LAB 4 - CLASSIFICATION (DECISION TREE)

SUBMITTED BY:

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LAB OVERVIEW:

Perform Classification using Decision Trees.

Demonstrate Multiple Datasets, do the necessary EDA and show various evaluation metrics.

PROBLEM DEFINITION:

To import multiple datasets and perform various exploratory data analysis on it. Split the dataset into train and test. Perform Classification using Decision Trees and evaluate the model.

APPROACH:

Use Pandas to Import the Datasets.

Performing necessary Exploratory Data Analysis. Visualizing the dataset using various plots from matplotlib and seaborn.

Use the train_test_split method available in SCIKIT to split the dataset into Train Dataset and Test Dataset.

Perform classification on the datasets using Decision tree with various parameters.

Finding the accuracy of the model adn evaluation the model based on various evaluation metrics.

Importing the necessary libraries

Importing a dataset which contains various attributes about a car based on which the car is being evaluated for its safety.

```
In [2]: 1 df = pd.read_csv('car_evaluation.csv', header=None)
```

Exploratory data analysis

```
In [3]:
             df.head()
Out[3]:
               0
                     1 2 3
                                      5
                                            6
            vhigh vhigh
                        2
                          2
                             small
                                    low
                                        unacc
            vhigh vhigh 2 2 small med
                                        unacc
            vhigh
                  vhigh 2 2
                             small
                                   high
                 vhigh 2 2
            vhigh
                              med
                                        unacc
                                    low
            vhigh vhigh 2 2
                              med
                                   med
                                        unacc
In [4]:
             df.columns
Out[4]: Int64Index([0, 1, 2, 3, 4, 5, 6], dtype='int64')
```

Rename column names

We can see that the dataset does not have proper column names. The columns are merely labelled as 0,1,2.... and so on. WE are assigning them names based on their nature as follows:

```
In [5]:
              col_names = ['buying_price', 'maint', 'doors', 'persons', 'lug_boot', 'safet
             df.columns = col names
             col names
Out[5]: ['buying_price', 'maint', 'doors', 'persons', 'lug_boot', 'safety', 'class']
In [6]:
              df.head()
Out[6]:
             buying_price
                         maint doors persons lug_boot safety
                                                                class
          0
                          vhigh
                                    2
                                            2
                   vhigh
                                                   small
                                                           low
                                                               unacc
                          vhigh
                                            2
                   vhigh
                                    2
                                                   small
                                                          med
                                                               unacc
                          vhigh
                   vhigh
                                                   small
                                                          high
                                                               unacc
                          vhigh
                   vhigh
                                    2
                                            2
                                                   med
                                                           low
                                                               unacc
```

2

med

med

unacc

vhigh

2

vhigh

```
In [7]: 1 df.describe()
```

Out[7]:

6

class

dtypes: object(7)
memory usage: 94.6+ KB

	buying_price	maint	doors	persons	lug_boot	safety	class
count	1728	1728	1728	1728	1728	1728	1728
unique	4	4	4	3	3	3	4
top	vhigh	vhigh	3	more	small	high	unacc
freq	432	432	432	576	576	576	1210

```
In [8]:
          1 df.info()
        <class 'pandas.core.frame.DataFrame'>
        RangeIndex: 1728 entries, 0 to 1727
        Data columns (total 7 columns):
         #
             Column
                           Non-Null Count Dtype
                           -----
        ---
         0
             buying_price 1728 non-null
                                           object
             maint
                           1728 non-null
                                           object
         1
         2
             doors
                           1728 non-null
                                           object
         3
             persons
                           1728 non-null
                                           object
         4
                           1728 non-null
                                           object
             lug_boot
         5
             safety
                           1728 non-null
                                           object
```

object

The dataframe contains 7 columns and 1728 entries in each column.

1728 non-null

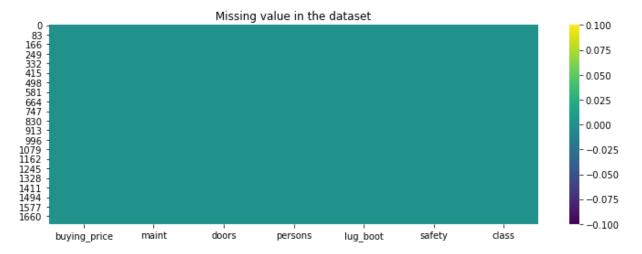
Frequency distribution of values in variables¶

```
In [9]:
          1
             for col in col names:
          2
          3
                  print(df[col].value_counts())
                  432
         vhigh
         high
                  432
                  432
         low
         med
                  432
         Name: buying_price, dtype: int64
         vhigh
                  432
         high
                  432
         low
                  432
                  432
         med
         Name: maint, dtype: int64
                  432
         3
         5more
                  432
                  432
         2
         4
                  432
         Name: doors, dtype: int64
                 576
         more
         2
                 576
         4
                 576
         Name: persons, dtype: int64
         small
                  576
         big
                  576
         med
                  576
         Name: lug_boot, dtype: int64
         high
                 576
                 576
         low
         med
                 576
         Name: safety, dtype: int64
         unacc
                  1210
         acc
                   384
                    69
         good
                    65
         vgood
         Name: class, dtype: int64
```

INFERENCE:

There are 7 variables in the dataset. All the variables are of categorical data type. These are given by buying, maint, doors, persons, lug_boot, safety and class. Where buying, maint, doors, persons, lug_boot, safety are the feature variables. Class is the target variable.

Checking for null values in the dataframe



There are no null values

Encode categorical variables

Machine learning algorithms cannot work with categorical data directly, categorical data must be converted to number.

Since the variables are mostly categorical data type, converting them into numerical form using label encoder.

Label encoding refers to transforming the word labels into numerical form so that the algorithms can understand how to operate on them.

```
In [11]: 1 label_encoder = preprocessing.LabelEncoder()
```

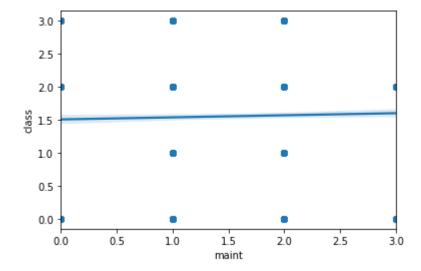
```
list = ['buying_price', 'maint', 'doors', 'persons', 'lug_boot', 'safety',
In [12]:
              for i in list:
           2
                  print(df[i].unique())
           3
           4
                  df[i]= label_encoder.fit_transform(df[i])
              df.head()
          ['vhigh' 'high' 'med' 'low']
         ['vhigh' 'high' 'med' 'low']
         ['2' '3' '4' '5more']
         ['2' '4' 'more']
         ['small' 'med' 'big']
         ['low' 'med' 'high']
         ['unacc' 'acc' 'vgood' 'good']
```

Out[12]:

	buying_price	maint	doors	persons	lug_boot	safety	class
0	3	3	0	0	2	1	2
1	3	3	0	0	2	2	2
2	3	3	0	0	2	0	2
3	3	3	0	0	1	1	2
4	3	3	0	0	1	2	2

```
In [13]: 1 sns.regplot(x = 'maint', y = 'class',data=df)
```

Out[13]: <AxesSubplot:xlabel='maint', ylabel='class'>



```
In [14]:
                  corr = df.corr()
               1
                  sns.heatmap(corr, cmap = 'Wistia', annot= True);
               2
                                                                                - 1.0
                                 -3.4e-162.1e-164.1e-171.7e-162.4e-16 0.051
              buying_price
                                                                               - 0.8
                                        -6.5e-174.3e-171.5e-161.4e-16 0.04
                                                                               - 0.6
                    doors -2.1e-166.5e-17
                                                2e-17 -1.9e-171.1e-16 -0.031
                  persons -4.1e-174.3e-17 2e-17
                                                      3.9e-183.4e-17 -0.3
                                                                               - 0.2
                 lug_boot -1.7e-161.5e-161.9e-173.9e-18
                                                            -1.5e-17 0.033
                                                                               -0.0
                    safety -2.4e-161.4e-161.1e-163.4e-17-1.5e-17
                                                                    -0.021
```

0.033 -0.021

safety

lug_boot .

persons

dass -

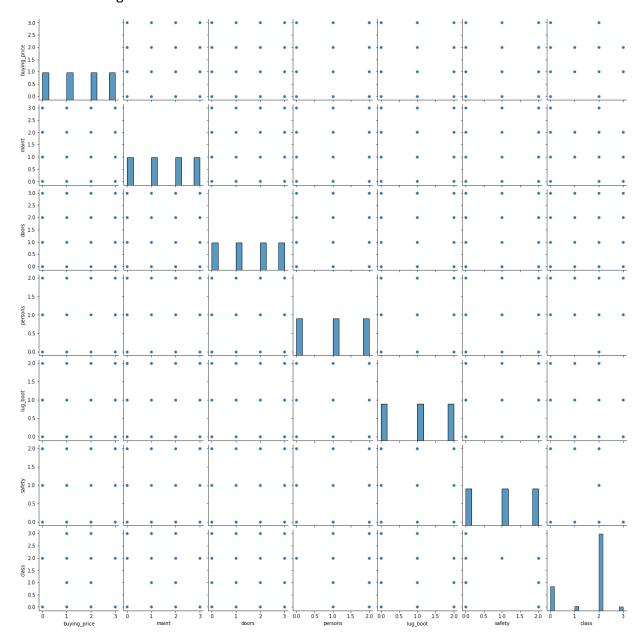
- -0.2

dass - 0.051 0.04 -0.031 -0.3

buying_price

In [15]: 1 sns.pairplot(df)

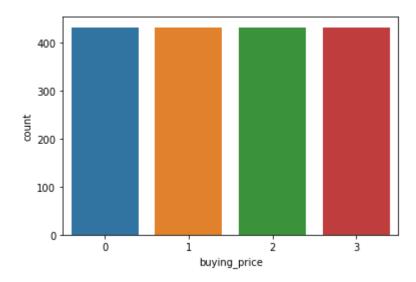
Out[15]: <seaborn.axisgrid.PairGrid at 0x14b32e763a0>



In [16]: 1 sns.countplot("buying_price",data=df)

C:\Users\SRIDHAR\anaconda3\lib\site-packages\seaborn_decorators.py:36: FutureW
arning: Pass the following variable as a keyword arg: x. From version 0.12, the
only valid positional argument will be `data`, and passing other arguments with
out an explicit keyword will result in an error or misinterpretation.
 warnings.warn(

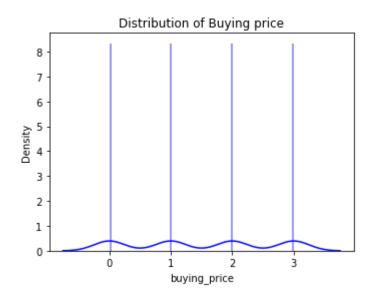
Out[16]: <AxesSubplot:xlabel='buying_price', ylabel='count'>



C:\Users\SRIDHAR\anaconda3\lib\site-packages\seaborn\distributions.py:2557: Fut ureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histogram s).

warnings.warn(msg, FutureWarning)

Out[17]: Text(0.5, 1.0, 'Distribution of Buying price')



Declare feature vector and target variable

Split data into separate training and test set

```
In [19]:
              from sklearn.model selection import train test split
            3 | X_train, X_test, y_train, y_test = train_test_split(X, y, test_size = 0.33,
In [20]:
            1 X train.shape, X test.shape
Out[20]: ((1157, 6), (571, 6))
In [21]:
            1 X train.head()
Out[21]:
                 buying_price maint doors persons lug_boot safety
             48
                          3
                                                2
                                                               1
            468
                          0
                                                         2
                                 3
                                       1
                                                1
                                                               1
            155
                          3
                                 0
                                       1
                                                2
                                                         2
                                                               0
                                                         2
           1721
                          1
                                       3
                                                2
                                                               0
           1208
                          2
                                 1
                                       0
                                                2
                                                         2
                                                               0
In [22]:
            1 y train.head()
Out[22]: 48
                   2
                   2
          468
          155
                   2
          1721
                   1
          1208
                   2
```

Decision Tree Classifier with criterion gini index

Predict the Test set results with criterion gini index

```
In [25]: 1 y_pred_gini = clf_gini.predict(X_test)
```

Check accuracy score

Name: class, dtype: int32

```
In [26]: 1 print('Model accuracy score with criterion gini index: {0:0.4f}'. format(acc
```

Model accuracy score with criterion gini index: 0.7653

Compare the train-set and test-set accuracy

```
Out[27]: array([2, 2, 0, ..., 0, 2, 2])
```

```
In [28]: 1 print('Training-set accuracy score: {:f}'. format(accuracy_score(y_train, y_
```

Training-set accuracy score: 0.774417

Print the scores on training and test set

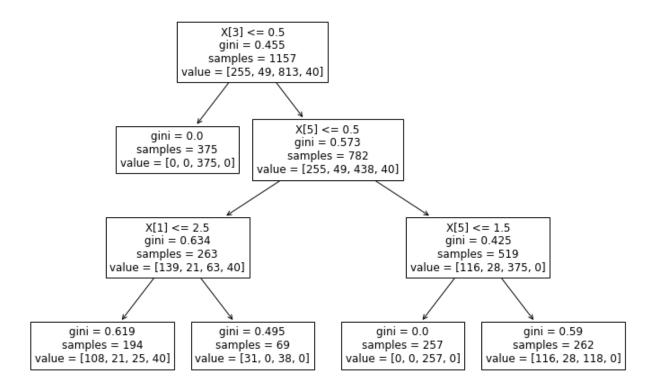
Training set score: 0.7744
Test set score: 0.7653

EVALUATION METRICS

Mean Absolute Error : 0.47810858143607704 Mean Squared Error : 1.052539404553415 Root Mean Squared Error : 1.0259334308586572

Visualize decision-trees

Out[31]: [Text(251.10000000000002, 380.52, 'X[3] <= 0.5\ngini = 0.455\nsamples = 1157\nv alue = [255, 49, 813, 40]'), Text(167.4, 271.8, 'gini = 0.0\nsamples = 375\nvalue = [0, 0, 375, 0]'), Text(334.8, 271.8, $X[5] \le 0.5 \le 0.5 \le 0.573 \le 0.573$ 9, 438, 40]'), Text(167.4, 163.079999999999, $'X[1] \le 2.5 \text{ ngini} = 0.634 \text{ nsamples} = 263 \text{ nval}$ ue = [139, 21, 63, 40]'), Text(83.7, 54.36000000000014, 'gini = 0.619\nsamples = 194\nvalue = [108, 21, 25, 40]'), Text(251.1000000000000, 54.36000000000014, 'gini = 0.495\nsamples = 69\nvalu e = [31, 0, 38, 0]'), $Text(502.20000000000005, 163.0799999999999, 'X[5] <= 1.5 \cdot in = 0.425 \cdot in = 0.42$ es = 519\nvalue = [116, 28, 375, 0]'), Text(418.5, 54.36000000000014, 'gini = 0.0\nsamples = 257\nvalue = [0, 0, 25 7, 0]'), Text(585.9, 54.36000000000014, 'gini = 0.59\nsamples = 262\nvalue = [116, 28, 118, 0]')]



Decision Tree Classifier with criterion entropy

```
In [32]: 1 clf_en = DecisionTreeClassifier(criterion='entropy')
In [33]: 1 clf_en.fit(X_train, y_train)
Out[33]: DecisionTreeClassifier(criterion='entropy')
```

Predict the Test set results and Check accuracy score with criterion entropy

```
In [34]: 1 y_pred_en = clf_en.predict(X_test)
2 print('Model accuracy score with criterion entropy: {0:0.4f}'. format(accurate)
```

Compare the train-set and test-set score

Model accuracy score with criterion entropy: 0.9720

Training-set accuracy score: 1.0000

Print the scores on training and test set

```
In [37]: 1 print('Training set score: {:.4f}'.format(clf_en.score(X_train, y_train)))
2 print('Test set score: {:.4f}'.format(clf_en.score(X_test, y_test)))

Training set score: 1.0000
Test set score: 0.9720
```

INFERENCE:

Now, based on the above analysis we can conclude that our classification model accuracy is very good. Our model is doing a very good job in terms of predicting the class labels. In case of classification with criterion entropy, The training accuracy score is 1 showing the excellent training of the model on the training data, because we dint mention any parameter and the dataset is very

small, the model trained well on all the data. Whereas in the Classification with criterion gingi index the training accuracy was a bit less, because the max_depth was 3. Showing the the branching stooped at 3rd step and the model has been trained until only that.

Confusion matrix

Confusion matrix

```
[[118 9 2 0]
[ 0 20 0 0]
[ 2 0 395 0]
[ 3 0 0 22]]
```

In [39]:	1	<pre>print(classification_r</pre>	eport(y_	_test, y_pro	red_en))	
		precision	recall	f1-score	support	

	0	0.96	0.91	0.94	129
	1	0.69	1.00	0.82	20
	2	0.99	0.99	0.99	397
	3	1.00	0.88	0.94	25
accur	acy			0.97	571
macro	avg	0.91	0.95	0.92	571
weighted	avg	0.98	0.97	0.97	571

EVALUATION METRICS

Mean Absolute Error : 0.04553415061295972 Mean Squared Error : 0.09106830122591944 Root Mean Squared Error : 0.30177524952507195

Visualize decision-trees

```
Out[42]: [Text(357.78319672131147, 420.384, 'X[3] <= 0.5\nentropy = 1.2\nsamples = 1157
                                                                                    \nvalue = [255, 49, 813, 40]'),
                                                                                         Text(346.8061475409836, 391.392, 'entropy = 0.0 \nsamples = 375 \nvalue = [0, 0, 0]
                                                                                    375, 0]'),
                                                                                          Text(368.76024590163934, 391.392, X[5] <= 0.5 \neq 1.465 = 782
                                                                                    \nvalue = [255, 49, 438, 40]'),
                                                                                         Text(198.6159836065574, 362.4, 'X[1] <= 2.5 \setminus 1.684 \le 2.63 \le 2.
                                                                                   alue = [139, 21, 63, 40]'),
                                                                                          Text(111.82868852459016, 333.408, X[0] \le 0.5 = 1.668 = 194
                                                                                    \nvalue = [108, 21, 25, 40]'),
                                                                                         Text(32.93114754098361, 304.416, 'X[2] \le 0.5 \le 0.232 \le 0.232
                                                                                   value = [51, 0, 2, 0]),
                                                                                            Text(21.95409836065574, 275.424, 'X[4] <= 1.5 \neq 0.65 = 12 \neq 0.65
                                                                                    alue = [10, 0, 2, 0]'),
                                                                                            Text(10.97704918032787, 246.432, 'entropy = 0.0\nsamples = 8\nvalue = [8, 0,
                                                                                   0, 0]'),
                                                                                          Text(32.93114754098361, 246.432, 'X[3] <= 1.5 \neq 1.0 = 1.0 = 4 \neq 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 1.0 = 
                                                                                   ue = [2, 0, 2, 0]),
                                                                                         Text(21.95409836065574, 217.44, 'entropy = 0.0 \times 10^{-2} = 0.0
                                                                                   0]'),
                                                                                            Text(43.90819672131148, 217.44, 'entropy = 0.0 \nsamples = 2 \nvalue = [0, 0, 2, 0]
                                                                                   0]'),
                                                                                          Text(43.90819672131148, 275.424, 'entropy = 0.0\nsamples = 41\nvalue = [41, 0,
                                                                                   0, 0]'),
                                                                                          Text(190.72622950819672, 304.416, 'X[0] \leftarrow 2.5 \neq 1.88 \Rightarrow 1
                                                                                    \nvalue = [57, 21, 23, 40]'),
                                                                                         Text(145.44590163934427, 275.424, 'X[4] <= 1.5 \neq 1.5 \neq 1.753 = 92
                                                                                    \nvalue = [26, 21, 5, 40]'),
                                                                                          Text(87.81639344262295, 246.432, 'X[1] <= 0.5 \neq 1.196 = 59 
                                                                                   value = [13, 6, 0, 40]'),
                                                                                         Text(65.86229508196722, 217.44, 'X[0] <= 1.5 \neq 0.988 = 23 \neq 0.988
                                                                                    alue = [13, 0, 0, 10]'),
                                                                                          Text(54.885245901639344, 188.4479999999999, |X[4] <= 0.5 \neq 0.779 
                                                                                   mples = 13\nvalue = [3, 0, 0, 10]'),
                                                                                          Text(43.90819672131148, 159.4559999999996, 'entropy = 0.0\nsamples = 8\nvalue
                                                                                   = [0, 0, 0, 8]'),
                                                                                          Text(65.86229508196722, 159.45599999999996, 'X[2] <= 2.0 \neq 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0
                                                                                    ples = 5\nvalue = [3, 0, 0, 2]'),
                                                                                            Text(54.885245901639344, 130.464, 'entropy = 0.0\nsamples = 3\nvalue = [3, 0,
                                                                                   0, 0]'),
                                                                                          Text(76.83934426229509, 130.464, 'entropy = 0.0\nsamples = 2\nvalue = [0, 0, 0]
                                                                                   0, 2]'),
                                                                                         Text(76.83934426229509, 188.4479999999998, 'entropy = 0.0\nsamples = 10\nvalu
                                                                                    e = [10, 0, 0, 0]'),
                                                                                         Text(109.77049180327869, 217.44, 'X[4] <= 0.5 \setminus pertopy = 0.65 \setminus pertopy = 36 \setminus
                                                                                   alue = [0, 6, 0, 30]'),
                                                                                          Text(98.79344262295082, 188.4479999999998, 'entropy = 0.0\nsamples = 19\nvalu
                                                                                   e = [0, 0, 0, 19]'),
                                                                                            Text(120.74754098360656, 188.4479999999999, |X[2]| <= 0.5 = 0.937
```

mples = $17 \cdot \text{nvalue} = [0, 6, 0, 11]'$),

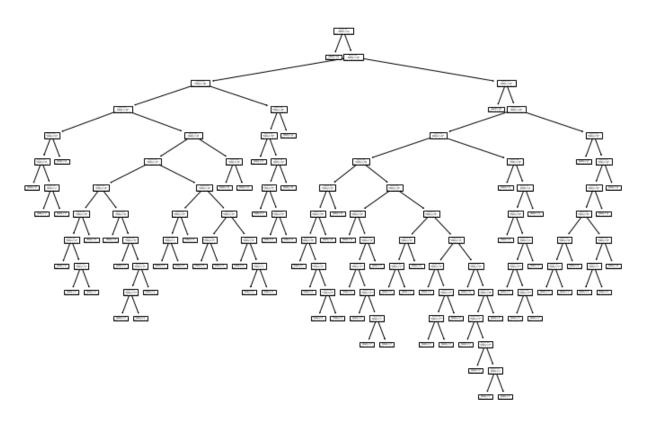
```
Text(109.77049180327869, 159.4559999999996, 'entropy = 0.0\nsamples = 5\nvalu
e = [0, 5, 0, 0]'),
     Text(131.72459016393444, 159.45599999999996, |X[2]| \le 1.5 \le 0.414 \le 0.414
mples = 12\nvalue = [0, 1, 0, 11]'),
      Text(120.74754098360656, 130.464, 'X[3] \le 1.5 \neq 0.918 \le 3 n
value = [0, 1, 0, 2]'),
       Text(109.77049180327869, 101.4719999999999, 'entropy = 0.0\nsamples = 1\nvalu
e = [0, 1, 0, 0]'),
       Text(131.72459016393444, 101.4719999999999, 'entropy = 0.0\nsamples = 2\nvalu
e = [0, 0, 0, 2]'),
      Text(142.7016393442623, 130.464, 'entropy = 0.0 \times 9 = 9 \times 9 = 0.0 \times 9 = 0.
0, 9]'),
      Text(203.07540983606557, 246.432, X[1] \le 0.5 = 1.459 = 33
\nvalue = [13, 15, 5, 0]'),
      alue = [10, 0, 1, 0]'),
       Text(164.65573770491804, 188.44799999999999, 'X[3] <= 1.5\nentropy = 1.0\nsamp
les = 2\nvalue = [1, 0, 1, 0]'),
      Text(153.67868852459017, 159.45599999999996, 'entropy = 0.0\nsamples = 1\nvalu
e = [1, 0, 0, 0]'),
      Text(175.6327868852459, 159.4559999999996, 'entropy = 0.0\nsamples = 1\nvalue
= [0, 0, 1, 0]'),
      Text(186.60983606557377, 188.4479999999999, 'entropy = 0.0\nsamples = 9\nvalu
e = [9, 0, 0, 0]'),
      Text(230.51803278688524, 217.44, 'X[2] <= 0.5 \neq 1.216 = 22 = 22 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 = 2.5 
value = [3, 15, 4, 0]),
     Text(208.5639344262295, 188.4479999999998, 'X[3] <= 1.5 \neq 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.985 = 0.
ples = 7\nvalue = [0, 3, 4, 0]'),
       Text(197.58688524590164, 159.45599999999996, 'entropy = 0.0\nsamples = 3\nvalu
e = [0, 3, 0, 0]'),
      Text(219.54098360655738, 159.4559999999996, 'entropy = 0.0\nsamples = 4\nvalu
e = [0, 0, 4, 0]'),
       Text(252.47213114754098, 188.4479999999999, X[0] <= 1.5 \neq 0.722 
mples = 15 \cdot \text{nvalue} = [3, 12, 0, 0]'),
       Text(241.4950819672131, 159.4559999999996, 'entropy = 0.0\nsamples = 9\nvalue
= [0, 9, 0, 0]'),
     Text(263.4491803278689, 159.4559999999996, 'X[1] <= 1.5 \setminus nentropy = 1.0 \setminus nentropy = 1.0
es = 6\nvalue = [3, 3, 0, 0]'),
      Text(252.47213114754098, 130.464, 'entropy = 0.0 \times 10^{-2} = 3 \times 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-2} = 10^{-
0, 0]'),
      Text(274.42622950819674, 130.464, 'entropy = 0.0 \times 10^{-2} = 3 \times 10^{-2} = 3 \times 10^{-2} Text(274.42622950819674, 130.464, 'entropy = 0.0 \times 10^{-2} = 3 \times 10^{
0, 0]'),
      Text(236.00655737704918, 275.424, 'X[1] \le 0.5 \neq 0.949 \le 0.949 \le 49
\nvalue = [31, 0, 18, 0]'),
      Text(225.0295081967213, 246.432, 'entropy = 0.0\nsamples = 18\nvalue = [0, 0,
18, 0]'),
      Text(246.98360655737704, 246.432, 'entropy = 0.0\nsamples = 31\nvalue = [31,
0, 0, 0]'),
      Text(285.4032786885246, 333.408, 'X[0] <= 2.5 \setminus equal = 0.993 \setminus equal = 69 \setminus equal = 0.993 \setminus
value = [31, 0, 38, 0]'),
     Text(274.42622950819674, 304.416, 'X[0] \leftarrow 0.5\nentropy = 0.958\nsamples = 50
\nvalue = [31, 0, 19, 0]'),
      Text(263.4491803278689, 275.424, 'entropy = 0.0\nsamples = 17\nvalue = [0, 0,
17, 0]'),
       Text(285.4032786885246, 275.424, X[2] <= 0.5\nentropy = 0.33\nsamples = 33\nv
alue = [31, 0, 2, 0]'),
       Text(274.42622950819674, 246.432, X[4] <= 1.5 \neq 0.863 = 7 = 7 = 7
```

```
value = [5, 0, 2, 0]),
      Text(263.4491803278689, 217.44, 'entropy = 0.0\nsamples = 4\nvalue = [4, 0, 0, 0]
0]'),
      Text(285.4032786885246, 217.44, 'X[3] <= 1.5\nentropy = 0.918\nsamples = 3\nva
lue = [1, 0, 2, 0]),
      Text(274.42622950819674, 188.4479999999999, 'entropy = 0.0\nsamples = 1\nvalu
e = [1, 0, 0, 0]'),
     Text(296.3803278688525, 188.44799999999998, 'entropy = 0.0 \nsamples = 2 \nvalue
= [0, 0, 2, 0]'),
      0, 0]'),
      Text(296.3803278688525, 304.416, 'entropy = 0.0 \times 10^{-1} = 19 \times 10^{-
19, 0]'),
      Text(538.9045081967213, 362.4, 'X[5] <= 1.5\nentropy = 1.049\nsamples = 519\nv
alue = [116, 28, 375, 0]'),
      Text(527.9274590163934, 333.408, 'entropy = 0.0 \times 0.0 = 257 \times 0.0 = 0.0 \times 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.0 = 0.
257, 0]'),
     Text(549.8815573770491, 333.408, 'X[4] <= 1.5\nentropy = 1.383\nsamples = 262
\nvalue = [116, 28, 118, 0]'),
      Text(463.094262295082, 304.416, X[0] <= 2.5 \neq 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.432 = 1.
value = [91, 28, 51, 0]'),
      Text(377.3360655737705, 275.424, 'X[0] \le 0.5 \neq 1.381 \le 1.25
\nvalue = [74, 28, 23, 0]'),
      Text(340.28852459016395, 246.432, 'X[1] <= 2.5\nentropy = 0.974\nsamples = 42
\nvalue = [25, 0, 17, 0]'),
      Text(329.3114754098361, 217.44, 'X[2] \le 1.5 \neq 0.758 \le 32 \le 1.5 \le
alue = [25, 0, 7, 0]'),
      Text(318.3344262295082, 188.4479999999998, 'X[4] \le 0.5 \neq 0.989 
ples = 16 \cdot value = [9, 0, 7, 0]'),
      Text(307.35737704918034, 159.4559999999999, 'entropy = 0.0\nsamples = 7\nvalu
e = [7, 0, 0, 0]'),
     Text(329.3114754098361, 159.4559999999996, 'X[3] <= 1.5 \setminus entropy = 0.764 \setminus entrop
ples = 9\nvalue = [2, 0, 7, 0]'),
      Text(318.3344262295082, 130.464, 'entropy = 0.0 \times 6 = 6 \times 6 = 0, 'entropy = 0.0 \times 6 = 0, 'e
6, 0]'),
      Text(340.28852459016395, 130.464, 'X[2] \le 0.5 \text{ nentropy} = 0.918 \text{ nsamples} = 3 \text{ nentropy}
value = [2, 0, 1, 0]'),
      Text(329.3114754098361, 101.4719999999998, 'entropy = 0.0\nsamples = 1\nvalue
= [0, 0, 1, 0]'),
      Text(351.2655737704918, 101.4719999999998, 'entropy = 0.0 \nsamples = 2 \nvalue
= [2, 0, 0, 0]'),
      Text(340.28852459016395, 188.4479999999999, 'entropy = 0.0\nsamples = 16\nval
ue = [16, 0, 0, 0]'),
      Text(351.2655737704918, 217.44, 'entropy = 0.0\nsamples = 10\nvalue = [0, 0, 1]
0, 0]'),
      Text(414.38360655737705, 246.432, 'X[1] <= 0.5\nentropy = 1.252\nsamples = 83
\nvalue = [49, 28, 6, 0]'),
      Text(373.21967213114755, 217.44, 'X[4] <= 0.5\nentropy = 0.439\nsamples = 22\n
value = [20, 0, 2, 0]'),
      Text(362.2426229508197, 188.4479999999998, 'entropy = 0.0 \nsamples = 12 \nvalue
e = [12, 0, 0, 0]'),
     Text(384.1967213114754, 188.4479999999998, 'X[2] <= 1.5 \neq 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.722 = 0.
ples = 10 \setminus value = [8, 0, 2, 0]'),
      Text(373.21967213114755, 159.4559999999999, |X[0] <= 1.5 \neq 0.971 
mples = 5\nvalue = [3, 0, 2, 0]'),
      Text(362.2426229508197, 130.464, 'entropy = 0.0\nsamples = 2\nvalue = [2, 0,
0, 0]'),
```

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Text(384.1967213114754, 130.464, 'X[3] <= 1.5\nentropy = 0.918\nsamples = 3\nv
alue = [1, 0, 2, 0]),
  Text(373.21967213114755, 101.4719999999999, 'entropy = 0.0\nsamples = 1\nvalu
e = [0, 0, 1, 0]'),
  Text(395.1737704918033, 101.4719999999998, 'X[2] <= 0.5 \setminus nentropy = 1.0 \setminus nentropy = 1.0
es = 2\nvalue = [1, 0, 1, 0]'),
  Text(384.1967213114754, 72.4799999999996, 'entropy = 0.0 \times 10^{-1} = 1\nvalue
= [0, 0, 1, 0]'),
  Text(406.15081967213115, 72.479999999999, 'entropy = 0.0\nsamples = 1\nvalue
= [1, 0, 0, 0]'
   Text(395.1737704918033, 159.45599999999996, 'entropy = 0.0 \times 5 = 5 \times 10^{-2}
= [5, 0, 0, 0]'),
  Text(455.54754098360655, 217.44, 'X[1] <= 1.5\nentropy = 1.283\nsamples = 61\n
value = [29, 28, 4, 0]'),
  Text(428.1049180327869, 188.4479999999998, 'X[2] <= 0.5\nentropy = 0.276\nsam
ples = 21\nvalue = [1, 20, 0, 0]'),
  Text(417.127868852459, 159.45599999999996, 'X[4] <= 0.5\nentropy = 0.722\nsamp
les = 5\nvalue = [1, 4, 0, 0]'),
   Text(406.15081967213115, 130.464, 'entropy = 0.0\nsamples = 4\nvalue = [0, 4,
0, 0]'),
  Text(428.1049180327869, 130.464, 'entropy = 0.0\nsamples = 1\nvalue = [1, 0,
0, 0]'),
  Text(439.08196721311475, 159.4559999999999, 'entropy = 0.0\nsamples = 16\nval
ue = [0, 16, 0, 0]'),
   Text(482.9901639344262, 188.4479999999999, 'X[0] <= 1.5 \setminus nentropy = 1.157 \setminus nentropy =
ples = 40\nvalue = [28, 8, 4, 0]'),
  Text(461.0360655737705, 159.45599999999996, 'X[1] <= 2.5\nentropy = 1.272\nsam
ples = 16\nvalue = [7, 8, 1, 0]'),
   Text(450.0590163934426, 130.464, 'entropy = 0.0\nsamples = 8\nvalue = [0, 8]
0, 0]'),
   Text(472.01311475409835, 130.464, 'X[2] <= 1.0 \nentropy = 0.544 \nsamples = 8 \ngmath{n}
value = [7, 0, 1, 0]),
   Text(461.0360655737705, 101.47199999999998, 'X[4] <= 0.5\nentropy = 0.918\nsam
ples = 3\nvalue = [2, 0, 1, 0]'),
   Text(450.0590163934426, 72.4799999999996, 'entropy = 0.0 \nsamples = 2 \nvalue
= [2, 0, 0, 0]'),
  Text(472.01311475409835, 72.4799999999996, 'entropy = 0.0 \nsamples = 1 \nvalue
= [0, 0, 1, 0]'),
  Text(482.9901639344262, 101.4719999999998, 'entropy = 0.0 \times 10^{-1} = 0.0 \times 10^{-1}
= [5, 0, 0, 0]'),
  Text(504.94426229508196, 159.45599999999996, 'X[1] <= 2.5 \nentropy = 0.544 \nsa
mples = 24 \cdot value = [21, 0, 3, 0]'),
   Text(493.9672131147541, 130.464, 'entropy = 0.0\nsamples = 14\nvalue = [14, 0,
0, 0]'),
   Text(515.9213114754099, 130.464, X[2] \le 1.5 \le 0.881 \le 10 
value = [7, 0, 3, 0]),
  Text(504.94426229508196, 101.47199999999998, X[4] <= 0.5 \neq 0.971 
mples = 5\nvalue = [2, 0, 3, 0]'),
  Text(493.9672131147541, 72.4799999999996, 'entropy = 0.0 \times 10^{-1} = 1\nvalue
= [1, 0, 0, 0]'),
  Text(515.9213114754099, 72.4799999999996, |X[2]| \le 0.5 = 0.811 = 0.811
les = 4\nvalue = [1, 0, 3, 0]'),
  Text(504.94426229508196, 43.488, 'entropy = 0.0 \times 2 = 2 \times 2 = 0, 0,
2, 0]'),
  Text(526.8983606557377, 43.488, 'X[3] <= 1.5\nentropy = 1.0\nsamples = 2\nvalu
e = [1, 0, 1, 0]'),
   Text(515.9213114754099, 14.495999999999991, 'entropy = 0.0 \nsamples = 1 \nvalue
```

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= [0, 0, 1, 0]'),
      = [1, 0, 0, 0]'),
      Text(526.8983606557377, 101.4719999999999, 'entropy = 0.0\nsamples = 5\nvalue
= [5, 0, 0, 0]'),
      Text(548.8524590163935, 275.424, 'X[1] <= 0.5 \neq 0.956 = 45 
value = [17, 0, 28, 0]'),
     Text(537.8754098360656, 246.432, 'entropy = 0.0\nsamples = 11\nvalue = [0, 0,
11, 0]'),
     Text(559.8295081967213, 246.432, 'X[1] \le 2.5 \neq 1.0 \le 34 
lue = [17, 0, 17, 0]),
      Text(548.8524590163935, 217.44, 'X[4] <= 0.5 \neq 0.5 = 0.828 = 23 \neq 0.5 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.828 = 0.82
alue = [17, 0, 6, 0]),
       Text(537.8754098360656, 188.4479999999998, 'entropy = 0.0 \nsamples = 11 \nvalu
e = [11, 0, 0, 0]'),
      Text(559.8295081967213, 188.4479999999998, 'X[2] <= 1.5 \setminus nentropy = 1.0 \setminus nentropy = 1.0
es = 12 \cdot value = [6, 0, 6, 0]'),
     Text(548.8524590163935, 159.45599999999996, 'X[3] <= 1.5 \neq 0.592 \Rightarrow 0
ples = 7 \cdot value = [1, 0, 6, 0]'),
       Text(537.8754098360656, 130.464, 'entropy = 0.0 \times 10^{-1} = 1.0 \times 10^{-1} Text(537.8754098360656, 130.464, 'entropy = 1.0 \times 10^{-1} Text(537.8754098806), 'entropy = 1.0 \times 10^{-1} Text(537.875409806), '
4, 0]'),
       Text(559.8295081967213, 130.464, X[2] <= 0.5\nentropy = 0.918\nsamples = 3\nv
alue = [1, 0, 2, 0]'),
      Text(548.8524590163935, 101.4719999999998, 'entropy = 0.0 \times 2 \times 10^{-1}
= [0, 0, 2, 0]'),
       Text(570.8065573770492, 101.4719999999998, 'entropy = 0.0 \times 10^{-1} = 1\nvalue
= [1, 0, 0, 0]'),
     Text(570.8065573770492, 159.4559999999996, 'entropy = 0.0 \nsamples = 5 \nvalue
= [5, 0, 0, 0]'),
      Text(570.8065573770492, 217.44, 'entropy = 0.0 \times 11 = 11 \times 11 = 10, 0, 1
1, 0]'),
      Text(636.6688524590164, 304.416, X[0] \le 0.5 \le 0.844 \le 92 \le 9.844 \le 9
value = [25, 0, 67, 0]'),
     Text(625.6918032786886, 275.424, 'entropy = 0.0\nsamples = 24\nvalue = [0, 0,
24, 0]'),
     Text(647.6459016393443, 275.424, 'X[0] \le 2.5 \neq 0.949 \le 0.949 \le 68 
value = [25, 0, 43, 0]'),
       Text(636.6688524590164, 246.432, 'X[1] <= 2.5\nentropy = 0.995\nsamples = 46\n
value = [25, 0, 21, 0]'),
       Text(625.6918032786886, 217.44, 'X[1] <= 0.5\nentropy = 0.834\nsamples = 34\nv
alue = [25, 0, 9, 0]),
     Text(603.7377049180328, 188.4479999999998, 'X[0] <= 1.5 \neq 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.971 = 0.
ples = 10 \setminus value = [4, 0, 6, 0]'),
      Text(592.760655737705, 159.45599999999996, |X[2]| \le 0.5 = 0.722 
les = 5 \cdot value = [4, 0, 1, 0]'),
      Text(581.7836065573771, 130.464, 'entropy = 0.0 \times 1.7836065573771, 130.464, 'entropy = 0.0 \times 1.7836065771, 130.464, 'entropy = 0.0 \times 1.7836067, 130.464, 'entropy = 0.0 \times 1.7836067, 130.464, 130.464, 'entropy = 0.0 \times 1.783606, 'entropy = 0.0 \times 1.783606
1, 0]'),
      0, 0]'),
      Text(614.7147540983607, 159.4559999999996, 'entropy = 0.0\nsamples = 5\nvalue
= [0, 0, 5, 0]'),
     Text(647.6459016393443, 188.4479999999998, 'X[2] <= 0.5 \nentropy = 0.544 \nsam
ples = 24\nvalue = [21, 0, 3, 0]'),
      Text(636.6688524590164, 159.4559999999996, 'X[3] <= 1.5\nentropy = 1.0\nsampl
es = 6\nvalue = [3, 0, 3, 0]'),
      Text(625.6918032786886, 130.464, 'entropy = 0.0\nsamples = 3\nvalue = [3, 0,
0, 0]'),
```

```
Text(647.6459016393443, 130.464, 'entropy = 0.0\nsamples = 3\nvalue = [0, 0,
3, 0]'),
  Text(658.6229508196722, 159.4559999999996, 'entropy = 0.0\nsamples = 18\nvalue = [18, 0, 0, 0]'),
  Text(647.6459016393443, 217.44, 'entropy = 0.0\nsamples = 12\nvalue = [0, 0, 1 2, 0]'),
  Text(658.6229508196722, 246.432, 'entropy = 0.0\nsamples = 22\nvalue = [0, 0, 22, 0]')]
```



IMPORTING THE SECOND DATASET

We are using the wine dataset which is already present in the sklearn.

```
In [43]: 1 from sklearn import datasets
2 from sklearn.datasets import load_wine

In [44]: 1 wine = datasets.load_wine(as_frame = True)
```

Declare feature vector and target variable

data_wine are the feature variables target is the target variable

Out[45]:

	alcohol	malic_acid	ash	alcalinity_of_ash	magnesium	total_phenols	flavanoids	nonflavanoid_
0	14.23	1.71	2.43	15.6	127.0	2.80	3.06	_
1	13.20	1.78	2.14	11.2	100.0	2.65	2.76	
2	13.16	2.36	2.67	18.6	101.0	2.80	3.24	
3	14.37	1.95	2.50	16.8	113.0	3.85	3.49	
4	13.24	2.59	2.87	21.0	118.0	2.80	2.69	
4								>

EXPLORATORY DATA ANALYSIS

In [46]:	1	target.head()
Out[46]:	0	0
	1	0
	2	0
	3	0
	4	0
	Name	e: target, dtype: int32

In [47]: 1 data_wine.describe()

Out[47]:

	alcohol	malic_acid	ash	alcalinity_of_ash	magnesium	total_phenols	flavanoids
count	178.000000	178.000000	178.000000	178.000000	178.000000	178.000000	178.000000
mean	13.000618	2.336348	2.366517	19.494944	99.741573	2.295112	2.029270
std	0.811827	1.117146	0.274344	3.339564	14.282484	0.625851	0.998859
min	11.030000	0.740000	1.360000	10.600000	70.000000	0.980000	0.340000
25%	12.362500	1.602500	2.210000	17.200000	88.000000	1.742500	1.205000
50%	13.050000	1.865000	2.360000	19.500000	98.000000	2.355000	2.135000
75%	13.677500	3.082500	2.557500	21.500000	107.000000	2.800000	2.875000
max	14.830000	5.800000	3.230000	30.000000	162.000000	3.880000	5.080000
4							+

```
In [48]:
           1 target.describe()
Out[48]: count
                   178.000000
                     0.938202
          mean
          std
                     0.775035
          min
                     0.000000
          25%
                     0.000000
          50%
                     1.000000
          75%
                     2.000000
                     2.000000
          max
          Name: target, dtype: float64
In [49]:
              data wine.isnull().sum()
Out[49]: alcohol
                                           0
          malic acid
                                           0
          ash
                                           0
          alcalinity_of_ash
                                           0
          magnesium
          total_phenols
          flavanoids
          nonflavanoid phenols
          proanthocyanins
          color_intensity
                                           0
                                           0
          od280/od315_of_diluted_wines
          proline
          dtype: int64
```

Split data into separate training and test set

```
In [50]:
           1 | X_train, X_test, y_train, y_test = train_test_split(data_wine, target, test
In [51]:
           1 print('X train shape=', X_train.shape)
           2 print('X test shape=', X_test.shape)
           3 print('y train shape=', y_train.shape)
             print('y test shape=', y test.shape)
         X train shape= (106, 13)
         X test shape= (72, 13)
         y train shape= (106,)
         y test shape= (72,)
```

Decision Tree Classifier with criterion gini index

```
1 clf_gini = DecisionTreeClassifier(criterion='gini')
In [52]:
           2 clf_gini.fit(X_train, y_train)
```

Out[52]: DecisionTreeClassifier()

Predict the Test set results and Check accuracy score

```
In [53]: 1 y_pred_gini = clf_gini.predict(X_test)
```

In [54]: 1 print('Model accuracy score with criterion gini index: {0:0.4f}'. format(acc

Model accuracy score with criterion gini index: 0.9306

Compare the train-set and test-set accuracy

```
In [55]: 1 y_pred_train_gini = clf_gini.predict(X_train)
2 
y_pred_train_gini
```

```
Out[55]: array([2, 2, 1, 1, 0, 2, 0, 1, 2, 0, 1, 0, 2, 1, 1, 0, 1, 1, 1, 0, 1, 1, 1, 2, 1, 1, 1, 1, 1, 0, 0, 0, 2, 0, 1, 2, 2, 0, 1, 0, 1, 1, 0, 2, 1, 1, 2, 2, 1, 1, 1, 2, 2, 1, 0, 1, 0, 2, 1, 1, 0, 0, 1, 0, 0, 2, 0, 2, 2, 2, 2, 2, 2, 1, 0, 0, 2, 1, 1, 2, 1, 2, 2, 1, 2, 0])
```

```
In [56]: 1 print('Training-set accuracy score: {0:0.4f}'. format(accuracy_score(y_train
```

Training-set accuracy score: 1.0000

Print the scores on training and test set

Training set score: 1.0000 Test set score: 0.9306

EVALUATION METRICS

```
In [58]: 1 print('Mean Absolute Error : ', metrics.mean_absolute_error(y_test, y_pred_g
print('Mean Squared Error : ', metrics.mean_squared_error(y_test, y_pred_gin
print('Root Mean Squared Error : ', np.sqrt(metrics.mean_squared_error(y_test))
```

Classification Report

```
In [59]:
           1 print(classification report(y test, y pred gini))
                        precision
                                      recall f1-score
                                                          support
                              0.96
                                        0.93
                     0
                                                  0.95
                                                               28
                     1
                              0.93
                                        0.93
                                                  0.93
                                                               27
                     2
                              0.89
                                        0.94
                                                  0.91
                                                               17
                                                  0.93
                                                               72
              accuracy
             macro avg
                                                  0.93
                                                               72
                              0.93
                                        0.93
          weighted avg
                              0.93
                                        0.93
                                                  0.93
                                                               72
```

Decision Tree Classifier with criterion entropy

```
In [60]: 1 clf_en = DecisionTreeClassifier(criterion='entropy',max_depth=4)
In [61]: 1 clf_en.fit(X_train, y_train)
Out[61]: DecisionTreeClassifier(criterion='entropy', max_depth=4)
```

Predict the Test set results and Check accuracy score

```
In [62]: 1 y_pred_en = clf_en.predict(X_test)
2 print('Model accuracy score with criterion entropy: {0:0.4f}'. format(accurate)
```

Model accuracy score with criterion entropy: 0.9306

Compare the train-set and test-set accuracy

```
In [64]: 1 y_pred_train_en = clf_en.predict(X_train)
2 print('Training-set accuracy score: {0:0.4f}'. format(accuracy_score(y_train))
```

Training-set accuracy score: 1.0000

Print the scores on training and test set

```
In [65]: 1 print('Training set score: {:.4f}'.format(clf_en.score(X_train, y_train)))
2 print('Test set score: {:.4f}'.format(clf_en.score(X_test, y_test)))
```

Training set score: 1.0000 Test set score: 0.9306

EVALUATION METRICS

```
In [68]: 1 print('Mean Absolute Error : ', metrics.mean_absolute_error(y_test, y_pred_e
    print('Mean Squared Error : ', metrics.mean_squared_error(y_test, y_pred_en)
    print('Root Mean Squared Error : ', np.sqrt(metrics.mean_squared_error(y_test))
```

Mean Absolute Error : 0.0694444444444445 Mean Squared Error : 0.069444444444445 Root Mean Squared Error : 0.26352313834736496

Confusion matrix

```
In [69]: 1 cm = confusion_matrix(y_test, y_pred_en)
2 print('Confusion matrix\n\n', cm)

Confusion matrix

[[27  1  0]
  [ 3  24  0]
```

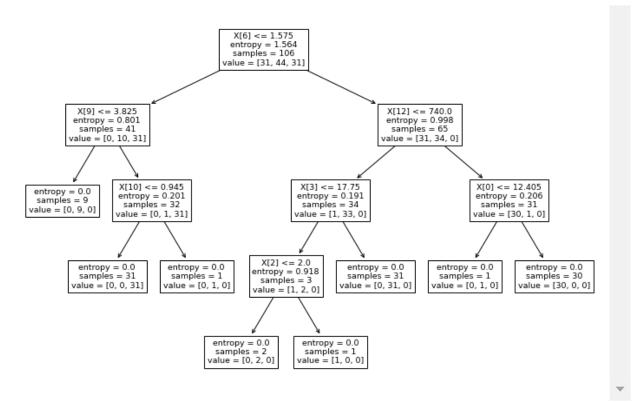
Classification Report

[0 1 16]]

In [70]:	<pre>print(classification_report(y_test, y_pred_en))</pre>							
		precision	recall	f1-score	support			
	0	0.90	0.96	0.93	28			
	1	0.92	0.89	0.91	27			
	2	1.00	0.94	0.97	17			
	accuracy			0.93	72			
	macro avg	0.94	0.93	0.94	72			
,	weighted avg	0.93	0.93	0.93	72			

Visualize decision-trees¶

```
Out[71]: [Text(283.2923076923077, 391.392, 'X[6] <= 1.575\nentropy = 1.564\nsamples = 10
                         6\nvalue = [31, 44, 31]'),
                           Text(103.01538461538462, 304.416, X[9] <= 3.825 \nentropy = 0.801 \nsamples = 4
                         1\nvalue = [0, 10, 31]'),
                           Text(51.50769230769231, 217.44, 'entropy = 0.0 \times 9, 'entropy = 
                         0]'),
                           Text(154.52307692307693, 217.44, 'X[10] <= 0.945\nentropy = 0.201\nsamples = 3
                         2\nvalue = [0, 1, 31]'),
                           Text(103.01538461538462, 130.464, 'entropy = 0.0\nsamples = 31\nvalue = [0, 0,
                         31]'),
                           Text(206.03076923076924, 130.464, 'entropy = 0.0\nsamples = 1\nvalue = [0, 1, 1]
                         0]'),
                           Text(463.5692307692308, 304.416, 'X[12] <= 740.0 \nentropy = 0.998 \nsamples = 6
                         5\nvalue = [31, 34, 0]'),
                           Text(360.55384615384617, 217.44, 'X[3] <= 17.75\nentropy = 0.191\nsamples = 34
                         \nvalue = [1, 33, 0]'),
                           Text(309.04615384615386, 130.464, 'X[2] <= 2.0 \nentropy = 0.918 \nsamples = 3 \n
                         value = [1, 2, 0]'),
                           Text(257.53846153846155, 43.488, 'entropy = 0.0\nsamples = 2\nvalue = [0, 2, 1]
                         0]'),
                           Text(360.55384615384617, 43.488, 'entropy = 0.0\nsamples = 1\nvalue = [1, 0,
                         0]'),
                           Text(412.0615384615385, 130.464, 'entropy = 0.0\nsamples = 31\nvalue = [0, 31,
                         0]'),
                           Text(566.5846153846154, 217.44, X[0] <= 12.405 \setminus 1000 = 0.206 \setminus 1000 = 31
                         \nvalue = [30, 1, 0]'),
                           Text(515.0769230769231, 130.464, 'entropy = 0.0\nsamples = 1\nvalue = [0, 1,
                         0]'),
                           Text(618.0923076923077, 130.464, 'entropy = 0.0\nsamples = 30\nvalue = [30, 0,
                         0]')]
```



CONCLUSION:

Imported two dataset and perfored classification using decision tree with various criterion. Evaluated each model on various evaluation metrics.

REFERENCES:

https://www.kaggle.com/code/prashant111/decision-tree-classifier-tutorial/notebook (https://www.kaggle.com/code/prashant111/decision-tree-classifier-tutorial/notebook) https://www.kaggle.com/code/satishgunjal/tutorial-decision-tree/notebook (https://www.kaggle.com/code/satishgunjal/tutorial-decision-tree/notebook) https://scikit-learn.org/stable/modules/generated/sklearn.tree.DecisionTreeClassifier.html (https://scikit-learn.org/stable/modules/generated/sklearn.tree.DecisionTreeClassifier.html)