

1. Terry goes to the bank - $P(A) = 0.2$
 Susan goes to the bank - $P(B) = 0.3$
 Together they are at the bank $P(A \cap B) = 0.08$
 Terry is not at Bank - $P(A') = 1 - 0.2 = 0.8$
 Susan is not at Bank - $P(B') = 1 - 0.3 = 0.7$

	$P(B)$	$P(B')$
$P(A)$	0.08	0.12
$P(A')$	0.22	0.58

a) $P(\text{Terry at Bank} / \text{Susan at Bank})$

$$= \frac{P(A \cap B)}{P(B)} = \frac{0.08}{0.3} = 0.266 = \underline{\underline{26.66\%}}$$

b) $P(\text{Terry at Bank} / \text{Susan not at Bank})$

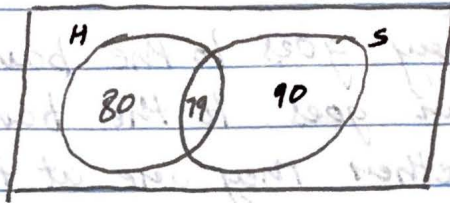
$$= \frac{P(A \cap B')}{P(B')} = \frac{0.12}{0.7} = 0.1714 = \underline{\underline{17.14\%}}$$

(c) $P(\text{Both were there} / \text{At least one of them was there})$

$$= \frac{P(A \cap B)}{P(A \cup B)}$$

$$= \frac{P(A \cap B)}{P(A \cup B)} = \frac{0.08}{0.42} = 0.1904 = \underline{\underline{19.04\%}}$$

1.2



Harold's chances for getting B = $P(A) = 0.80$

Sharon's chances for getting B = $P(B) = 0.90$

At least one of them getting B = $P(A \cup B) = 0.91$

Both getting B = $P(A \cap B) = 0.79$

a] $P(\text{only Harold gets B})$

$$= 0.80 - 0.79$$

$$= 0.1$$

$$= \underline{\underline{10\%}}$$

b] $P(\text{only Sharon gets B})$

$$= 0.90 - 0.79$$

$$= 0.11$$

$$= 11\%$$

$$\underline{\underline{11\%}}$$

(c) $P(\text{Both not getting B})$

$$= 1 - P(A \cup B)$$

$$= 1 - 0.91$$

$$= 0.09$$

$$= \underline{\underline{9\%}}$$

1.3

Jerry goes to the bank $= P(A) = 0.20$

Susan goes to the bank $= P(B) = 0.30$

Together at the Bank $= P(A \cap B) = 0.08$

For event to be Independent

$$P(A/B) = \frac{P(A \cap B)}{P(B)} = P(A)$$

i.e. $P(A \cap B) = P(A) \cdot P(B)$

In this case

$$\begin{aligned} 0.08 &\neq 0.20 \times 0.30 \\ 0.08 &\neq 0.06 \end{aligned}$$

Therefore they are not Independent.

1.4

Two dice are rolled

a)

$P(A) = \text{Sum is } 6$

$$P(S) = 36$$

$$P(A) = \frac{\{(1,5), (2,4), (3,3), (4,2), (5,1)\}}{P(S)}$$

$$P(A) = \boxed{\frac{5}{36}}$$

$$P(B) = \frac{\{(1,5), (2,5), (3,5), (4,5), (5,5), (6,5)\}}{P(S)}$$

$$P(B) = \frac{6}{36} = \boxed{\frac{1}{6}}$$

$$P(A \cap B) = \frac{\{(5,5)\}}{P(S)} = \boxed{\frac{1}{36}}$$

$$P(A) \times P(B) = P(A \cap B) \text{ For events to be independent}$$

$$\frac{5}{36} \times \frac{1}{6} \neq \frac{1}{36}$$

\therefore The events are not Independent.

b)

A: Sum is 7

B: The First die shows '5'

$$P(s) = \underline{\underline{36}}$$

$$P(A) = \frac{\{ (1,6) (2,5) (3,4) (4,3) (5,2) (6,1) \}}{P(s)} \quad P(s)$$

$$P(A) = \frac{6}{36} = \boxed{\frac{1}{6}}$$

$$P(B) = \frac{\{ (5,1) (5,2) (5,3) (5,4) (5,5) (5,6) \}}{P(s)}$$

$$= \frac{6}{36} = \boxed{\frac{1}{6}}$$

$$P(A \cap B) = \frac{\{ (5,2) \}}{P(s)}$$

$$= \boxed{\frac{1}{36}}$$

$$P(A \cap B) = P(A) \times P(B)$$

$$\frac{1}{36} = \frac{1}{6} \times \frac{1}{6}$$

\therefore The events are independent.

1.5

A = Drilling in TX

B = Drilling in AK

C = Drilling in NJ

$$P(A) = 0.60$$

$$P(B) = 0.30$$

$$P(C) = 0.10$$

$$P(\text{oil in TX}) = 0.30$$

$$P(\text{oil in AK}) = 0.20$$

$$P(\text{oil in NJ}) = 0.1$$

$$P(\text{oil in TX} \cap A) = 0.18$$

$$P(\text{oil in AK} \cap B) = 0.06$$

$$P(\text{oil in NJ} \cap C) = 0.01$$

$$1. \quad P(\text{finding oil}) = 0.18 + 0.06 + 0.01$$

$$= 0.25$$

$$= \underline{\underline{25\%}}$$

$$2. \quad P(A | \text{found oil}) = \frac{P(A \cap \text{found oil})}{P(\text{oil found})}$$

$$= \frac{0.18}{0.25} = 0.72$$

$$= \underline{\underline{72\%}}$$

"Including 'new' in passengers"

1.6

$$1. P(\text{Passenger did not survive}) = \frac{1490}{2201}$$

$$= 0.6769$$

$$= 67.69\%$$

$$2. P(\text{Passenger staying in 2nd class})$$

$$= \frac{325}{2201}$$

$$= 0.1476$$

$$= 14.76\%$$

$$3. P(\text{First class} | \text{Passenger survived})$$

$$= \frac{203}{711}$$

$$= 0.2855$$

$$= 28.55\%$$

$$4] P(\text{Survival}) = \frac{711}{2201} = 0.3230 = 32.30\%$$

$$P(\text{First class}) = \frac{325}{2201} = 0.1476 = 14.76\%$$

$$P(\text{Survival} \cap \text{First class}) = \frac{203}{2201} = 0.0922$$

$$= 9.22\%$$

$$P(\text{Survival} \cap \text{First class}) \neq P(A) \cdot P(B)$$

$$9.22$$

$$\neq 32.30 \times 14.76$$

They are not independent.

$$5. P(\text{First class} \cap \text{child} / \text{survived}) = \frac{6}{711}$$

$$= \frac{0.84\%}{1000}$$

$$6. P(\text{Adult} / \text{survived})$$

$$= \frac{654}{711}$$

$$= 91.98\%$$

$$7. P(\text{F.C.} \& \text{survived}) = 0.285$$

$$P(\text{Adults} \& \text{survived}) = 0.919$$

$$P(\text{child} \& \text{survived}) = 0.08$$

$$① P(\text{F.C.} \& \text{survived}) \cap P(\text{Adults} \& \text{survived}) = 0.277$$

$$②. P(\text{F.C.} \& \text{survived}) \cap P(\text{child} \& \text{survived}) = 0.008$$

$$P(\text{Adult} \& \text{survived}) \times P(\text{F.C.} \& \text{survived})$$

$$= 0.919 \times 0.285$$

$$= 0.26 \neq 0.277$$

They are not independent

$$P(\text{child} \& \text{survived}) \cap P(\text{F.C.} \& \text{survived})$$

$$= 0.08 \times 0.285 = 0.02$$

$$\neq ②.$$

Hence the events are not independent.