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basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 10

MATHEMATICS P2

NOVEMBER 2018

MARKS: 100

TIME: 2 hours

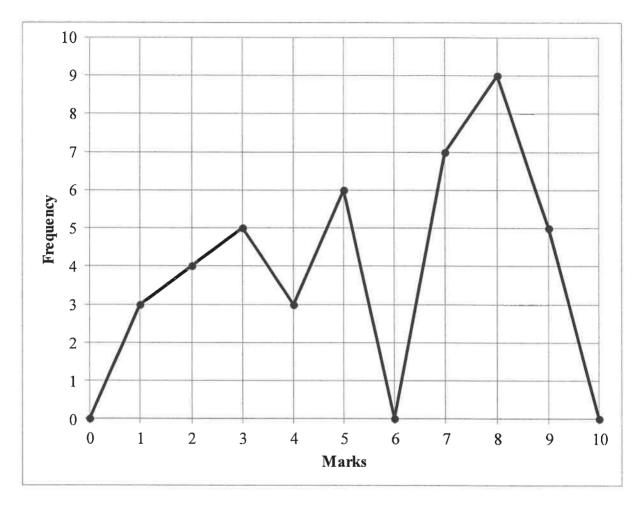
This question paper consists of 9 pages and a 12-page answer book.

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of EIGHT questions.
- 2. Answer ALL the questions in the SPECIAL ANSWER BOOK provided.
- 3. Clearly show ALL calculations, diagrams, graphs, etc. that you used to determine the answers.
- 4. Answers only will NOT necessarily be awarded full marks.
- 5. If necessary, round off answers to TWO decimal places, unless stated otherwise.
- 6. Diagrams are NOT necessarily drawn to scale.
- 7. You must use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
- 8. Write neatly and legibly.

The line graph below shows test marks out of 10 obtained by a Grade 10 class.



1.1 Complete the frequency column in the table provided in the ANSWER BOOK. (2)

1.2 How many learners wrote the test? (1)

1.3 Calculate the:

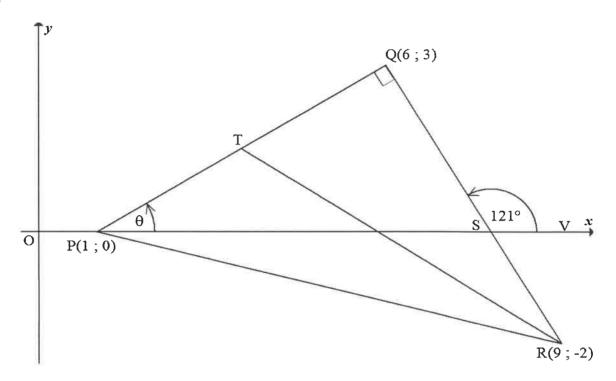
1.3.1 Range for the data (2)

1.3.2 Mean for the test (3)

1.4 Determine the median for the data. (3)

1.5 Draw a box and whisker diagram for the data. (3) [14]

In the diagram below, P(1; 0), Q(6; 3) and R (9; -2) are the vertices of a triangle such that PQ = QR and PQ \perp QR. T is a point on PQ such that T is the midpoint of PQ. S is the point of intersection of RQ and the x-axis. V is a point on the x-axis such that QŜV = 121°. QPS = θ



2.1 Determine the:

2.1.1 Length of PQ. Leave your answer in surd form. (2)

2.1.2 Gradient of PQ (2)

2.1.3 Coordinates of T (2)

2.2 Calculate the:

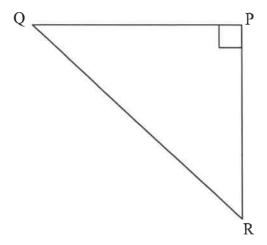
2.2.1 Area of $\triangle QTR$ (3)

2.2.2 Size of θ , with reasons (2)

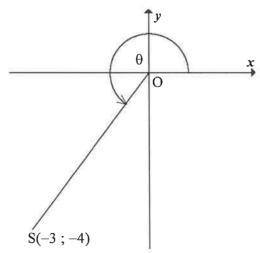
2.2.3 Coordinates of S (3)

2.3 Determine, with reasons, the gradient of the line through T and the midpoint of PR. (3) [17]

3.1 In the diagram below, $\triangle QPR$ is a right-angled triangle with $Q\hat{P}R = 90^{\circ}$.



- 3.1.1 Use the sketch to determine the ratio of $tan(90^{\circ} R)$. (1)
- 3.1.2 Write down the trigonometric ratio that is equal to $\frac{QR}{QP}$. (1)
- S(-3; -4) is a point on the Cartesian plane such that OS makes an angle of θ with the positive x-axis.



Calculate the following WITHOUT using a calculator:

3.2.1 The length of OS (2)

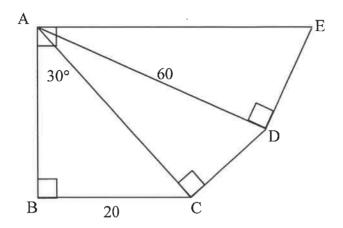
3.2.2 The value of $\sec \theta + \sin^2 \theta$ (3)

3.3 Determine the value of the following WITHOUT using a calculator:

$$\frac{\csc 45^{\circ}}{\sin 90^{\circ}. \tan 60^{\circ}} \tag{4}$$

[11]

In the diagram below, ABC, ACD and ADE are right-angled tirangles. $B\hat{A}E = 90^{\circ}$ and $B\hat{A}C = 30^{\circ}$. BC = 20 units and AD = 60 units.



Calculate the:

4.2 Solve for x, correct to ONE decimal place, where $0^{\circ} \le x \le 90^{\circ}$:

4.2.1
$$\tan x = 2.01$$
 (2)

$$4.2.2 5\cos x + 2 = 4 (3)$$

4.2.3
$$\frac{\csc x}{2} = 3$$
 (3)

QUESTION 5

5.1 Consider the function $f(x) = -3 \tan x$.

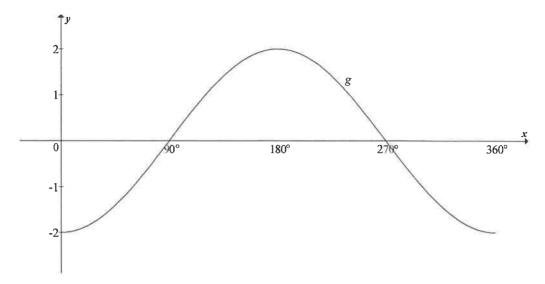
5.1.1 Sketch, on the grid provided in the ANSWER BOOK, the graph of f for $0^{\circ} \le x \le 360^{\circ}$. Clearly show ALL the intercepts and asymptotes. (3)

5.1.2 Hence, or otherwise, write down the:

(a) Period of
$$f$$
 (1)

(b) Equation of h if h is the reflection of f about the x-axis (1)

Sketched below is the graph of $g(x) = a \cdot \cos b\theta$

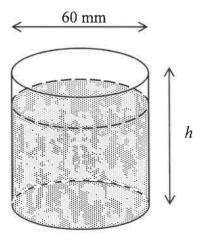


- 5.2.1 Write down the values of a and b. (2)
- 5.2.2 Use the graph to determine the value(s) of x for which g(x) > 0. (1)
- 5.2.3 Determine the range of h if h is the image of g if g is shifted down TWO units. (2)
- 5.2.4 Determine, using the graph, the value of:

$$-2(\cos 0^{\circ} + \cos 1^{\circ} + \cos 2^{\circ} + ... + \cos 358^{\circ} + \cos 359^{\circ} + \cos 360^{\circ})$$
 (2) [12]

QUESTION 6

The diagram below shows a cup with a volume of 117π cm³ and an inner diameter of 60 mm. Ignore the thickness of the cup.



Calculate the:

6.1 Height of the cup (3)

Total surface area of the water that touches the cup if the cup is 80% full with water (4)

[7]

Give reasons for ALL geometry statements in QUESTIONS 7 and 8.

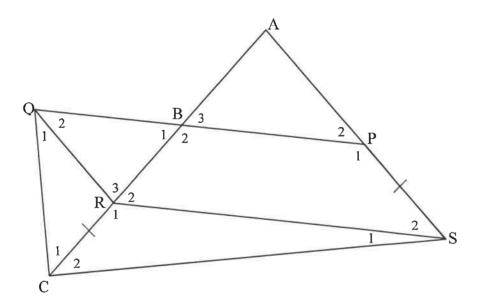
QUESTION 7

7.1 Complete the statement so that it is TRUE:

The line drawn from the midpoint of the one side of a triangle, parallel to the second side, ...

(1)

ACS is a triangle. P is a point on AS and R is a point on AC such that PSRQ is a parallelogram. PQ intersects AC at B such that B is the midpoint of AR. QC is joined. Also, CR = PS, $\hat{C}_1 = 50^{\circ}$ and BP = 60 mm.

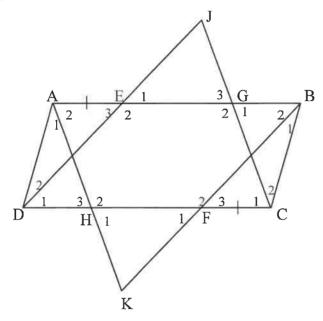


7.2.1 Calculate the size of \hat{A} . (5)

7.2.2 Determine the length of QP. (3)

[9]

8.1 ABCD is a parallelogram. E and F are points on AB and DC respectively such that AE = CF. DE is produced to J and CJ is drawn. BF is produced to K and AK is drawn.

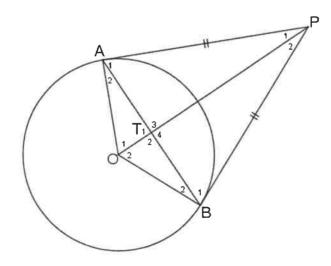


Prove that:

8.1.1 DJ
$$\parallel$$
 BK (5)

8.1.2
$$\hat{E}_1 = \hat{F}_1$$
 (4)

8.2 In the diagram below O is the centre of the circle. A and B lie on the circumference of the circle. AP = BP.



Prove that:

$$8.2.1 \qquad AT = BT \tag{5}$$

8.2.2
$$O\hat{T}A = 90^{\circ}$$
 (1)

[15]

TOTAL: 100