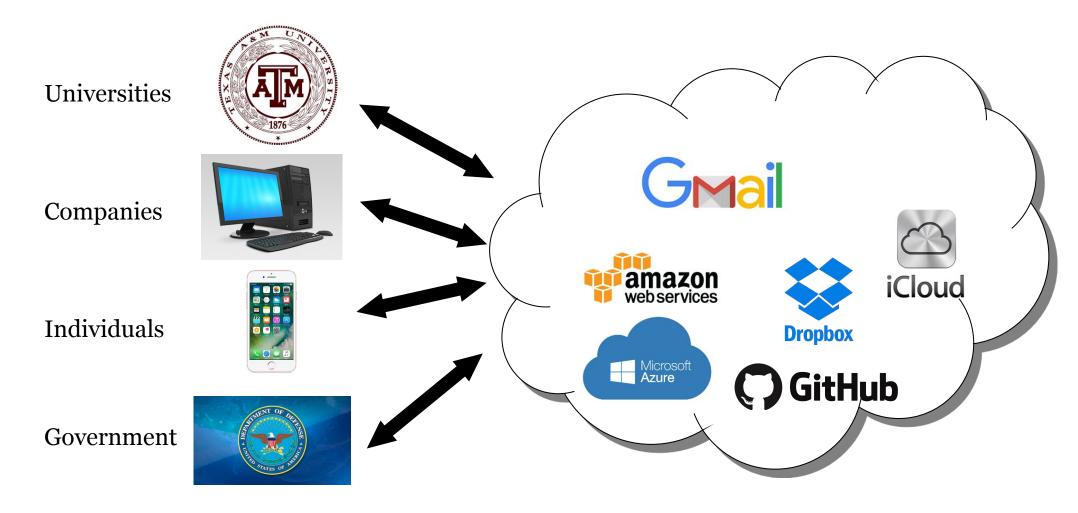
# Searchable Encryption

## **Cloud Computing**



#### Data breaches

#### Data on nearly 200 million US voters exposed in huge GOP contractor leak Storage Server By: Sean Michael Kerner | February 16, 2018

#### FedEx Customer Data Left Publicly Exposed on Cloud

By James Rogers - Published June 20, 2 List of data breaches

s time it's 119,000 documents with FedEx-owned company Bongo

From Wikipedia, the free encyclopedia

For broader coverage of this topic, see Data breach

his is a list of data breaches, using data compiled from various sources, including press reports, government news releases, and mainstream news articles. The list includes those involving the maller breaches occur continually. Breaches of large organizations where the number of records is still unknown are also listed. The various methods used in the breaches are also listed, with ha

Most breaches occur in North America. It is estimated that the average cost of a data breach will be over \$150 million by 2020, with the global annual cost forecast to be \$2.1 trillion.[1][2] It is estim exposed as a result of data breaches.[3] In 2019, a collection of 2.7 billion identity records, consisting of 774 million unique email addresses and 21 million unique passwords, was posted on the w

| HOTOTOTOTOTOTOTOTOTOTOTOTOTO                     | Entity                                | Year ▼ | Records +        | Organization type •       | Method ♦                 | Sources \$   |
|--|---------------------------------------|--------|------------------|---------------------------|--------------------------|--------------|
| HO TO        | 2019 Bulgarian revenue agency hack    | 2019   | over 5,000,000   | government                | hacked                   | [54]         |
| 0101010101000000000000001                        | Canva                                 | 2019   | 140,000,000      | web                       | hacked                   | [56][57][58] |
| 0101010101001001001001001001001001010101         | Capital One                           | 2019   | 106,000,000      | financial                 | hacked                   | [59][60]     |
| 010100101000000000000000000000000000000          | Desjardins                            | 2019   | 2,900,000        | financial                 | inside job               | [89]         |
| 10100101010101010101010101010101010              | Facebook                              | 2019   | 540,000,000      | social network            | poor security            | [121]        |
| 01010101010010100101010101010010                 | Facebook                              | 2019   | 1,500,000        | social network            | accidentally uploaded    | [122]        |
| Picture illustration. (REUTERS/Pawel Kopczynski) | First American Corporation            | 2019   | 885,000,000      | financial service company | poor security            | [124]        |
| 010100101010010100000000101001                   | Health Sciences Authority (Singapore) | 2019   | 808,000          | healthcare                | poor security            | [151]        |
|  | Justdial                              | 2019   | 100,000,000      | local search              | unprotected api          | [170]        |
| The personal details of nearly 200               | Ministry of Health (Singapore)        | 2019   | 14,200           | healthcare                | poor security/inside job | [196][197]   |
| exposed in the largest U.S. leak of              | Quest Diagnostics                     | 2019   | 11,900,000       | Clinical Laboratory       | poor security            | [223]        |
|  | StockX                                | 2019   | 6,800,000        | retail                    | hacked                   | [255]        |
|  | Truecaller                            | 2019   | 299,055,819      | Telephone directory       | unknown                  | [277][278]   |
| Information on more than 198 mill                | Woodruff Arts Center                  | 2019   | unknown          | arts group                | poor security            | [314]        |
| the Internet by a firm working on b              | Westpac                               | 2019   | 98,000           | financial                 | hacked                   | [329]        |
| Committee (RNC) in their efforts t               | Australian National University        | 2019   | 19 years of data | academic                  | hacked                   | [330]        |
|  | AerSery (subsidiary of InMobi)        | 2018   | 75,000           | advertising               | hacked                   | [13]         |
| Vickery, a cyber-risk researcher a               | Air Canada                            | 2018   | 20,000           | transport                 | hacked                   | [15]         |
|  | Bell Canada                           | 2018   | 100,000          | telecoms                  | hacked                   | [42]         |
|  | Bethesda Game Studios                 | 2018   |                  | gaming                    | accidentally published   | [44]         |
|  | Blank Media Games                     | 2018   | 7,633,234        | gaming                    | hacked                   | [45][46]     |
|  | BMO and Simplii                       | 2018   | 90,000           | banking                   | poor security            | [50]         |
|  | British Airways                       | 2018   | 380,000          | transport                 | hacked                   | [51][52]     |
|  | Cathay Pacific Airways                | 2018   | 9,400,000        | transport                 | hacked                   | [63]         |



#### **AMERICA**

#### Watchdog: Hillary Clinton Violated State Dept. Policies By Using Private Email

May 25, 2016 · 1:09 PM ET

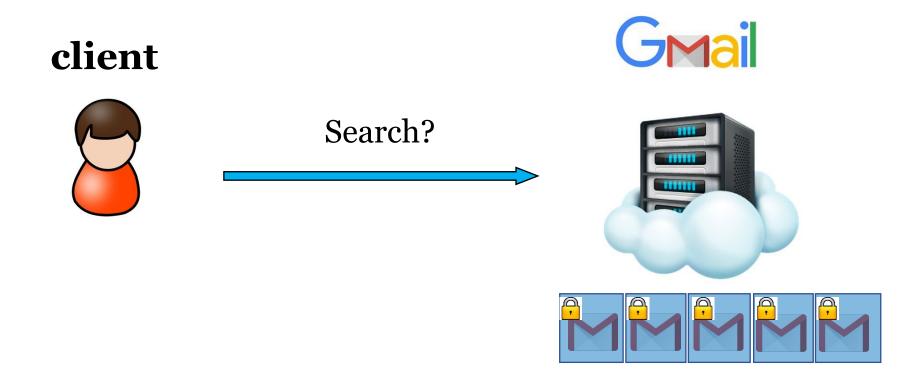




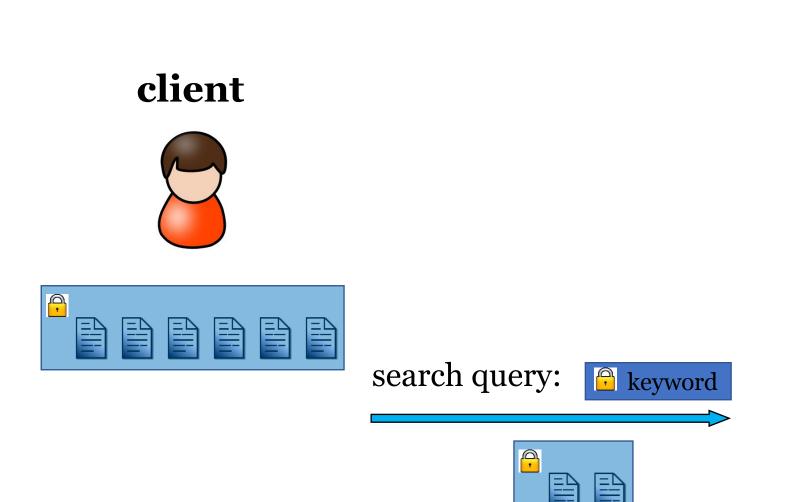
Democratic presidential candidate Hillary Clinton speaks at an International Brotherhood of Electrical Workers training center on Tuesday in Commerce, Calif.

John Locher/AP

### Is encryption enough?



#### Searchable symmetric encryption (SSE)







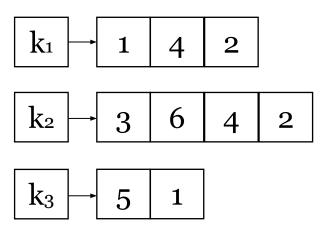


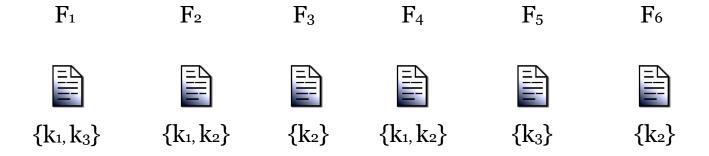
# MPC, fully homomorphic encryption (FHE) and oblivious RAM (ORAM)

Solves the problem in theory, but too slow

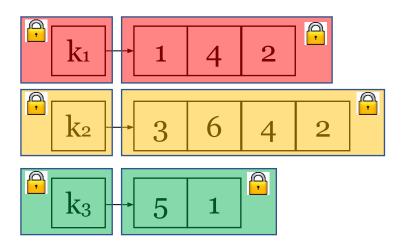
#### Static SSE

#### Inverted index





Pseudo random function:

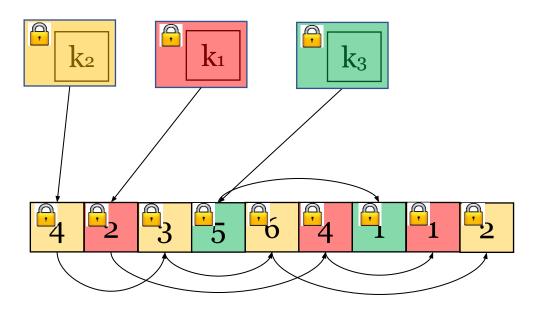


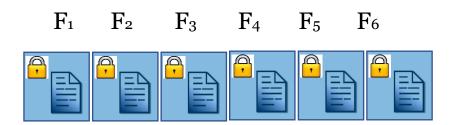
Encryption:

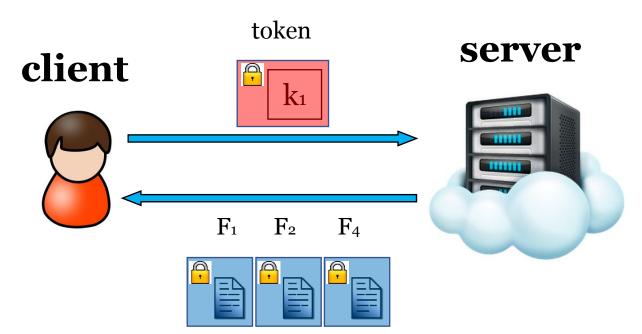


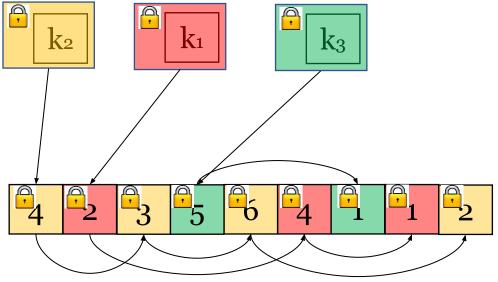
 $F_6$ 

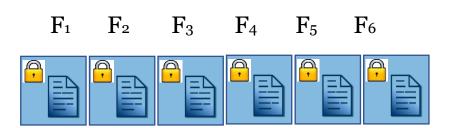
 $F_1$   $F_2$   $F_3$   $F_4$   $F_5$ 











#### Advantage

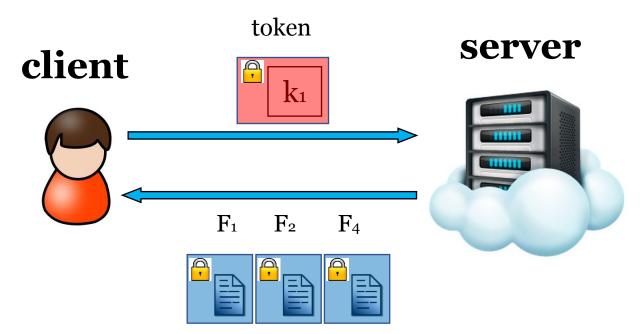
• Super efficient in practice. Encrypt and PRF are not bottleneck.

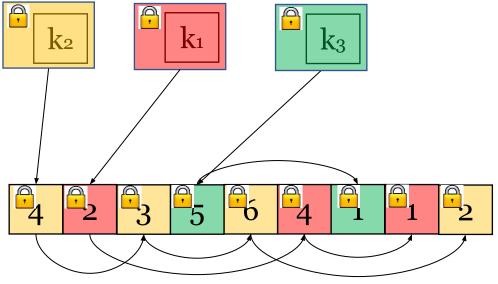
People are looking at locality

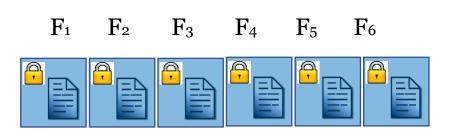
### Leakage

• Search pattern leakage: token is generated from keyword deterministically

#### deterministic!





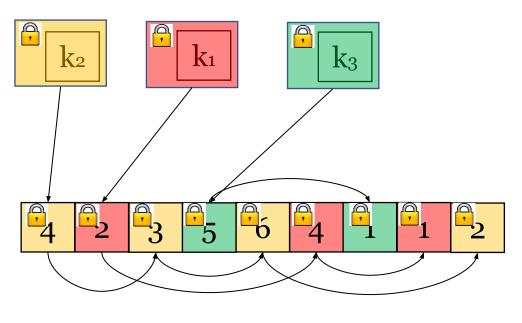


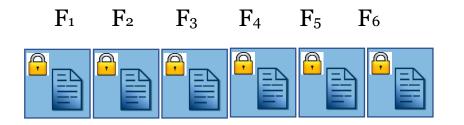
#### Leakage

• Search pattern leakage: token is generated from keyword deterministically

• Access pattern leakage: whether a file is returned

#### deterministic! token server client 111111 $\mathbf{F}_{1}$ $F_2$ $F_4$





file access patterns!

#### Leakage

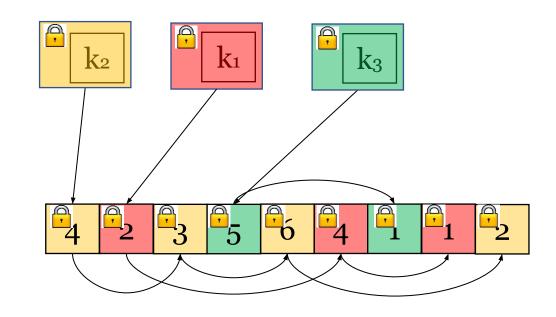
• Search pattern leakage: token is generated from keyword deterministically

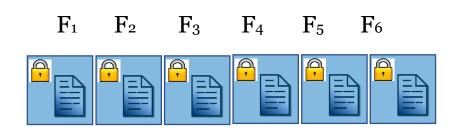
• Access pattern leakage: whether a file is returned

Different from MPC!

#### Security definitions

- $\Delta = (w_1, ..., w_d)$  : keywords set
- $\mathbf{D} = (D_1, \dots, D_n)$ : documents set
- $\mathbf{D}(w)$ : search result for w
- $K \leftarrow Gen(1^k)$
- $(I, c) \leftarrow Enc(K, \mathbf{D})$
- $t \leftarrow \operatorname{Trpdr}(K, w)$
- $X \leftarrow Search(I, t)$
- $D_i \leftarrow \text{Dec}(K, c_i)$





#### Correctness

An index-based SSE scheme is correct if for all  $k \in \mathbb{N}$ , for all K output by  $\text{Gen}(1^k)$ , for all  $\mathbf{D} \subseteq 2^{\Delta}$ , for all  $(I, \mathbf{c})$  output by  $\text{Enc}_K(\mathbf{D})$ , for all  $w \in \Delta$ ,

$$\mathsf{Search}\big(I,\mathsf{Trpdr}_K(w)\big) = \mathbf{D}(w) \bigwedge \mathsf{Dec}_K(c_i) = D_i, \ \textit{for} \ 1 \leq i \leq n.$$

- $\Delta = (w_1, ..., w_d)$  : keywords set
- $\mathbf{D} = (D_1, ..., D_n)$ : documents set
- $\mathbf{D}(w)$ : search result for w
- $K \leftarrow Gen(1^k)$
- $(I, c) \leftarrow Enc(K, \mathbf{D})$
- $t \leftarrow \operatorname{Trpdr}(K, w)$
- $X \leftarrow Search(I, t)$
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### Soundness/security

**Definition 4.2** (History). Let  $\Delta$  be a dictionary and  $\mathbf{D} \subseteq 2^{\Delta}$  be a document collection over  $\Delta$ . A q-query history over  $\mathbf{D}$  is a tuple  $H = (\mathbf{D}, \mathbf{w})$  that includes the document collection  $\mathbf{D}$  and a vector of q keywords  $\mathbf{w} = (w_1, \dots, w_q)$ .

**Definition 4.3** (Access Pattern). Let  $\Delta$  be a dictionary and  $\mathbf{D} \subseteq 2^{\Delta}$  be a document collection over  $\Delta$ . The access pattern induced by a q-query history  $H = (\mathbf{D}, \mathbf{w})$ , is the tuple  $\alpha(H) = (\mathbf{D}(w_1), \dots, \mathbf{D}(w_q))$ .

**Definition 4.4** (Search Pattern). Let  $\Delta$  be a dictionary and  $\mathbf{D} \subseteq 2^{\Delta}$  be a document collection over  $\Delta$ . The search pattern induced by a q-query history  $H = (\mathbf{D}, \mathbf{w})$ , is a symmetric binary matrix  $\sigma(H)$  such that for  $1 \leq i, j \leq q$ , the element in the  $i^{th}$  row and  $j^{th}$  column is 1 if  $w_i = w_j$ , and 0 otherwise.

- $\Delta = (w_1, ..., w_d)$  : keywords set
- $\mathbf{D} = (D_1, \dots, D_n)$ : documents set
- $\mathbf{D}(w)$ : search result for w
- $K \leftarrow Gen(1^k)$
- $(I, c) \leftarrow Enc(K, \mathbf{D})$
- $t \leftarrow \text{Trpdr}(K, w)$
- $X \leftarrow Search(I, t)$
- $D_i \leftarrow \text{Dec}(K, c_i)$

### Soundness/security

**Definition 4.5** (Trace). Let  $\Delta$  be a dictionary and  $\mathbf{D} \subseteq 2^{\Delta}$  be a document collection over  $\Delta$ . The trace induced by a q-query history  $H = (\mathbf{D}, \mathbf{w})$ , is a sequence  $\tau(H) = (|D_1|, \dots, |D_n|, \alpha(H), \sigma(H))$  comprised of the lengths of the documents in  $\mathbf{D}$ , and the access and search patterns induced by H.

Throughout this work, we will assume that the dictionary  $\Delta$  and the trace are such that all histories H over  $\Delta$  are non-singular as defined below.

**Definition 4.6** (Non-singular history). We say that a history H is non-singular if (1) there exists at least one history  $H' \neq H$  such that  $\tau(H) = \tau(H')$ ; and if (2) such a history can be found in polynomial-time given  $\tau(H)$ .

- $\Delta = (w_1, ..., w_d)$  : keywords set
- $\mathbf{D} = (D_1, ..., D_n)$ : documents set
- $\mathbf{D}(w)$ : search result for w
- $K \leftarrow Gen(1^k)$
- $(I, c) \leftarrow Enc(K, \mathbf{D})$
- $t \leftarrow \text{Trpdr}(K, w)$
- $X \leftarrow Search(I, t)$
- $D_i \leftarrow \text{Dec}(K, c_i)$

#### Soundness/security

**Definition 4.7** (Non-adaptive indistinguishability). Let SSE = (Gen, Enc, Trpdr, Search, Dec) be an index-based SSE scheme over a dictionary  $\Delta$ ,  $k \in \mathbb{N}$  be the security parameter, and  $A = (A_1, A_2)$  be a non-uniform adversary and consider the following probabilistic experiment  $\mathbf{Ind}_{\mathsf{SSE},A}(k)$ :

Ind<sub>SSE,A</sub>(k)  

$$K \leftarrow \text{Gen}(1^k)$$
  
 $(st_A, H_0, H_1) \leftarrow A_1(1^k)$   
 $b \stackrel{\$}{\leftarrow} \{0, 1\}$   
 $parse\ H_b\ as\ (\mathbf{D}_b, \mathbf{w}_b)$   
 $(I_b, \mathbf{c}_b) \leftarrow \text{Enc}_K(\mathbf{D}_b)$   
 $for\ 1 \le i \le q,$   
 $t_{b,i} \leftarrow \text{Trpdr}_K(w_{b,i})$   
 $let\ \mathbf{t}_b = (t_{b,1}, \dots, t_{b,q})$   
 $b' \leftarrow A_2(st_A, I_b, \mathbf{c}_b, \mathbf{t}_b)$   
 $if\ b' = b,\ output\ 1$   
 $otherwise\ output\ 0$ 

with the restriction that  $\tau(H_0) = \tau(H_1)$ , and where  $st_A$  is a string that captures  $A_1$ 's state. We say that SSE is secure in the sense of non-adaptive indistinguishability if for all polynomial-size adversaries  $A = (A_1, A_2)$ ,

$$\Pr\left[\mathbf{Ind}_{\mathsf{SSE},\mathcal{A}}(k) = 1\right] \leq \frac{1}{2} + \mathsf{negl}(k),$$

where the probability is taken over the choice of b and the coins of Gen and Enc.

- $\Delta = (w_1, ..., w_d)$  : keywords set
- $\mathbf{D} = (D_1, \dots, D_n)$ : documents set
- $\mathbf{D}(w)$ : search result for w
- $K \leftarrow Gen(1^k)$
- $(I, c) \leftarrow Enc(K, \mathbf{D})$
- $t \leftarrow \text{Trpdr}(K, w)$
- $X \leftarrow Search(I, t)$
- $D_i \leftarrow \text{Dec}(K, c_i)$

#### Simulation-based security definition

**Definition 4.8** (Non-adaptive semantic security). Let SSE = (Gen, Enc, Trpdr, Search, Dec) be an index-based SSE scheme,  $k \in \mathbb{N}$  be the security parameter,  $\mathcal{A}$  be an adversary,  $\mathcal{S}$  be a simulator and consider the following probabilistic experiments:

$$\begin{aligned} & \mathbf{Real}_{\mathsf{SSE},\mathcal{A}}(k) \\ & K \leftarrow \mathsf{Gen}(1^k) \\ & (st_{\mathcal{A}}, H) \leftarrow \mathcal{A}(1^k) \\ & parse \ H \ as \ (\mathbf{D}, \, \boldsymbol{w}) \\ & (I, \, \boldsymbol{c}) \leftarrow \mathsf{Enc}_K(\mathbf{D}) \\ & for \ 1 \leq i \leq q, \\ & t_i \leftarrow \mathsf{Trpdr}_K(w_i) \\ & let \ \boldsymbol{t} = (t_1, \dots, t_q) \\ & output \ \forall = (I, \, \boldsymbol{c}, \, \boldsymbol{t}) \ and \ st_{\mathcal{A}} \end{aligned}$$

We say that SSE is semantically secure if for all polynomial-size adversaries A, there exists a polynomial-size simulator S such that for all polynomial-size distinguishers D,

$$\left|\Pr\left[\left.\mathcal{D}(\mathbf{V}, st_{\mathcal{A}}) = 1: (\mathbf{V}, st_{\mathcal{A}}) \leftarrow \mathbf{Real}_{\mathsf{SSE}, \mathcal{A}}(k)\right.\right] - \Pr\left[\left.\mathcal{D}(\mathbf{V}, st_{\mathcal{A}}) = 1: (\mathbf{V}, st_{\mathcal{A}}) \leftarrow \mathbf{Sim}_{\mathsf{SSE}, \mathcal{A}, \mathcal{S}}(k)\right.\right]\right| \leq \mathsf{negl}(k),$$

where the probabilities are over the coins of Gen and Enc.

- $\Delta = (w_1, ..., w_d)$  : keywords set
- $\mathbf{D} = (D_1, \dots, D_n)$ : documents set
- $\mathbf{D}(w)$ : search result for w
- $K \leftarrow Gen(1^k)$
- $(I, c) \leftarrow Enc(K, \mathbf{D})$
- $t \leftarrow \text{Trpdr}(K, w)$
- $X \leftarrow Search(I, t)$
- $D_i \leftarrow \text{Dec}(K, c_i)$

#### Non-adaptive vs. adaptive

**Definition 4.7** (Non-adaptive indistinguishability). Let SSE = (Gen, Enc, Trpdr, Search, Dec) be an index-based SSE scheme over a dictionary  $\Delta$ ,  $k \in \mathbb{N}$  be the security parameter, and  $A = (A_1, A_2)$  be a non-uniform adversary and consider the following probabilistic experiment  $\mathbf{Ind}_{\mathsf{SSE},A}(k)$ :

$$\begin{aligned} &\mathbf{Ind}_{\mathsf{SSE},\mathcal{A}}(k) \\ &K \leftarrow \mathsf{Gen}(1^k) \\ &(st_{\mathcal{A}}, H_0, H_1) \leftarrow \mathcal{A}_1(1^k) \\ &b \overset{\$}{\leftarrow} \{0, 1\} \\ &parse \ H_b \ as \ (\mathbf{D}_b, \mathbf{w}_b) \\ &(I_b, \mathbf{c}_b) \leftarrow \mathsf{Enc}_K(\mathbf{D}_b) \\ &for \ 1 \leq i \leq q, \\ &t_{b,i} \leftarrow \mathsf{Trpdr}_K(w_{b,i}) \\ &let \ t_b = (t_{b,1}, \dots, t_{b,q}) \\ &b' \leftarrow \mathcal{A}_2(st_{\mathcal{A}}, I_b, \mathbf{c}_b, t_b) \\ &if \ b' = b, \ output \ 1 \\ &otherwise \ output \ 0 \end{aligned}$$

with the restriction that  $\tau(H_0) = \tau(H_1)$ , and where  $st_A$  is a string that captures  $A_1$ 's state. We say that SSE is secure in the sense of non-adaptive indistinguishability if for all polynomial-size adversaries  $A = (A_1, A_2)$ ,

$$\Pr\left[\mathbf{Ind}_{\mathsf{SSE},\mathcal{A}}(k) = 1\right] \leq \frac{1}{2} + \mathsf{negl}(k),$$

where the probability is taken over the choice of b and the coins of Gen and Enc.

**Definition 4.10** (Adaptive indistinguishability security for SSE). Let SSE = (Gen, Enc, Trpdr, Search, Dec) be an index-based SSE scheme,  $k \in \mathbb{N}$  be a security parameter,  $\mathcal{A} = (\mathcal{A}_0, \dots, \mathcal{A}_{q+1})$  be such that  $q \in \mathbb{N}$  and consider the following probabilistic experiment  $\mathbf{Ind}^*_{\mathcal{A},\mathsf{SSE}}(k)$ :

$$\begin{split} & \operatorname{Ind}^{\star}_{\mathsf{SSE},\mathcal{A}}(k) \\ & K \leftarrow \operatorname{Gen}(1^k) \\ & b \overset{\$}{\leftarrow} \{0,1\} \\ & (st_{\mathcal{A}}, \mathbf{D}_0, \mathbf{D}_1) \leftarrow \mathcal{A}_0(1^k) \\ & (I_b, \boldsymbol{c}_b) \leftarrow \operatorname{Enc}_K(\mathbf{D}_b) \\ & (st_{\mathcal{A}}, w_{0,1}, w_{1,1}) \leftarrow \mathcal{A}_1(st_{\mathcal{A}}, I_b) \\ & t_{b,1} \leftarrow \operatorname{Trpdr}_K(w_{b,1}) \\ & for \ 2 \leq i \leq q, \\ & (st_{\mathcal{A}}, w_{0,i}, w_{1,i}) \leftarrow \mathcal{A}_i(st_{\mathcal{A}}, I_b, \boldsymbol{c}_b, t_{b,1}, \dots, t_{b,i-1}) \\ & t_{b,i} \leftarrow \operatorname{Trpdr}_K(w_{b,i}) \\ & let \ t_b = (t_{b,1}, \dots, t_{b,q}) \\ & b' \leftarrow \mathcal{A}_{q+1}(st_{\mathcal{A}}, I_b, \boldsymbol{c}_b, t_b) \\ & if \ b' = b, \ output \ 1 \\ & otherwise \ output \ 0 \end{split}$$

with the restriction that  $\tau(\mathbf{D}_0, w_{0,1}, \dots, w_{0,q}) = \tau(\mathbf{D}_1, w_{1,1}, \dots, w_{1,q})$  and where  $st_{\mathcal{A}}$  is a string that captures  $\mathcal{A}$ 's state. We say that SSE is secure in the sense of adaptive indistinguishability if for all polynomial-size adversaries  $\mathcal{A} = (\mathcal{A}_0, \dots, \mathcal{A}_{q+1})$  such that  $q = \mathsf{poly}(k)$ ,

$$\Pr\left[\mathbf{Ind^{\star}}_{\mathsf{SSE},\mathcal{A}}(k) = 1\right] \leq \frac{1}{2} + \mathsf{negl}(k),$$

where the probability is over the choice of b, and the coins of Gen and Enc.

### SSE with adaptive security

I: lookup table for k,j instead of k

