

19/4/22

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ASSESSMENT

STATISTICS AND PROBABILITY

1) Cards = 52

Diamond = 13

Heart = 13

Spade = 13

$$\text{Required Probability} = \frac{{}^{13}C_1 \times {}^{13}C_1 \times {}^{13}C_1}{{}^{52}C_3}$$

$$= \frac{13 \times 13 \times 13}{52 \times 51 \times 50} = \frac{2197}{132600}$$

$$= 0.016$$

The Probability of getting one card is
diamond, one card is heart and
one card is spade } = 0.016

2) Given

$$P(A) = \text{Action movies} = 42\% \Rightarrow 42/100$$

$$P(B) = \text{Comedy movies} = 54\% \Rightarrow 54/100$$

$$P(C) = \text{Drama movies} = 36\% \Rightarrow 36/100$$

$$P(D) = \text{Horror movies} = 12\% \Rightarrow 12/100$$

$$\begin{aligned} \text{Total Probability} &= P(A) + P(B) + P(C) + P(D) \\ &= 42 + 54 + 36 + 12 \\ &= 144 \end{aligned}$$

$$\boxed{\text{Total Probability} = 144}$$

a) Favorite movie type is either action or drama

$$P(A \cup C) = P(A) + P(C)$$

$$= 42 + 36$$

$$P(A \cup C) = 78$$

b) Favorite movie type is either comedy or horror

$$P(B \cup D) = P(B) + P(D)$$

$$= 54 + 12$$

$$P(B \cup D) = 66$$

b) Given

$$\text{Average} = 350870$$

$$\text{Standard Deviation} = 12405$$

$$75^{\text{th}} \text{ Percentile}(z) = \frac{X - \mu}{\sigma}$$

$$0.675 = \frac{X - 350870}{12405}$$

$$X = (0.675 \times 12405) + 350870$$

$$X = 8373.375 + 350870$$

$$X = 359243.75$$

$$75^{\text{th}} \text{ Percentile} = 359243.75$$

3) Given:

Bag A \rightarrow red ball - 3
black ball - 5

Bag B \rightarrow white ball - 4
black ball - 7

$$P(A) = 1/2$$

$$P\left(\frac{\text{Black ball}}{A}\right) = 5/8$$

$$P(B) = 1/2$$

$$P\left(\frac{\text{Black ball}}{B}\right) = 7/11$$

$$\begin{aligned} P(B/\text{Black Ball}) &= \frac{P(B) \times P\left(\frac{\text{Black ball}}{B}\right)}{P(A) \times P\left(\frac{\text{Black ball}}{A}\right) + P(B) \times P\left(\frac{\text{Black ball}}{B}\right)} \\ &= \frac{1/2 \times 7/11}{(1/2 \times 5/8) + (1/2 \times 7/11)} \\ &= 0.5045 \end{aligned}$$

4) Given

One hour = 450 Application

$$\begin{aligned} \lambda (\text{mean}) &= 450/60 \\ \lambda &= 15/2 \end{aligned}$$

$$x = 10$$

$$P(X=x) = \frac{e^{-15/2} \cdot (15/2)^{10}}{10!} \quad \left| P(X=x) = 0.0858 \right|$$