (Last 5 Rows) ---")
display(returns.tail())
# Step 6: Summary Info print(f"\nAdjusted Close Data
Shape: {adj_close.shape}") print(f"Returns Data Shape:
{returns.shape}") print("\nData Info:")
display(adj_close.info())
print("\nBasic Statistics for Adjusted Close Prices:")
display(adj_close.describe())
10.6.2 Task 02
# -----#
# Task 2: Expected Returns & Risk Calculation
# -----#
import numpy as np
```

```
# Step 1: Calculate Annualized Mean Returns
# 252 trading days per year assumed
mean_returns = returns.mean() * 252
# Step 2: Calculate Annualized Covariance Matrix of returns
cov_matrix = returns.cov() * 252
# Step 3: Simulate a Basic Portfolio with Random Weights (must sum to
1) weights = np.random.random(len(tickers)) weights /= np.sum(weights)
# Step 4: Calculate Expected Portfolio Return & Volatility port_return =
np.dot(weights, mean_returns) port_volatility =
np.sqrt(np.dot(weights.T, np.dot(cov_matrix, weights)))
# Step 5: Display Results in Clean Tables print(" Annualized Mean Returns (%):")
display(mean_returns.to_frame(name='Annualized Mean
Return').style.format("{:.2%}"))
print(" Annualized Covariance Matrix:")
display(cov_matrix.style.format("{:.4f}"))
print(f" Simulated Portfolio Return: {port return:.2%}")
print(f" Simulated Portfolio Volatility: {port_volatility:.2%}")
print("\n Portfolio Weights Used:") for
ticker, weight in zip(tickers, weights):
  print(f" {ticker}: {weight:.2%}")
```

10.6.3 **Task 03**

```
# -----#
# Task 3: Monte Carlo Simulation for Efficient Frontier
# -----#
import numpy as np import
matplotlib.pyplot as plt
# Use previously defined variables from Task 2:
# - mean_returns
# - cov_matrix
# - tickers
# Step 1: Parameters num_portfolios = 10000
risk_free_rate = 0.02 # 2% risk-free rate as per
assignment
# Step 2: Arrays to store simulation results results = np.zeros((3,
num_portfolios)) # Rows: Return, Volatility, Sharpe Ratio weights_record = []
# Step 3: Monte Carlo Simulation Loop
for i in range(num_portfolios):
  # Step 3.1: Generate random weights that sum to 1
weights = np.random.random(len(tickers))
weights /= np.sum(weights)
weights_record.append(weights)
  # Step 3.2: Calculate expected return and volatility for the portfolio
                                                                    port_return =
np.dot(weights, mean_returns) port_volatility = np.sqrt(np.dot(weights.T, np.dot(cov_matrix,
weights)))
```

```
# Step 3.3: Calculate Sharpe Ratio
                                         sharpe_ratio =
(port_return - risk_free_rate) / port_volatility
  # Step 3.4: Store results
results[0, i] = port_return
results[1, i] = port_volatility
results[2, i] = sharpe_ratio
# Step 4: Plotting the Efficient Frontier plt.figure(figsize=(14, 8)) scatter =
plt.scatter(results[1, :], results[0, :], c=results[2, :], cmap='viridis', s=10, alpha=0.5)
plt.colorbar(scatter, label='Sharpe Ratio') plt.title('Monte Carlo Simulation - Efficient
Frontier (10,000 Portfolios)') plt.xlabel('Portfolio Volatility (Risk)') plt.ylabel('Expected
Portfolio Return') plt.grid(True)
# Step 5: Highlight Max Sharpe Ratio Portfolio max sharpe idx = np.argmax(results[2])
plt.scatter(results[1, max_sharpe_idx],
                                              results[0,
                                                             max_sharpe_idx],
                                                                                     c='red',
       s=100,
edgecolors='black', label='Max Sharpe Ratio')
# Step 6: Highlight Min Volatility Portfolio min_vol_idx = np.argmin(results[1])
plt.scatter(results[1, min_vol_idx], results[0,
                                                     min_vol_idx], c='blue',
                                                                                     s=100.
edgecolors='black', label='Min Volatility')
# Step 6.5: Add Efficient Frontier Line
sorted_indices = np.argsort(results[1])
sorted_vol = results[1][sorted_indices]
sorted ret = results[0][sorted indices]
```

```
efficient_vol = []
efficient_ret = []
max_ret_so_far = -np.inf
for vol, ret in zip(sorted_vol, sorted_ret):
if ret > max_ret_so_far:
efficient_vol.append(vol)
efficient_ret.append(ret)
max_ret_so_far = ret
plt.plot(efficient vol, efficient ret, 'r--', linewidth=2.5, label='Efficient Frontier')
plt.legend()
plt.show()
# Step 7: display portfolio details print(f"\nMax Sharpe Ratio
Portfolio
             Metrics:")
                            print(f"
                                             Return:
                                                         {results[0,
                            print(f"
max_sharpe_idx]:.2% }")
                                           Volatility:
                                                         {results[1,
max_sharpe_idx]:.2% }") print(f"
                                       Sharpe Ratio: {results[2,
max_sharpe_idx]:.2f}") print(" Weights:") for ticker, weight in
zip(tickers, weights_record[max_sharpe_idx]):
  print(f" {ticker}: {weight:.2%}")
print(f"\nMin Volatility Portfolio Metrics:")
print(f" Return: {results[0, min_vol_idx]:.2%}")
print(f" Volatility: {results[1,
min_vol_idx]:.2% }") print(f" Sharpe Ratio:
{results[2, min_vol_idx]:.2f}") print(" Weights:")
for ticker, weight in zip(tickers,
weights_record[min_vol_idx]):
  print(f" {ticker}: {weight:.2%}")
```

10.6.4 Task 04

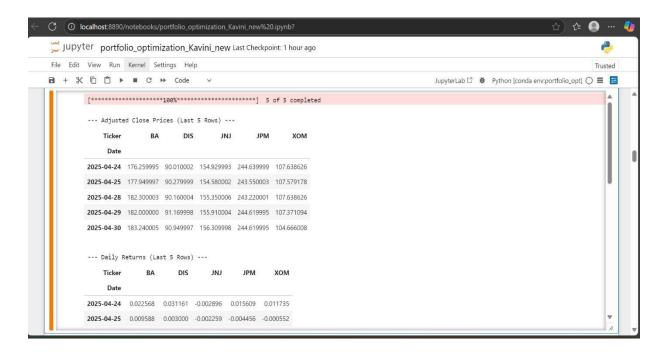
```
# -----#
# Task 4: Portfolio Optimization
# -----#
from scipy.optimize import
minimize import numpy as np
import pandas as pd import
matplotlib.pyplot as plt
# Already defined from Task 1,2 & 3
# tickers, mean_returns, cov_matrix, results
risk_free_rate = 0.02 # 2% risk-free rate
# Step 1: Function to Calculate Portfolio Performance def
portfolio_metrics(weights, mean_returns, cov_matrix, risk_free_rate):
  ret = np.dot(weights, mean_returns)
  vol = np.sqrt(np.dot(weights.T, np.dot(cov_matrix,
weights)))
            sharpe = (ret - risk_free_rate) / vol return ret,
vol, sharpe
# Step 2: Objective Function to Maximize Sharpe Ratio (minimize negative Sharpe)
def neg_sharpe_ratio(weights, mean_returns, cov_matrix, risk_free_rate):
  return -portfolio_metrics(weights, mean_returns, cov_matrix, risk_free_rate)[2]
# Step 3: Objective Function for Minimum Variance Portfolio
def portfolio_volatility(weights, mean_returns, cov_matrix):
  return portfolio_metrics(weights, mean_returns, cov_matrix, 0)[1]
```

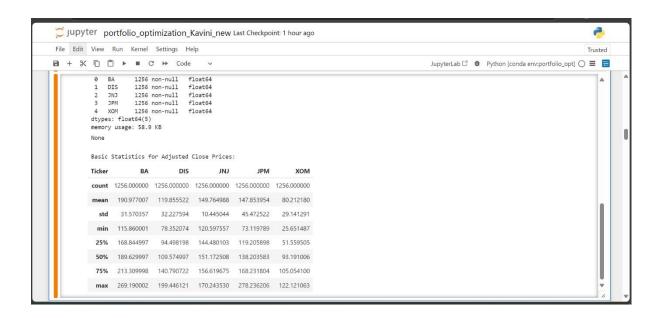
```
# Step 4: Constraints & Bounds constraints = {'type': 'eq', 'fun': lambda x:
np.sum(x) - 1 # Weights must sum to 1 bounds = tuple((0, 1) for in tickers) #
No short selling
# Step 5: Initial Guess (Equal allocation)
init guess = len(tickers) * [1. / len(tickers)]
# Step 6: Optimization for Maximum Sharpe Ratio Portfolio opt_sharpe
= minimize(neg_sharpe_ratio, init_guess,
args=(mean_returns, cov_matrix, risk_free_rate),
method='SLSQP', bounds=bounds, constraints=constraints)
# Step 7: Optimization for Minimum Variance Portfolio opt_min_var =
minimize(portfolio volatility, init guess,
args=(mean_returns, cov_matrix),
                                               method='SLSQP',
bounds=bounds, constraints=constraints)
# Step 8: Get Optimized Metrics
max sharpe return, max sharpe volatility,
                                                  max sharpe ratio
portfolio_metrics(opt_sharpe.x, mean_returns, cov_matrix, risk_free_rate)
min_var_return, min_var_volatility, min_var_sharpe = portfolio_metrics(opt_min_var.x,
mean_returns, cov_matrix, risk_free_rate)
# Step 9: Display Optimized Portfolios
comparison_df = pd.DataFrame({
  'Stock': tickers,
  'Max Sharpe Ratio Weights': opt_sharpe.x,
  'Min Variance Weights': opt_min_var.x
})
portfolio_summary = pd.DataFrame({
  'Portfolio': ['Max Sharpe Ratio', 'Min Variance'],
```

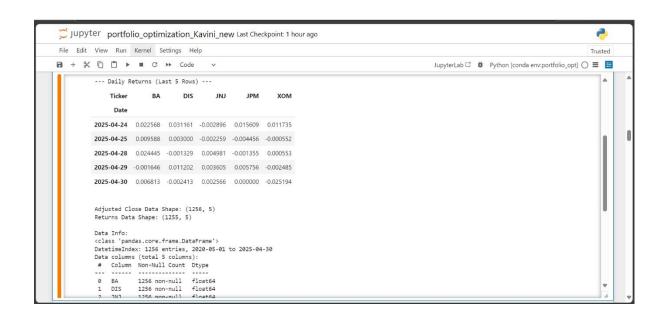
```
'Expected Return': [max_sharpe_return, min_var_return],
  'Volatility': [max_sharpe_volatility, min_var_volatility],
  'Sharpe Ratio': [max_sharpe_ratio, min_var_sharpe]
})
# Step 10: Display Optimized Portfolios
Table print("\nOptimized Portfolio
Allocations:")
display(comparison_df.style.format({
                                         'Max
Sharpe Ratio Weights': "{:.2%}",
  'Min Variance Weights': "{:.2%}"
}))
# Step 11: Display Portfolio Performance Summary Table
print("\nPortfolio Performance Summary:")
display(portfolio_summary.style.format({
  'Expected Return': "{:.2%}",
  'Volatility': "{:.2%}",
  'Sharpe Ratio': "{:.2f}"
}))
# Step 12: Plot Efficient Frontier and mark optimized points plt.figure(figsize=(12,
8)) plt.scatter(results[1, :], results[0, :], c=results[2, :], cmap='viridis', s=10,
alpha=0.5) plt.colorbar(label='Sharpe Ratio')
plt.scatter(max_sharpe_volatility, max_sharpe_return, c='red', s=100, edgecolors='black',
label='Max Sharpe Ratio')
plt.scatter(min_var_volatility, min_var_return, c='blue', s=100, edgecolors='black', label='Min
Variance') plt.xlabel('Volatility (Risk)') plt.ylabel('Expected Return') plt.title('Optimized
Portfolios on Efficient Frontier') plt.legend() plt.grid(True) plt.show()
```

10.7 Outputs (Screenshots)

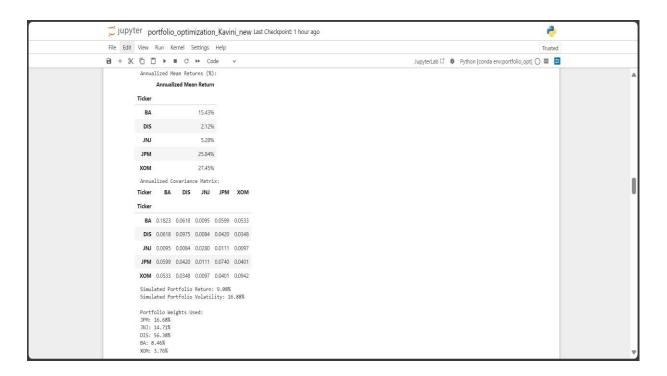
10.7.1 **Task 01**





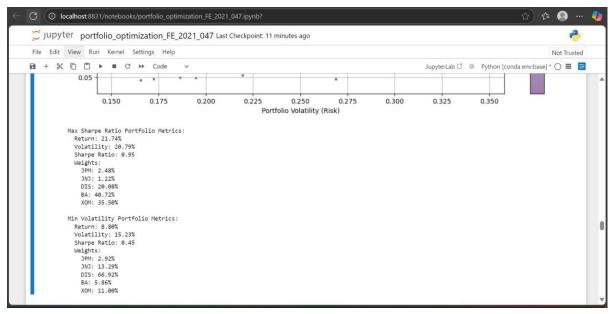


10.7.2 Task 02



10.7.3 **Task 03**





10.7.4 Task 04

