

## Z transforms.

→ Convert discrete signal to Continuous signal.

→ Denoted by -

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) \cdot z^{-n}$$

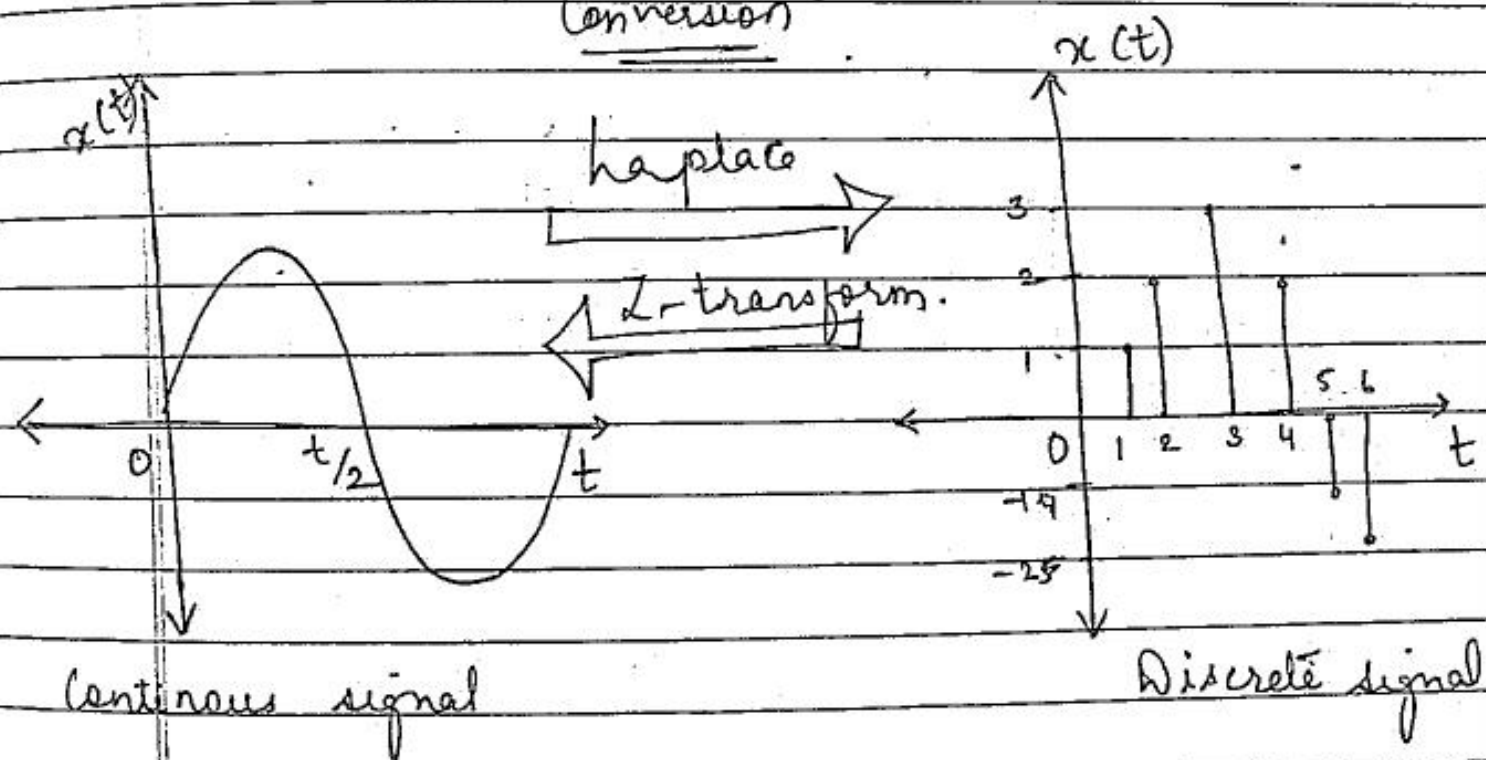
where  $X(z) \rightarrow$  Z transformed signal (s/p)

$x(n) \rightarrow$  discrete signal (i/p)

$z^{-n} \rightarrow$  complex variable.

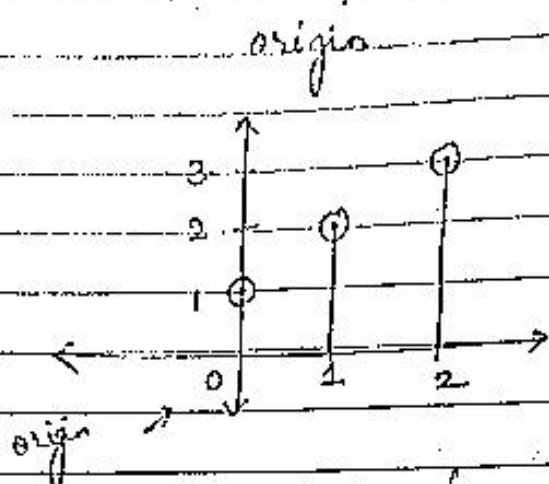
all of above continues for  $n = -\infty$  to  $\infty$ .

### Conversion



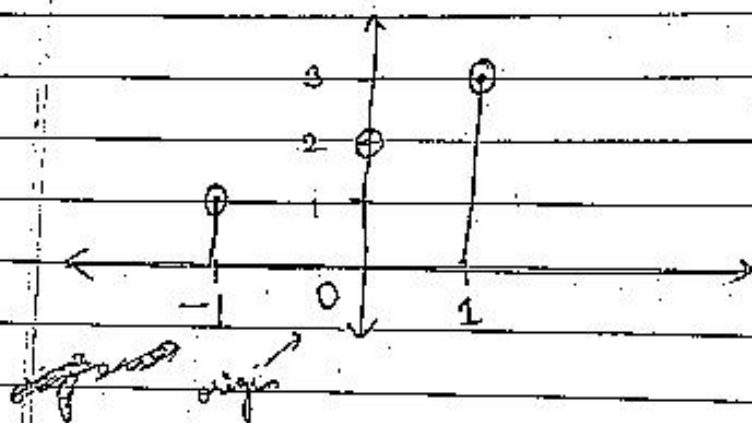
→ Types of Z transform.

Ex:  $x(n) = \{1, 2, 3\}$



∵ since signal is only in 1 quadrant it is a 'Unilateral signal'.

Similarly if  $x(n) = \{1, 2, 3\}$



∵ since signal is in both 2 quadrants, it is a 'Bilateral signal'.

★ Formula for Unilateral :-

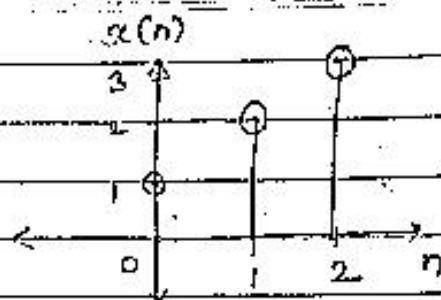
$$X(z) = \sum_{n=0}^{\infty} x(n) \cdot z^{-n}$$

★ Formula for Bilateral :-

$$X(z) = \sum_{n=-\infty}^{\infty} x(n) \cdot z^{-n}$$

Ex: If  $x(n) = \{1, 2, 3\}$

$n = 0 \quad 1 \quad 2$



formula for Z-transform -

Unilateral  
Z-transform

$$X(z) = \sum_{n=0}^{\infty} x(n) \cdot z^{-n}$$

our  $n$  ranges from 0 to 2.

$$\therefore X(z) = \sum_{n=0}^2 x(n) \cdot z^{-n}$$

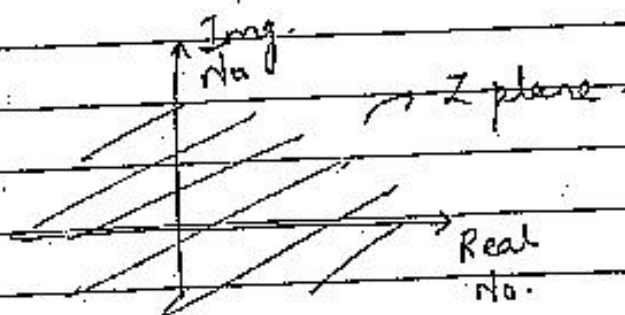
$$X(z) = x(0) \cdot z^0 + x(1) \cdot z^{-1} + x(2) \cdot z^{-2}$$

$$= 1 \cdot 1 + 2 \cdot z^{-1} + 3 \cdot z^{-2}$$

$$\therefore X(z) = 1 + \frac{2}{z} + \frac{3}{z^2}$$

→ Now, Region of convergence (ROC).

$z \rightarrow$  complex variable.



Region of convergence lies here where the value of  $n$  becomes finite.

→ Let's find the ROC of above eq<sup>n</sup> -

$$X(z) = 1 + \frac{2}{z} + \frac{3}{z^2}$$

Let's substitute  $z=0$  & check -

$$\therefore X(z) = 1 + \frac{2}{0} + \frac{3}{0}$$

Anything divided by 0 becomes  $\infty$ .

$$\therefore X(z) = 1 + \infty + \infty$$

$\therefore X(z) = \infty$  for  $z=0$  is  $\infty$

$\therefore$  Not ROC

Next substitute  $z=1$  & check -

$$X(z) = 1 + \frac{2}{1} + \frac{3}{1^2}$$

$$= 1 + 2 + 3$$

$\therefore X(z) = 6$  which is finite

$\therefore z=1$  is in ROC

Now let's substitute  $z=\infty$  & check -

$$X(z) = 1 + \frac{2}{\infty} + \frac{3}{\infty}$$

$$X(z) = 1 + 0 + 0$$

i.e.  $X(z) = 1$

(when anything divided by large no., it gives a very small no.)  
ex:  $\frac{1}{10} = 0.1$   
 $\frac{1}{100} = 0.01$

Thus the ROC for  $X(z) = 1 + \frac{2}{z} + \frac{3}{z^2}$

is anything but not Zero.

→ Lets plot —

