

Privacy-preserving Machine Learning

Machine Learning

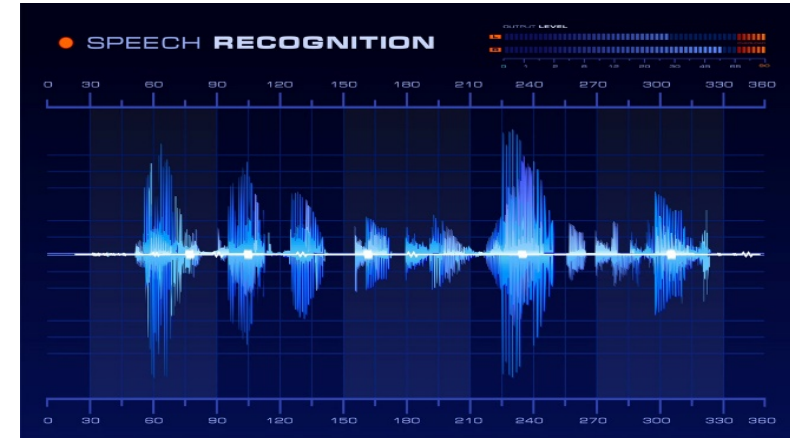
Image processing



Playing Go



Speech recognition

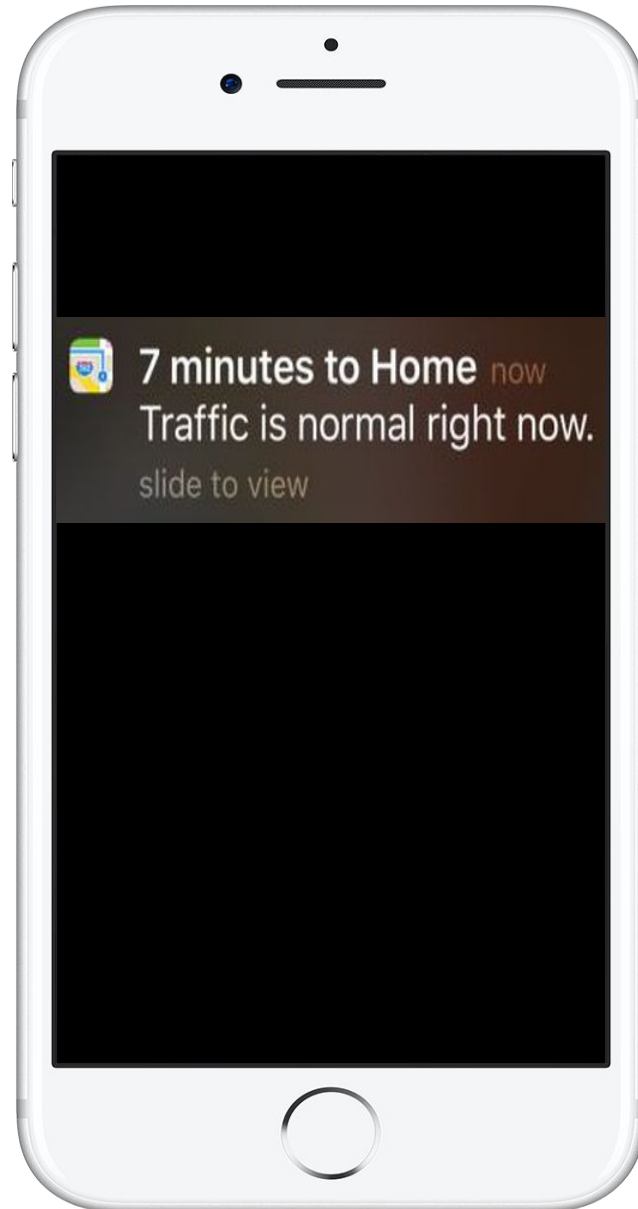


OpenAI



More data → Better Models

Map Predictions



Customized Homepage

Trending



DJ Khaled, Rihanna - Wild Thoughts (2018 Live)

Super Netvid
1.8M views • 23 hours ago



Rey Mysterio makes a shocking return in the Royal Rumble

WWE
4.6M views • 23 hours ago



George W. Bush Returns Cold Open - SNL

Saturday Night Live
4.1M views • 1 day ago



Cardi B Has Butterflies in Her Stomach & Where?! | E! Live

E! Live from the Red Carpet
503K views • 1 day ago



Bruno Mars and Cardi B - Finesse (LIVE From The 60th)

Vevo
2.3M views • 16 hours ago



Basketball - Topic Recommended channel



Most Funny Moments in Sports History • Part 1

Spor Delisi HD
4.7M views • 2 weeks ago



Celebrating Too Early Compilation [funny] (TOP 10)

Top 10 Videos
8M views • 6 months ago



Watts Zap 2018 Best Funny Sports - Part 139

Watts Zap
2.5M views • 1 week ago



5 Times NBA Fans CROSSED THE LINE

Heat Check
4.8M views • 1 month ago



NBA "Immoral" Actions From Fans

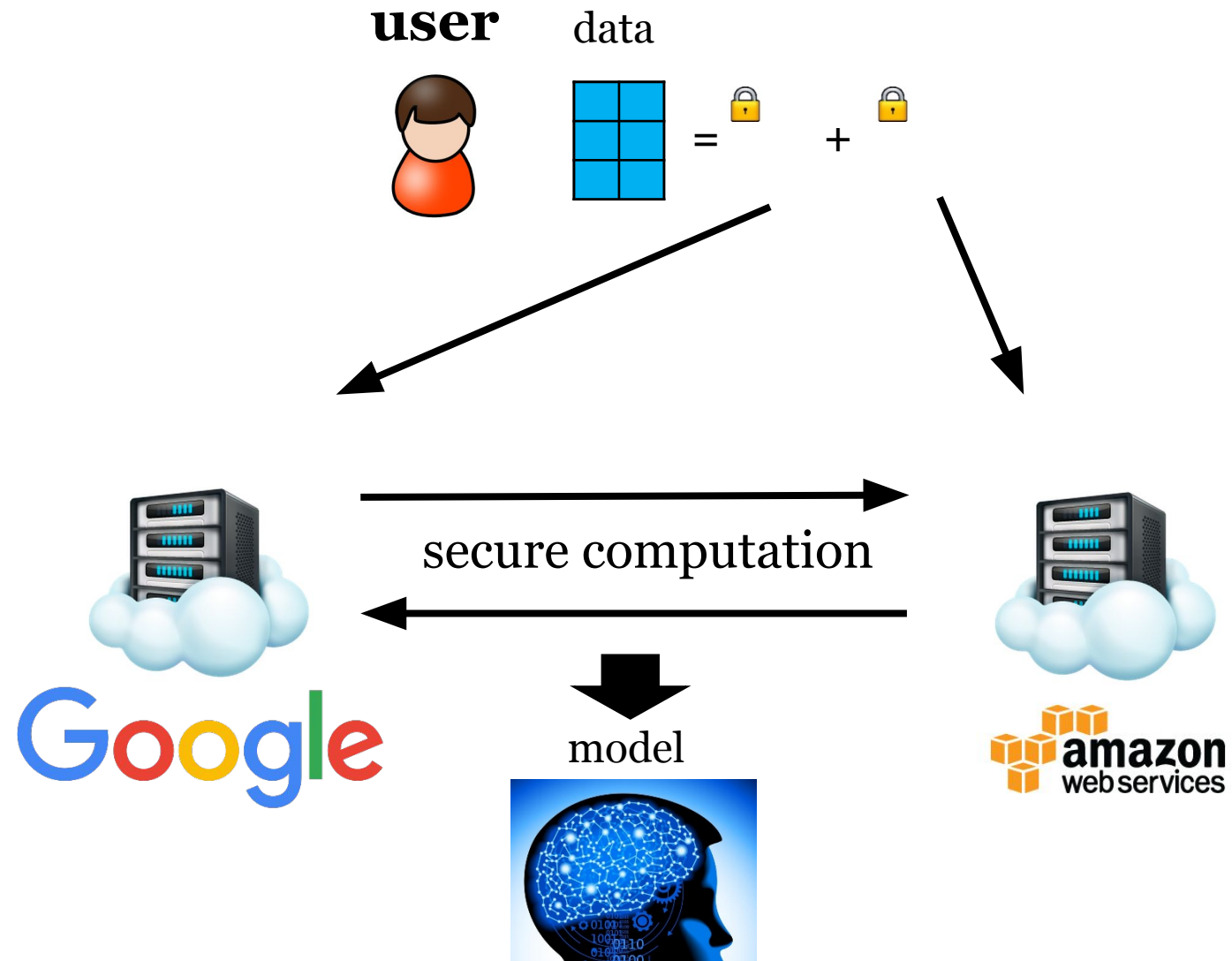
DeeBall
1.6M views • 2 weeks ago

- ✓ Nice machine learning applications benefiting our lives
- × Models trained on sensitive data

Can companies train the models without learning our data



Privacy-preserving Machine Learning



Use Case for Companies: Fraud detection



Card #	Time	Location	Amount
xxxxxxx	8/8/2016	CA, USA	xx.xx
.....			



xxxxxxx	x/xx/xxxx	xx,xxx	xx.xx
.....			

Name	SSN
Alice	xxxxxx
.....	
Alice	xxxxxx
.....	



Use Case for Hospitals



ID	Name	Sex	DOB	Disease xxx
101	Alice	F	1976-2-23	N
102	Bob	M	1992-10-12	N
103	Charlie	M	1983-1-15	N
104	David	M	2005-4-30	Y
...	N

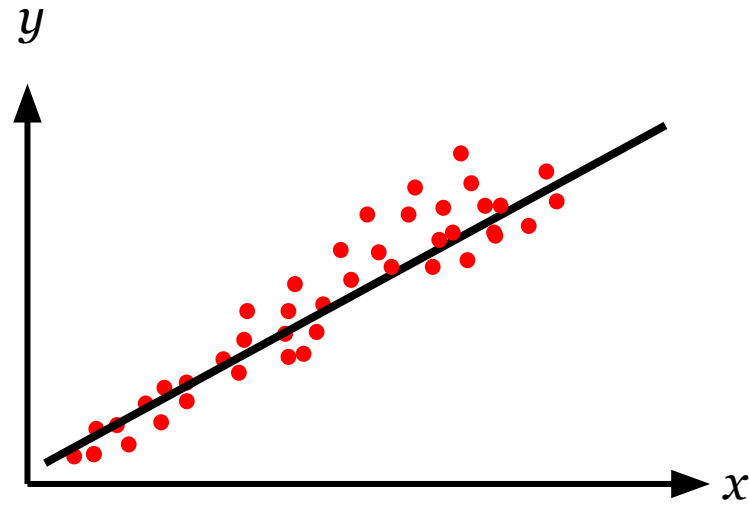


In theory, there is no difference between theory and practice;

In practice, there is.

Linear Regression

Linear Regression



Input: data value pairs (x, y) s

Output: model w

$$y^* = \sum_i w_i x_i = w \cdot x \approx y$$

Cost function (Loss function)

$$y^* = \sum_i w_i x_i = w \cdot x \approx y$$

-

$$C_x(w) = \frac{1}{2} (y^* - y)^2$$

$$C(w) = \frac{1}{n} \sum_x C_x(w)$$

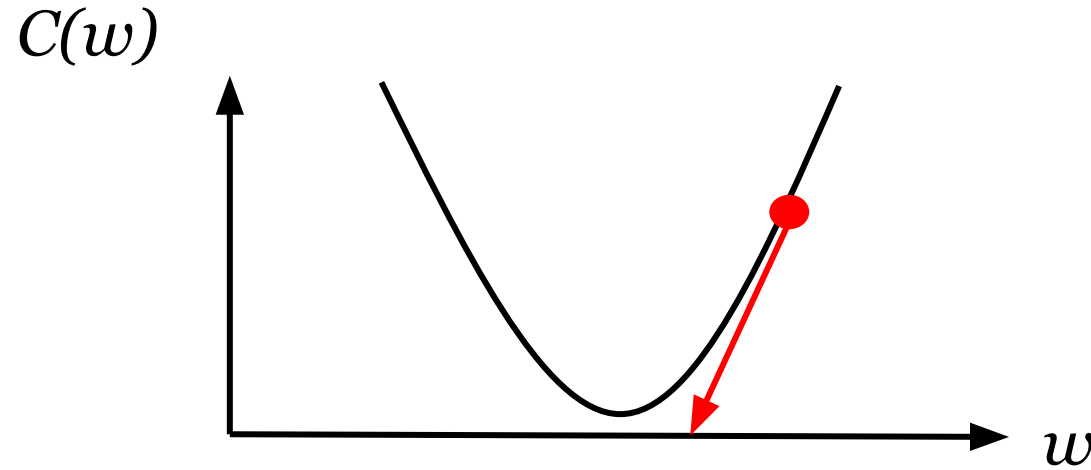
$$\arg \min_w C(w)$$

Closed-form solution for linear regression

- $$w = (X^T X)^{-1} X^T y$$

$O(n^3)$, slow for large datasets

Gradient decent



$$y^* = \sum_i w_i x_i = w \cdot x$$

$$C_x(w) = \frac{1}{2} (y^* - y)^2$$

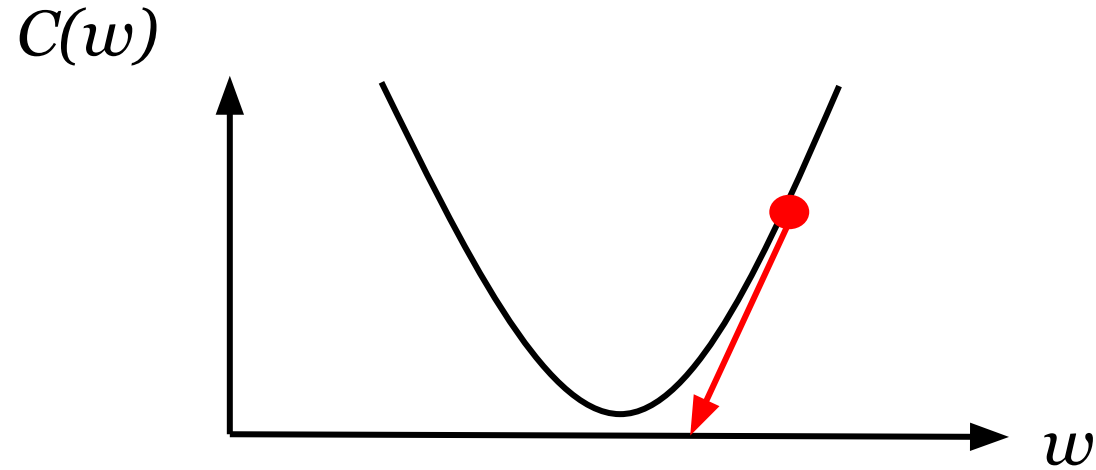
$$C(w) = \frac{1}{n} \sum_x C_x(w)$$

1. Initialize w randomly
2. Compute derivative of $C(w)$
3. Update w

$$w = w - \alpha \frac{1}{n} \sum_x (x \cdot w - y) x$$

$$w_i = w_i - \alpha \frac{1}{n} \sum_x (x \cdot w - y) x_i$$

Stochastic gradient decent (SGD)

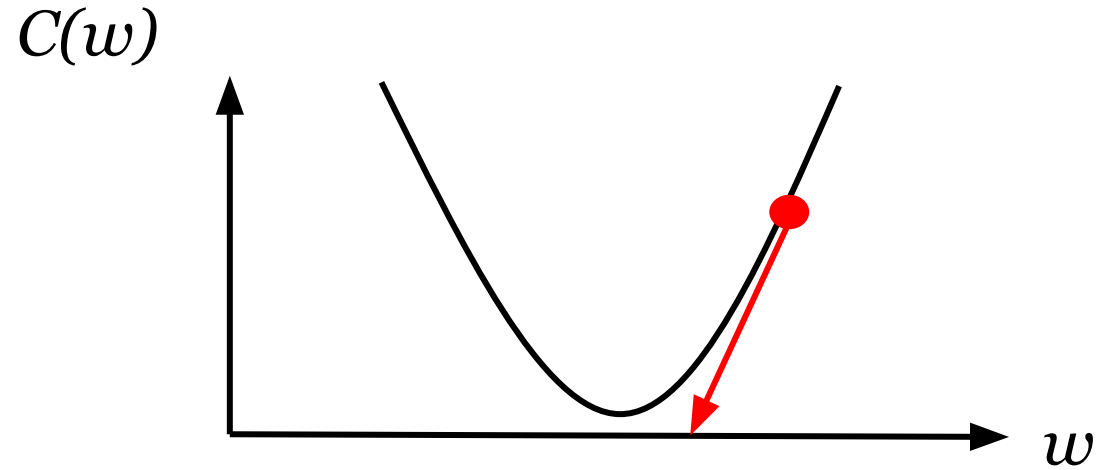


1. Initialize w randomly
2. Select a random sample (x, y) , compute derivative of $C_x(w)$
3. Update w

$$w = w - \alpha(x \cdot w - y)x$$

$$w_i = w_i - \alpha(x \cdot w - y)x_i$$

Mini-batch SGD



1. Initialize w randomly
2. Select a batch of random samples (x, y) , compute derivative
3. Update w

$$w = w - \alpha \frac{1}{|B|} \sum_{x \in B} (x \cdot w - y)x$$

Mini-batch SGD

- Epoch: randomly shuffle all the data, select $|B|$ samples each round
- Vectorization:

$$w = w - \alpha \frac{1}{|B|} \sum_{x \in B} (x \cdot w - y)x$$

$$w = w - \frac{\alpha}{|B|} \cdot X^T \times (X \times w - y)$$

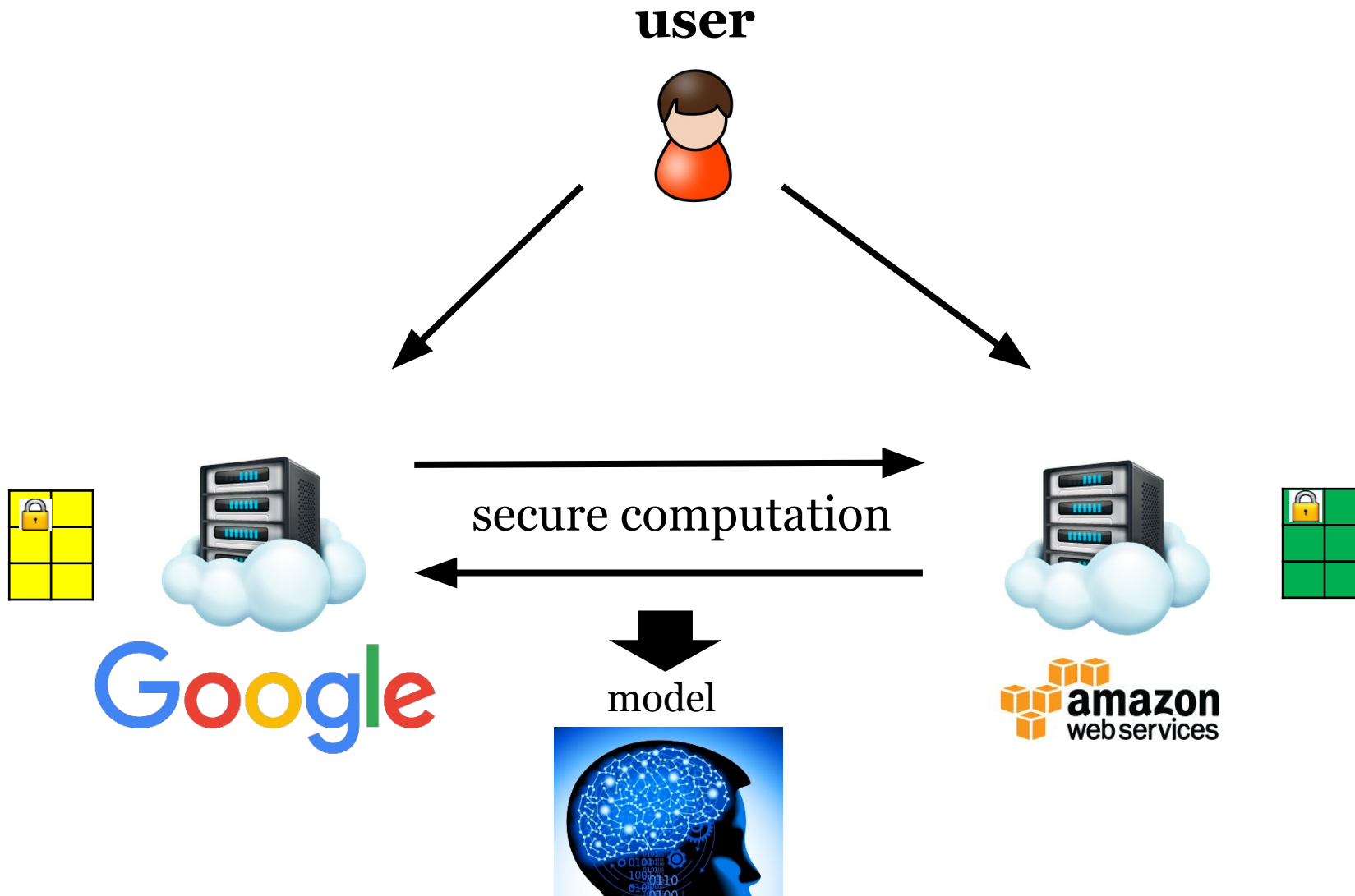
Other variants

$$y^* = \sum_i w_i x_i + b = \mathbf{w} \cdot \mathbf{x} + b$$

Ridge regression: $C_x(w) = \frac{1}{2} (y^* - y)^2 + \lambda ||w||_2^2$

Adaptive learning rate α

Privacy-preserving linear regression



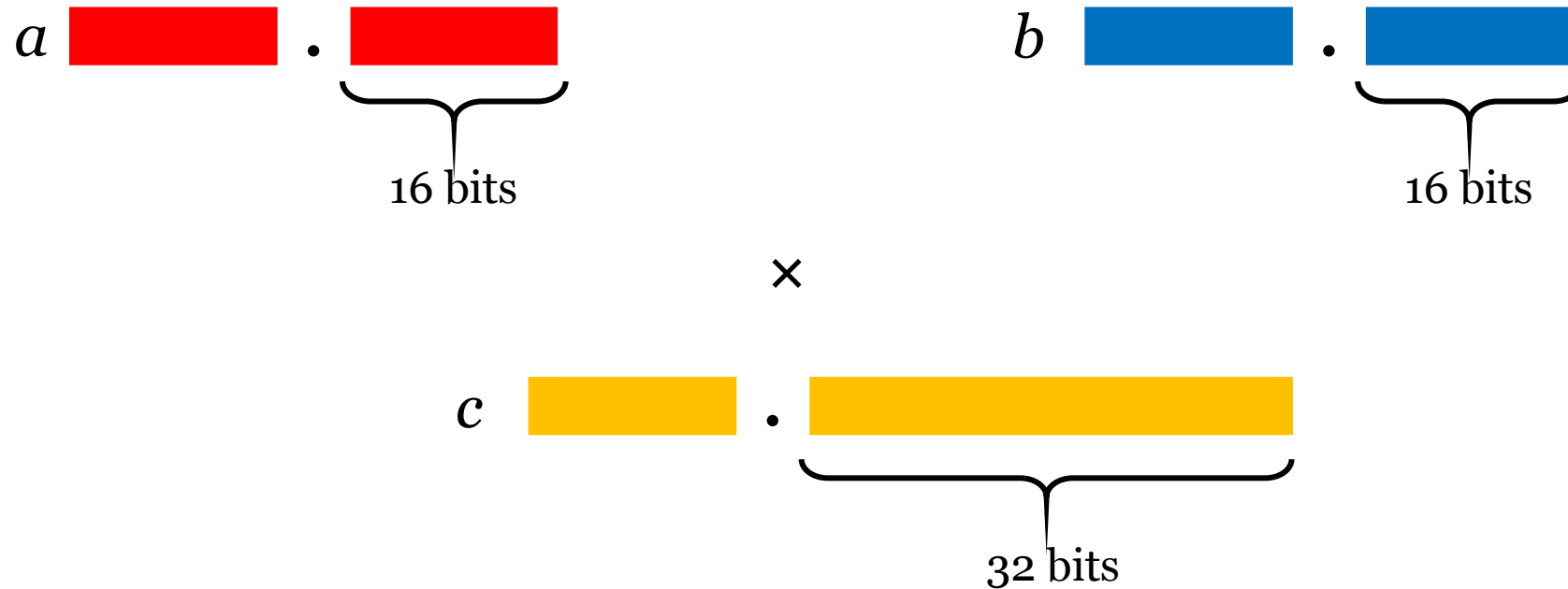
Privacy-preserving linear regression

SGD: $w_i = w_i - \alpha(x \cdot w - y)x_i$

1. Users secret share data and values (x,y)
2. Servers initialize and secret share the model w
3. Run SGD using GMW protocol

Decimal number?

Fixed-point multiplication

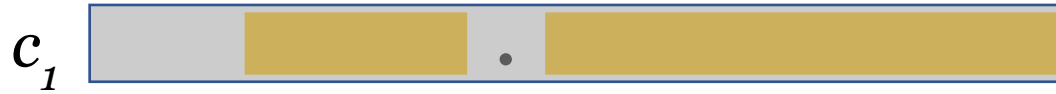


Truncation Same as integer multiplication

- Decimal part grows \rightarrow overflow

fixed-point multiplication

Truncation on shared values



×

Truncation:



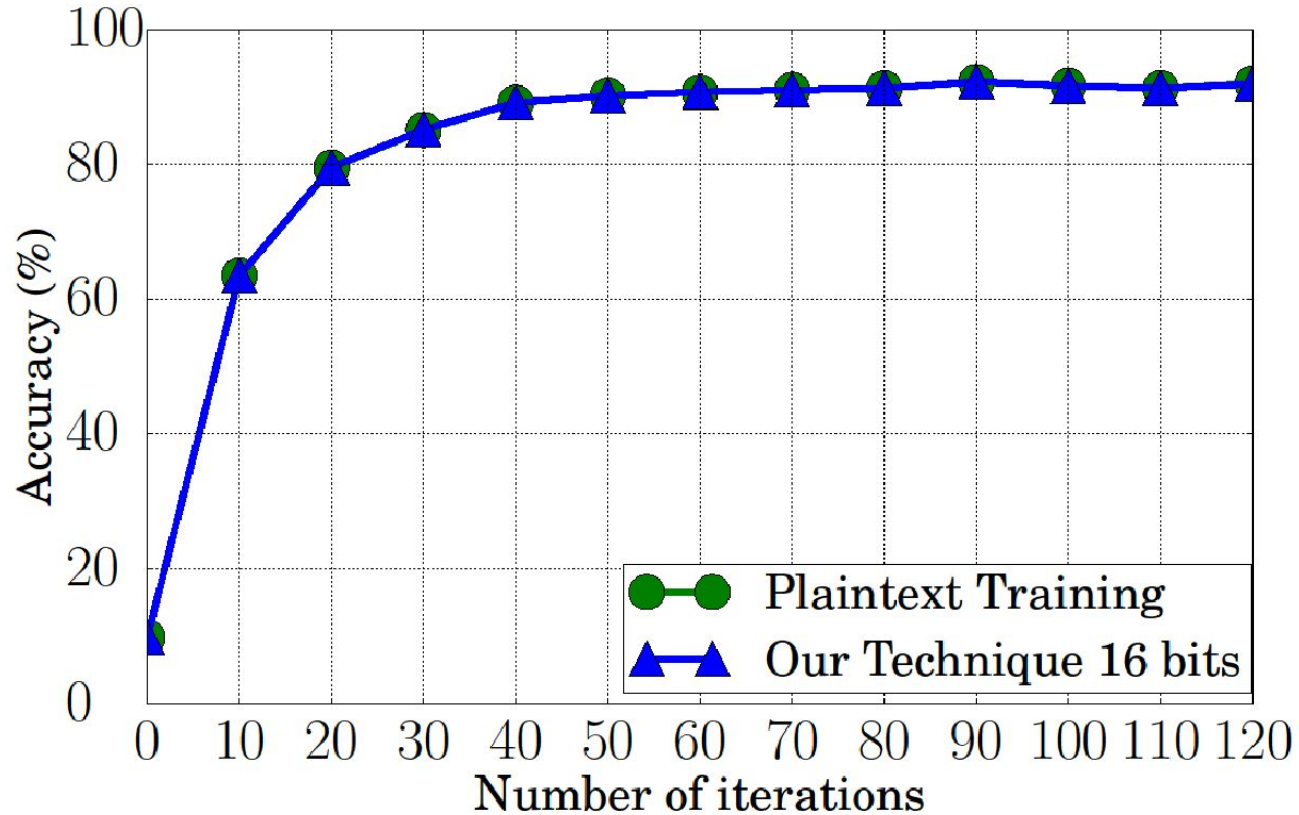
+1, +0 or -1 on the last bit, with high probability

Privacy-preserving linear regression

SGD: $w_i = w_i - \alpha(x \cdot w - y)x_i$

1. Users secret share data and values (x,y)
2. Servers initialize and secret share the model w
3. Run SGD using GMW protocol
4. Truncate the shares after every multiplication

Effects of truncation



- 4-8× faster than fix-point multiplication garbled circuit