

# Modular Design of Urban Traffic-Light Control Systems Based on Synchronized Timed Petri Nets

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**Abstract**—Timed Petri nets (TPNs) have been utilized as visual formalism for the modeling of complex discrete-event dynamic systems. They illuminate the features in describing the properties of causality and concurrency. Moreover, it is well known that a synchronized TPN (STPN) allows us to present all of the concurrent states in a complex TPN. In this paper, we propose a new methodology to design and analyze an urban traffic network control system by using the STPN. In addition, the applications of the STPN to eight-phase, six-phase, and two-phase traffic-light control systems are modularized. The advantage of the proposed approach is the clear presentation of the behaviors of traffic lights in terms of the conditions and events that cause phase alternations. Moreover, the size of the urban traffic network control system can be easily extended with our proposed modular technique. An analysis of the control models is performed via a reachability graph method to demonstrate how the models enforce the transitions of the traffic lights.

**Index Terms**—Modular, Petri net (PN), traffic control systems, traffic network.

## I. INTRODUCTION

WITH the growing number of vehicles, traffic congestion and transportation delay in urban arterial roads are increasing worldwide; hence, it is imperative to improve the safety and efficiency of transportation. Subsequently, several research teams focus their attention on the area of intelligent transport systems [14], [20]. In addition, they apply advanced communication, information, and electronics technology to solve transportation problems such as traffic congestion, and to improve transportation safety and efficiency [5]. Traffic light control systems regulate, warn, and guide transportation for the purpose of improving the safety and efficiency of pedestrians and vehicles. Much work has been done to develop various strategies [19], which are classified into two categories: fixed-

time and traffic-response. Nowadays, most industrialized countries are using the former for urban traffic control. In addition, the topics of traffic signal control can be separated into two classes [15]: determining which signal indication sequence optimizes the overall system performance and ascertaining how to implement the signal control logic.

However, several fundamental problems remain open, among which are the modeling methodologies. This paper concentrates on the second class, with a predetermined traffic signal timing plan. In other words, traffic signals are used to manage conflicting requirements for the use of road space, which are often at road junctions, by allocating the right-of-way to different sets of mutually compatible traffic movements during distinct time intervals. There is only one type of phase transition discussed in an urban net [15]. The variation of a vehicle's direction at a four-way intersection has two phases [22], four phases [24], or eight phases [15]. Febbraro *et al.* [6] proposed an urban traffic controller including four-phase and three-phase transitions. However, they failed to address the complicated movement direction of the traffic flow at intersections. For example, a traffic light not only has red, yellow, and green lights, but it also has a left-turn arrow on green, a right-turn arrow on green, and a straight arrow on green. As a result, it is possible to have both a right-turn arrow on green and a red signal turned on in an eastbound traffic light, and a green signal turned on in the northbound traffic light. In some countries, there may be additional lights, i.e., usually a green arrow to authorize turns (called a lead light in the U.S. because it usually leads to the main green light). Traffic light control systems regulate, warn, and guide transportation for the purpose of improving the safety and efficiency of pedestrians and vehicles. Obviously, an unsuitable modeling tool could make it difficult to evaluate the performance indexes of traffic control systems, such as the number of vehicles that are stopped by red signals and the subsequent time loss due to them.

Petri nets (PNs) have been proven to be a powerful modeling tool for various kinds of discrete-event systems [7], [17], and their formalism provides a clear means for presenting simulation and control logic. Hence, they are suitably used in traffic control systems. However, conventional PNs cannot determine the exact time of transition firing. To enhance their capability, timed PNs (TPNs) are proposed. Recently, they have been successfully used to model railway level crossing [3], [9], [18] and urban traffic network control systems [10]–[12], [23]. Moreover, timed colored PNs (TCPNs) are utilized as visual formalism for the modeling of complex systems. Our prior work used a TCPN to model an intelligent urban traffic-light control system [8], [12]. In summary, there are several modeling

Manuscript received March 28, 2013; revised July 3, 2013; accepted September 2, 2013. Date of publication November 12, 2013; date of current version March 28, 2014. This work was supported in part by the National Science Council of Taiwan under Grant NSC 102-2221-E-197-022-MY2 and National Natural Science Foundation of China, under Grant 61374148. The Associate Editor for this paper was Z. Li.

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Digital Object Identifier 10.1109/TITS.2013.2283034

tools applied in the traffic-light control field. However, they hardly present the alternation of the traffic-light phases in a clear manner. Therefore, this paper focuses on the use of a synchronized TPN (STPN) to model an urban traffic-light control system that may have eight-phase, six-phase, and/or two-phase traffic lights. The advantage of the new approach is that the behavior of the traffic lights in terms of the conditions and events that cause phase alternations can be presented clearly. Reachability graphs are adopted to analyze the proposed STPN models. More significantly, we propose a new method of modular design. It subdivides a system into smaller parts that can be independently created and then used in different systems to drive multiple functionalities. Its advantages include the ease of change to achieve technology transparency and the use of industry standards to design key interfaces.

Earlier contributions focused on finding optimal control strategies [2], [15]. A variety of mathematical programming methodologies [2], [4] and artificial intelligence techniques [1], [16] to model the traffic flow and the control logic are proposed. Nevertheless, they need to translate their control logic to computer codes. Unfortunately, previous work did not address the issue of how to implement signal control logic [15]. The proposed STPN can overcome this drawback.

The rest of this paper is organized as follows. Section II gives a brief description of STPN. Section III provides the description of an urban traffic network system. Section IV presents our STPN-based modular design technique. Section V depicts how to model and analyze it with STPN. Conclusions are given in Section VI.

## II. BASICS OF STPNs

A classical PN is a particular kind of bipartite directed graphs populated by three types of objects [25]–[27]. They are the places, transitions, and directed arcs that connect places to transitions and transitions to places. Because the classical PN is not capable of handling quantitative time, a timing concept is introduced to its transitions, thereby leading to TPNs [25]. A transition fires by removing tokens from its input places, and after a certain period (time delay), it deposits the tokens to its output places. In a synchronized PN, an event is associated with each transition, and the firing of this transition will occur, i.e., if the transition is enabled when the associated event occurs [21]. Therefore, synchronized PN is well suited for the modeling of the systems that are synchronized with external events at a hierarchical level. In this paper, we combine the TPN and synchronized PN models, resulting in STPN. STPN allows two types of transitions: the immediate transition, which is represented by a thin bar and is also called a slave transition, whose firing takes no time, and the deterministic transition, which is represented by an empty bar and is also called a master transition, whose firing takes a constant delay time. In a master module, an event is associated with a master transition. Therefore, once an external event happens, its corresponding slave transition fires in the slave modules.

Formally, STPN can be defined as

$$\text{STPN} = (P, T, I, O, M_0, \tau, E, H)$$

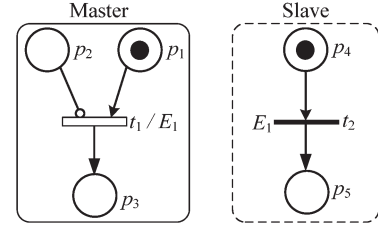


Fig. 1. STPN with an external event and an inhibitor arc.

where

$$P = \{p_1, p_2, \dots, p_m\}$$

a finite set of places;

$$T = \{t_1, t_2, \dots, t_n\}$$

a finite set of transitions, which are partitioned into two disjoint sets  $T^0$  and  $T^+$  that represent the immediate and deterministic transitions, respectively.  $P \cup T \neq \phi$ , and  $P \cap T = \phi$ ;

$$I : P \times T \rightarrow N$$

input function that defines the directed arcs from places to transitions, where  $N$  is a set of nonnegative integers;

$$O : P \times T \rightarrow N$$

output function that defines the directed arcs from transitions to places;

$$M_0 : P \rightarrow N$$

initial marking;

$$\tau : T \rightarrow R^+$$

firing time function, where  $R^+$  is the set of nonnegative real numbers;

$$E = \{E_1, E_2, \dots, E_i\}$$

set of events associated with the transitions;

$$H \subseteq P \times T$$

set of inhibitor arcs from  $p$  to  $t$ .

**Enabling Rule:** A transition  $t$  is enabled at marking  $M$  if  $\forall p \in P, M(p) \geq I(p, t)$  and  $M(p) = 0$  if  $(p, t) \in H$ .

**Firing Rule:** First, an enabled transition  $t$  may or may not fire depending on the additional interpretation. Second, firing  $t$  removes  $I(p, t)$  tokens from each input place  $p$  and deposits  $O(p, t)$  tokens to each output place  $p$  of  $t$ . Finally, a transition in the slave can fire if and only if the corresponding external event occurs, and each of its preset contains sufficient tokens.

The liveness of a PN means that, for each marking  $M \in R(M_0)$  that is reachable from  $M_0$ , it is finally possible to fire  $t \forall t \in T$  through some firing sequence. Note that  $R(M_0)$  is the set of all reachable markings from  $M_0$ . A marking  $M$  is reachable from  $M_0$  if there is a fireable transition sequence that converts  $M_0$  into  $M$ . A PN is said to be reversible if, for each marking  $M \in R(M_0)$ ,  $M_0$  is reachable from  $M$ . Thus, in a reversible net, it is always possible to go back to the initial marking (state)  $M_0$ .

An STPN with an inhibitor arc is shown in Fig. 1. In the presence of an inhibitor arc, a transition is regarded as enabled if input place  $p_1$ , which is connected to the transition by a normal arc (an arc that is terminated with an arrowhead), contains at least the number of tokens equal to the weight of the arc and if no tokens are present in input place  $p_2$ , which is connected to the transition by the inhibitor arc. Moreover, transition  $t/E_1$  fires by removing a token from  $p_1$ , and it deposits the token to  $p_3$  after a certain period  $\tau$ . Event  $E_1$  is associated with  $t_1$  if  $t_1$  fires and  $E_1$  occurs simultaneously. In the slave side,  $t_2$  is an immediate transition and is receptive to the same external event  $E_1$ . When  $E_1$  occurs,  $t_2$  fires by moving a token from  $p_4$  to  $p_5$  immediately.

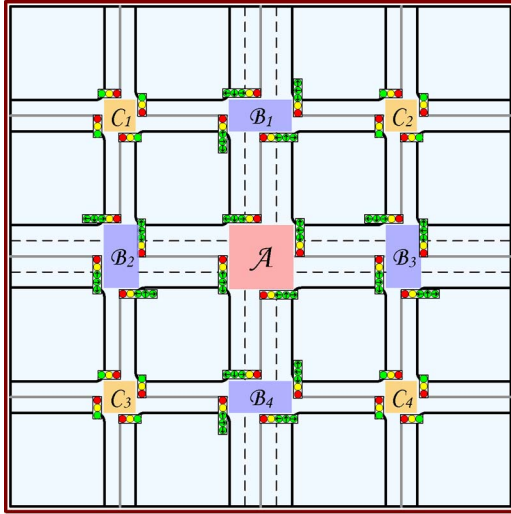


Fig. 2. Traffic network with nine intersections.

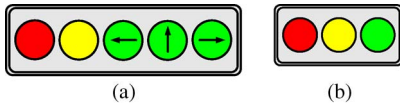


Fig. 3. (a) Five-light signal. (b) Three-light signal.

### III. SYSTEM DESCRIPTION AND METHODOLOGY DEVELOPMENT

The intersections are divided into three categories: main road, minor road, and tertiary road, which are called  $A$ ,  $B$ , and  $C$ , respectively. In Fig. 2, only one intersection belongs to the main road intersection, four ( $B_1$ – $B_4$ ) belong to the minor one, and four ( $C_1$ – $C_4$ ) belong to the tertiary one. Here, two types of traffic lights are employed. The first type consists of five signal lights as shown in Fig. 3(a), i.e., a left-turn arrow on green ( $GL$ ), a right-turn arrow on green ( $GR$ ), a straight arrow on green ( $GS$ ), a yellow light signal ( $Y$ ), and a red light signal ( $R$ ). There is either an eight-phase or six-phase transition available in this kind of traffic lights. The second type, as shown in Fig. 3(b), consists of three signal lights, i.e.,  $G$ ,  $Y$ , and  $R$ . Only two-phase transitions are needed. Considering the traffic flow, we assume that a traffic light has an eight-phase transition at  $A$ , a six-phase one at  $B$ , and a two-phase one at  $C$ .

This work proposes the following design procedure based on the idea of a modular design.

- **Inputs:** A traffic network with traffic-light requirements.
  - **Outputs:** The modular design and implementation of a traffic-light control system.
- 1) Calculate how many traffic lights are needed in the traffic network system.
  - 2) Identify the phase transition (i.e., two-phase, six-phase, and eight-phase transitions) for each traffic light.
  - 3) Define the phase transition models for each phase transition.
  - 4) Construct the STPN model for each phase transition.
  - 5) Design the master-slave module for each phase transition.

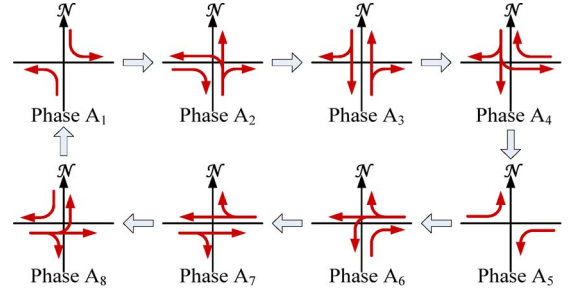


Fig. 4. Eight-phase transition and the phase alternating order.

- 6) Select one of the most complex modules (i.e., the eight-phase transition) as the master controller of the traffic-light control system.
- 7) Construct the traffic-light control system STPN model.
- 8) Analyze the control system STPN model.
- 9) Implement the traffic-light control system.

#### A. Phase Transition Models

Fig. 2 shows an urban traffic network with nine intersections that is taken from [13]. Consider the traffic area constructed in Fig. 2, which consists of intersections  $A$ ,  $B$ , and  $C$ . The flows at  $A$  are ruled by an eight-phase traffic light. The rules are shown in Fig. 4(a).

- 1) Phase  $A_0$ . A traffic-light control system can be started if its traffic signal lights are all in a red state.
- 2) Phase  $A_1$ .  $GL$  signals turn on in the northbound and the southbound traffic lights. The  $R$  signals are displayed in the east–westward traffic directions.
- 3) Phase  $A_2$ . The northbound traffic-light signals  $GL$ ,  $GR$ , and  $GS$  are on. The eastbound traffic lights indicate the  $GR$  signal. Notice that this phase is ignored in [6] and [24].
- 4) Phase  $A_3$ . Both the northbound and southbound traffic-light signals  $GS$  and  $GR$  are on.
- 5) Phase  $A_4$ . The southbound traffic-light signals  $GL$ ,  $GR$ , and  $GS$  are on. At the same time, the  $GR$  signal is displayed in the westward traffic direction.

Notice that phases ( $A_5$ – $A_8$ ) are similar to phases ( $A_1$ – $A_4$ ), respectively (but in a reverse order). We assume that the phase transition time is 45 s for each phase transition. For convenience, we define “set cycle time” as the period for a set of traffic lights to operate in one cycle. Since there are nine sets of traffic lights in the example network, we further define “system cycle time” as the period for all sets to operate in one cycle. As a result, it needs 360 s for a set cycle time. It hints that phase  $A_1$  should be changed to phase  $A_2$  after 45 s.

Considering the second category of intersections, the vehicle flows at intersection  $B$  are required to be ruled by a six-phase traffic light. Fig. 5 shows the definitions of the phases and their alternating order.

- 1) Phase  $B_0$ . A traffic-light control system can be started if its traffic signal lights are all in the red state.
- 2) Phase  $B_1$ .  $GL$ ,  $GS$ , and  $GL$  signals turn on in the northbound traffic light. The  $R$  signals are displayed in the other traffic directions.



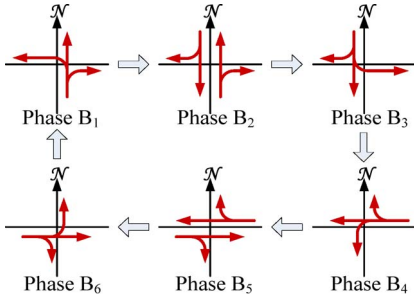


Fig. 5. Models of the six-phase transition.

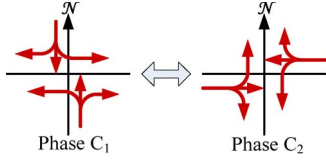


Fig. 6. Models of the two-phase transition.

- 3) Phase  $B_2$ . Both the northbound and southbound traffic lights are showing  $GS$  and  $GR$  signals.
- 4) Phase  $B_3$ .  $GL$ ,  $GS$ , and  $GL$  signals turn on in the southbound traffic lights. The  $R$  signals are displayed in the other traffic directions.

Finally, the two-phase transitions of the traffic lights that are located at intersections  $C$  are presented in Fig. 6.

- 1) Phase  $C_0$ . A traffic-light control system can be started if its traffic signal lights are all in the red state.
- 2) Phase  $C_1$ . Both the northbound and southbound traffic lights show  $G$  signals. This phase transition time is 90 s.
- 3) Phase  $C_2$ . Both the westbound and eastbound traffic lights show  $G$  signals. This phase transition time is also 90 s.

The three phase transition models illustrate the application of the urban traffic network control criteria.

### B. STPN Model of an Example Traffic-Light Control System

A road signal for directing vehicular traffic using colored lights typically uses red for stop, green for go, and yellow for proceeding with caution. A traffic light with the three colored lights is called a two-phase traffic light. A two-phase system model is depicted in Fig. 7(a). Considering the safety of vehicles, some important rules are needed.

- 1) A traffic-light control system can be started if its traffic signal lights are all in a red light state.
- 2) A 2-s overlap is needed while the phase is changing from northward/southward to eastward/westward.
- 3) Only one green light is allowed on the two ways simultaneously.
- 4) A traffic light changes in the order of green, yellow, and red.

According to the specification of the traffic-light system, the STPN model of Fig. 7(a) can be constructed in Fig. 7(b). It describes a two-phase traffic-light control system with three

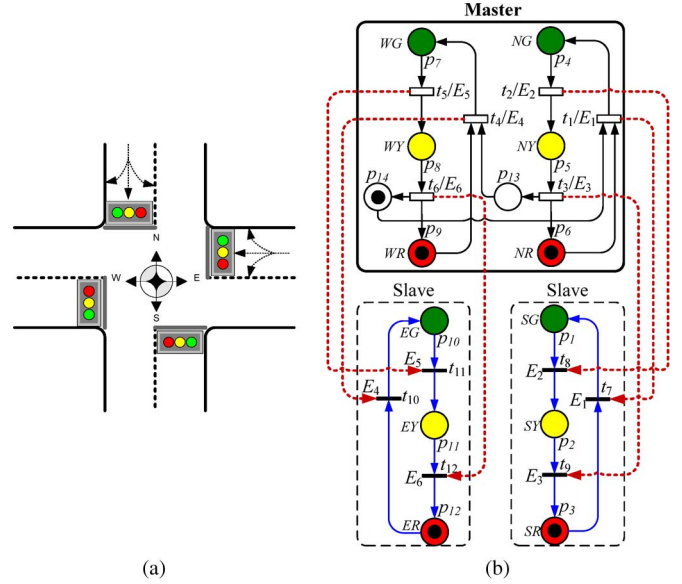


Fig. 7. (a) Two-phase traffic-light control system. (b) STPN model.

TABLE I  
ATTRIBUTION OF TRANSITIONS IN FIG. 7

$t_i$	Type	Parameter	value	units
$t_1$	deterministic	$\tau_1 / E_1$	2	sec
$t_2$	deterministic	$\tau_2 / E_2$	85	sec
$t_3$	deterministic	$\tau_3 / E_3$	3	sec
$t_4$	deterministic	$\tau_4 / E_4$	2	sec
$t_5$	deterministic	$\tau_5 / E_5$	85	sec
$t_6$	deterministic	$\tau_6 / E_6$	3	sec
$t_7$	immediate	$E_1$	0	sec
$t_8$	immediate	$E_2$	0	sec
$t_9$	immediate	$E_3$	0	sec
$t_{10}$	immediate	$E_4$	0	sec
$t_{11}$	immediate	$E_5$	0	sec
$t_{12}$	immediate	$E_6$	0	sec

traffic signal lights, i.e., green ( $G$ ), yellow ( $Y$ ), and red ( $R$ ). More detailed information of Fig. 7(b) is listed in Table I.

Regularly, there are four sets of traffic lights in a system, i.e., the northbound, southbound, eastbound, and westbound traffic lights, which are placed at each intersection. Vehicles heading northward/southward and heading eastward/westward are denoted by  $N/S$  and  $E/W$ , respectively. The system model is divided into two parts, i.e., the master and slave models. A master model consists of places  $p_4/p_7$ ,  $p_5/p_8$ , and  $p_6/p_9$ , and their associated arcs and transitions. A slave model consists of places  $p_1/p_{10}$ ,  $p_2/p_{11}$ , and  $p_3/p_{12}$ , and their associated arcs and transitions. For convenience,  $p_4/p_7$ ,  $p_5/p_8$ , and  $p_6/p_9$  are given physical names, i.e.,  $NG/WG$ ,  $NY/WY$ , and  $NR/WR$ , respectively. They represent three northward/westward traffic lights  $G$ ,  $Y$ , and  $R$ , respectively. Similarly,  $p_1/p_{10}$ ,  $p_2/p_{11}$ , and  $p_3/p_{12}$  are given names, i.e.,  $SG/EG$ ,  $SY/EY$ , and  $SR/ER$ , respectively. They represent three southward/eastward traffic

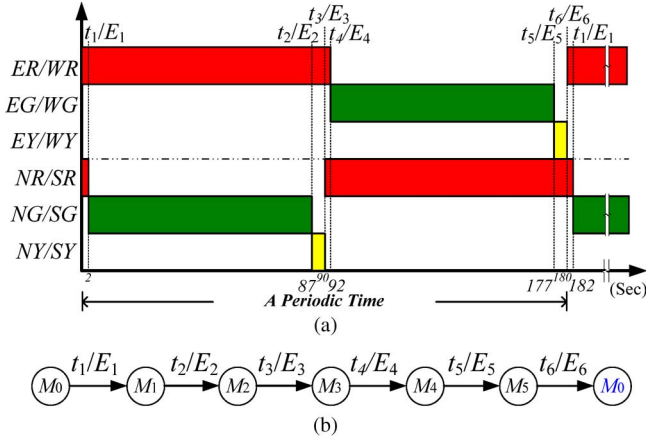


Fig. 8. (a) Duration diagram. (b) Reachability graph.

lights  $G$ ,  $Y$ , and  $R$ , respectively. The operations of the slave model are controlled by the master model via external events. For example, when  $t_1/E_1$  fires (in the master model), then  $t_7$  can be fired in the slave model.

Fig. 7(b) shows the initial state of the system model. To fit a physical system, it is natural to consider an upper limit of the number of tokens that each place can hold. This leads to a finite capacity net. Here, we apply the strict transition rule to our proposed models. For instance, Fig. 7(b) is a finite capacity net ( $N$ ,  $M_0$ ), and each place  $p$  has an associated capacity  $K(p) = 1$  [17]. We know that the initial state of traffic signal lights is in the  $R$  state. After 2 s (i.e., firing  $t_1/E_1$ ), a token is moved to  $p_4$ . In the meantime,  $t_7$  immediately fires as triggered by  $E_1$  such that a token is moved to  $p_1$  immediately. At this moment,  $NG$  turns on such that the way of vehicles can pass through the intersection. Next,  $NG$  should be off after the duration in  $t_2/E_2$ . Notice that event  $E_2$  is associated with  $t_2$ . Therefore,  $E_2$  will concurrently occur with the firing of  $t_2$ . It states that  $t_8$  fires when  $E_2$  occurs. It implies that  $SG$  has been on for 85 s. Then,  $NY$  is on for 3 s because the duration in  $t_3/E_3$  is 3 s.  $E_3$  is associated with  $t_3$ . Therefore,  $E_3$  will occur concurrently. It states that  $t_9$  fires when  $E_3$  occurs. Then, the token is moved to place  $p_6/p_3$  again. After 2 s (i.e., firing  $t_4/E_4$ ), a token in  $p_9/p_{12}$  is moved to  $p_7/p_{10}$ . At this moment,  $WG/EG$  turns on. It means that  $NW/EG$  has been on for 85 s. Then,  $WY$  is on for 3 s because the duration in  $t_6/E_6$  is 3 s. Finally, the token is moved to  $p_9/p_{12}$  again. According to the model, one can well describe the periodic property of the traffic-light control system. Fig. 8(a) shows its control process. It helps us understand the behavior of the system model.

A reachability graph can be generated to analyze the model. No conflict can be found, as shown in Fig. 8(b), as verified by its reachability graph. The reachability set  $R(M_0) = \{M_0, M_1, M_2, M_3, M_4, M_5\}$  contains all the markings that are reachable from  $M_0$ . Here,  $M_0 = (0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 1)$ ,  $M_1 = (1, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0)$ ,  $M_2 = (0, 1, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 0)$ ,  $M_3 = (0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 1, 0)$ ,  $M_4 = (0, 0, 1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0)$ , and  $M_5 = (0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0)$ . Since this graph is a finite circuit containing all transitions, one can infer that the STPN model in Fig. 7(b) is live and reversible.

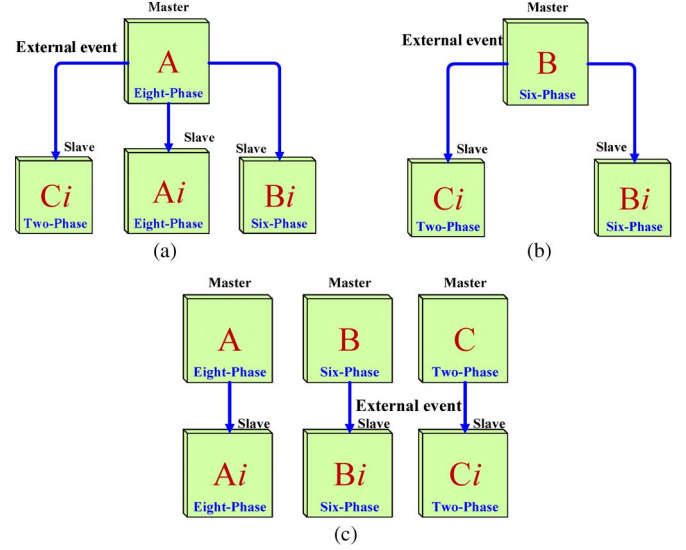


Fig. 9. All possible combinations for the master-slave traffic light controller.

#### IV. STPN-BASED MODULAR DESIGN TECHNIQUE FOR MASTER-SLAVE TRAFFIC SIGNAL CONTROLLER

In order to be able to integrate the different phases of traffic lights in different roadway intersections, all traffic lights (two-phase, six-phase, and eight-phase traffic lights) can independently operate and can be associated with each other. Fig. 9 shows all possible combinations for the master-slave traffic-light controller. For example, at a traffic network with three different intersections in Fig. 9(a), the most complex traffic light (i.e., the eight-phase traffic light) will be the master controller, and the others will be the slaves. If an urban traffic network only has the same phase traffic-light controller, all must serve as the master controller as shown in Fig. 9(c). In the proposed method, we need one model as the master that is able to trigger the slave models. Here, we leave out the details in Fig. 9(b). In addition, three capabilities offered by STPN are listed as follows.

- 1) *Master-slave configuration.* It is well known that STPN has external events that allow one to model the relation of the concurrence transitions, whatever the related transitions are in different levels. Therefore, we propose that the master-slave configuration is used to model the urban traffic-light system. Its advantage is that all external events (i.e., the transitions of the master) are able to trigger the corresponding transitions of the slaves.
- 2) *Timing specifications.* STPN is capable of handling quantitative time to model the timing specification in subnets. It is worth noting that such timing constraints can appear in subnets at any levels.
- 3) *Synchronization descriptions.* The ability of STPN to describe synchronization is crucial. In STPN, an event is associated with specific transitions. Once an event occurs, its corresponding transitions will fire. In Fig. 1, one can recall that  $t$  immediately fires when its external event  $E$  occurs. This representation is appropriate to model the occurrence transitions that depend on external events. Fig. 9 shows the relation of the traffic-light control system models with external events.

### A. Master-Slave Module of Eight-Phase Traffic-Light STPN Model

All external events (i.e.,  $E_i$ ) are designed to connect to their corresponding pins. Hence, a master-slave module of the eight-phase traffic-light STPN model that is designed in an IC style is depicted in Fig. 10. Here, eight external events (i.e.,  $E_1$ – $E_8$ ) are laid out in Fig. 10. This type of controllers can be only used in the main street intersection (i.e., the eight-phase traffic lights). We name it as Class A. It is the key to the urban traffic-light control system. There are four parts of traffic lights facing the four directions of an intersection. For example, the traffic light positioned at the southbound of intersection A is called the northbound traffic light, which is denoted as  $N\_A$ . The others are  $S\_A$ ,  $W\_A$ , and  $E\_A$  for the southbound, westbound, and eastbound traffic lights, respectively. Note that each of them has five light signals.

For convenience, only the places that are modeling the traffic-light signals are included in the elements of a marking. In this master-slave model, the marking ( $ANR$ ,  $ASR$ ,  $AWR$ ,  $AER$ ) is called initial state  $M_{a0}$ , which means that the four-part traffic lights are signaling  $R$ . The initial state will hold for 2 s, i.e., four parts of the traffic light signals stay red for 2 s simultaneously. Once  $t_1/E_1$  reaches 2 s, the initial marking configuration changing to ( $ANGL \wedge ANR$ ,  $ASGL \wedge ASR$ ,  $AWR$ ,  $AER$ ) is called  $M_{a1}$ . Notice that, at the same time, the transitions of two slave models  $t_{19}/t_{33}$  in Figs. 12 and 14 immediately fire when  $E_1$  occurs, such that marking  $M_{b0}/M_{c0}$  changes to  $M_{b1}/M_{c1}$ . In the meantime, phases  $A_1$ ,  $B_1$ , and  $C_1$  are derived. Once  $t_2$  has been firing for 40 s,  $M_{a1}$  changes to ( $ANGL \wedge ANR$ ,  $ASY \wedge ASR$ ,  $AWR$ ,  $AER$ ), which is called  $M_{a2}$ . During this period, the marking  $ASGL$  of  $S\_A$  is changed to  $ASR$  via  $ASY$ , which is called transient marking  $M_{a2}$ . It means that the left-turn arrow is green for 40 s, and then, the yellow light signal turns on for 3 s. Here, such kind of markings is called transient markings. The other markings involving ( $ANY$ ,  $ASY$ ,  $AWY$ ,  $AEY$ ) are also regarded as transient markings since one of the elements of the marking is a yellow light. When  $t_3$  fires, the transient marking is changed to  $M_{a3}$ . Once  $t_4/E_2$  fires,  $M_{a3}$  should immediately change to ( $ANGS \wedge ANGR$ ,  $ASGS \wedge ASGR$ ,  $AWR$ ,  $AER$ ), which is called marking  $M_{a4}$ . Once  $t_5/E_3$  fires,  $M_{a4}$  should immediately change to ( $ANY$ ,  $ASGS \wedge ASGR$ ,  $AWR$ ,  $AER$ ), which is called the transient marking  $M_{a5}$ . It is worth noticing that a 2 s overlap between the phase changes is needed for safety reasons. The transient marking  $M_{a5}$  changes to ( $ANR$ ,  $ASGS \wedge ASGR$ ,  $AWR$ ,  $AER$ ), which is called transition marking  $M_{a6}$ . After 2 s (firing  $t_7$ ),  $M_{a6}$  should immediately change to ( $ANR$ ,  $ASGL \wedge ASGS \wedge ASGR$ ,  $AWR \wedge AWGR$ ,  $AER$ ), which is called marking  $M_{a7}$ . After 42 s (firing  $t_8/E_4$ ),  $M_{a7}$  should change to the transient marking ( $ANR$ ,  $ASY$ ,  $AWR$ ,  $AER$ ), which is called  $M_{a8}$ . Finally,  $M_{a8}$  should change to the initial marking  $M_{a0}$ . Phases  $A_5$ – $A_8$  proceed in the same way.

For clarity, a reachability graph of the STPN is depicted in Fig. 11. First,  $M_{a0}$  should be changed to  $M_{a1}$  when  $t_1/E_1$  fires. In the meantime, the new marking should be held for

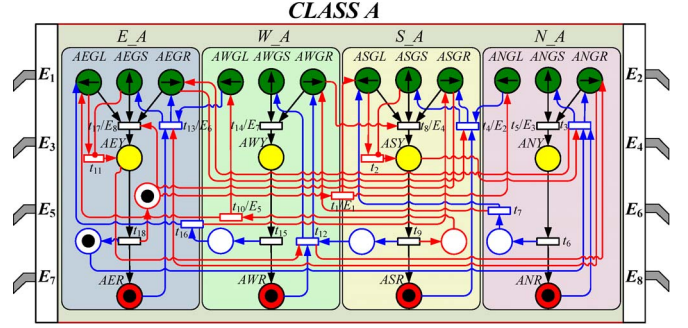


Fig. 10. Master-slave module of the eight-phase traffic-light STPN model.

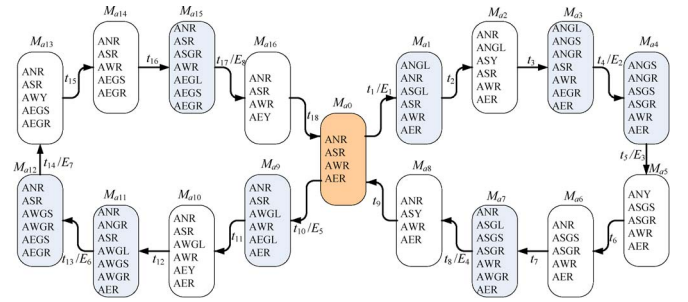


Fig. 11. Reachability graph of the eight-phase master-slave STPN model.

40 s. Then, the marking is changed to a transient marking, i.e.,  $M_{a2}$ . When  $t_3$  fires,  $M_{a2}$  is changed to  $M_{a3}$ . After 42 s (firing  $t_4/E_2$ ), a new event  $E_2$  is generated, and  $M_{a3}$  changes to  $M_{a4}$  and so forth. The reachability set  $R(M_{a0}) = \{M_{a0}, M_{a1}, M_{a2}, M_{a3}, M_{a4}, M_{a5}, M_{a6}, M_{a7}, M_{a8}, M_{a9}, M_{a10}, M_{a11}, M_{a12}, M_{a13}, M_{a14}, M_{a15}, M_{a16}\}$  contains all the markings that are reachable from  $M_{a0}$ . As a result, we can conclude that the eight-phase model is live and reversible.

### B. Master-Slave Module of the Six-Phase Traffic-Light STPN Model

One has seen that the eight-phase traffic-light STPN model can be designed in an eight-pin IC style. Similarly, a master-slave model of the six-phase traffic-light controller is constructed and is designed in a 16-pin IC style, as shown in Fig. 12. This type of controller can be only employed in the minor street intersection (six-phase traffic lights). Here, we name it as Class B. In details, the master-slave model consists of four parts:  $N\_B$ ,  $S\_B$ ,  $W\_B$ , and  $E\_B$ . They correspond to the four ways of traffic lights.

It is very important to notice that some external events are related to the eight-phase master-slave STPN model. We will use the external events as the path of the signal communication between the master and slave controllers. According to the preceding discussion, the six-phase traffic-light STPN model should change from  $M_{b0}$  to  $M_{b1}$ . Fig. 13 depicts the more detailed operations of the STPN model in a reachability graph.

It includes  $M_{b0}$ , six phase markings ( $M_{b1}$ – $M_{b2}$ ,  $M_{b5}$ ,  $M_{b7}$ – $M_{b8}$ , and  $M_{b11}$ ), and six transient ones ( $M_{b3}$ – $M_{b4}$ ,  $M_{b6}$ ,  $M_{b9}$ – $M_{b10}$ , and  $M_{b12}$ ).  $R(M_{b0}) = \{M_{b0}, M_{b1}, M_{b2}, M_{b3}, M_{b4}, M_{b5}, M_{b6}, M_{b7}, M_{b8}, M_{b9}, M_{b10}, M_{b11}, M_{b12}\}$  contains all the markings reachable from  $M_{b0}$ . The six-phase master-slave STPN model is live and reversible.



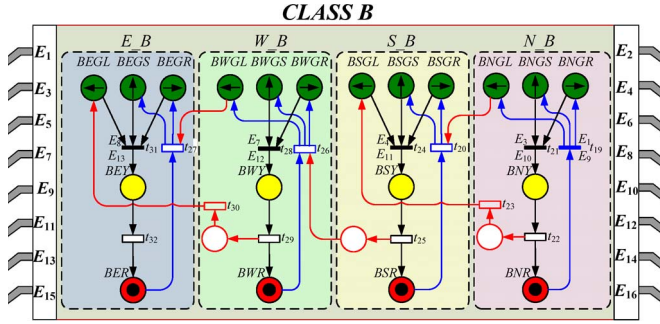


Fig. 12. Master-slave module of the six-phase traffic-light STPN model.

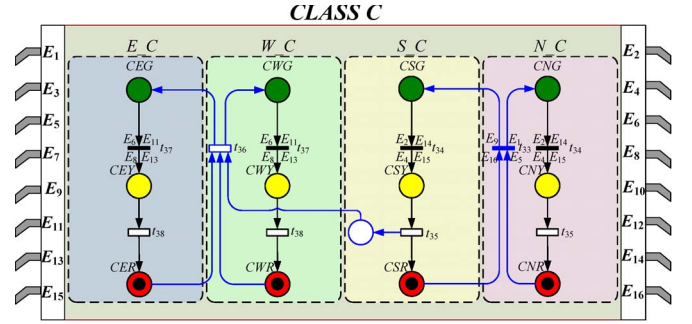


Fig. 14. Master-slave module of the two-phase traffic-light STPN model.

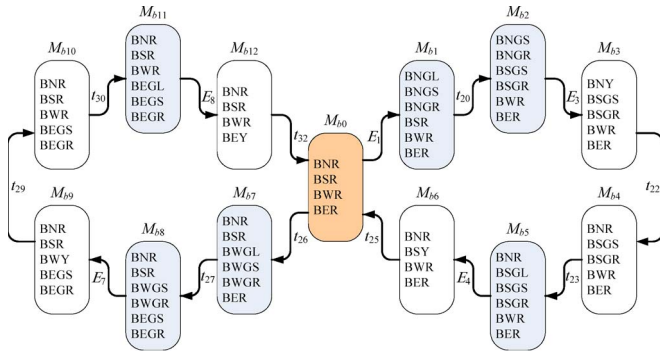


Fig. 13. Reachability graph of the six-phase master-slave STPN model.

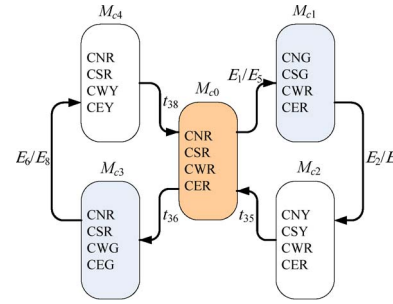
### C. Master-Slave Module of the Two-Phase Traffic-Light STPN Model

Next, we demonstrate the development the master-slave STPN model for two-phase traffic lights by a compact way. This kind of traffic lights is widely used at intersections of minor importance. The model of the two-phase traffic-light system is shown in Fig. 14. This kind of controllers can be only used in tertiary street intersections (i.e., the two-phase traffic lights). Here, we name it as Class C, as shown in Fig. 14. Likewise, a reachability graph of the master-slave STPN model is obtained, as shown in Fig. 15. It includes  $M_{c0}$ , two phase markings (i.e.,  $M_{c1}$  and  $M_{c3}$ ), and two transient ones (i.e.,  $M_{c2}$  and  $M_{c4}$ ).  $R(M_{c0}) = \{M_{c0}, M_{c1}, M_{c2}, M_{c3}, M_{c4}\}$ . As a result, we can infer that the two-phase model is live and reversible.

It is worth noting that the two-phase traffic light needs 180 s for a set cycle time. On the other hand, the system cycle of the urban traffic network system needs 360 s. Hence, the external event  $(E_2/E_4)/(E_6/E_8)$  can bring the transient marking  $M_{c2}/M_{c4}$  to the initial marking  $M_{c0}$ , respectively.

## V. MODELING AND ANALYSIS OF URBAN TRAFFIC NETWORK CONTROLLERS

In this section, we attempt to control an urban traffic network that consists of nine intersections. As aforementioned, the nine intersections are divided into three groups, i.e., main street, minor street, and tertiary street. To model the traffic network controllers of the nine intersections, one only needs one master eight-phase one, four slave six-phase one, and four two-phase ones. With a conventional methods, it is challenging to design a mechanism for coordinating the firing sequences of the traffic



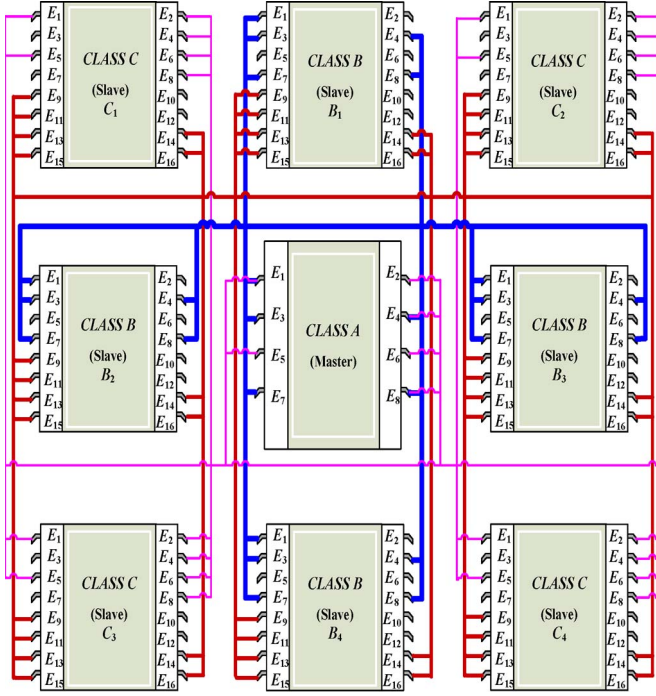


Fig. 16. Urban traffic network control system STPN model.

TABLE II  
DETAILED INFORMATION OF THE EXTERNAL EVENTS IN FIG. 16

Master CLASS A	Slave CLASS B <sub>1-4</sub>	Slave CLASS C <sub>1-4</sub>
$t_1/E_1$	$E_1/t_{19}$	$E_1/t_{33}$
$t_4/E_2$		$E_2/t_{34}$
$t_5/E_3$	$E_3/t_{21}$	
$t_8/E_4$	$E_4/t_{24}$	$E_4/t_{34}$
$t_{10}/E_5$		$E_5/t_{33}$
$t_{13}/E_6$		$E_6/t_{37}$
$t_{14}/E_7$	$E_7/t_{28}$	
$t_{17}/E_8$	$E_8/t_{31}$	$E_8/t_{37}$

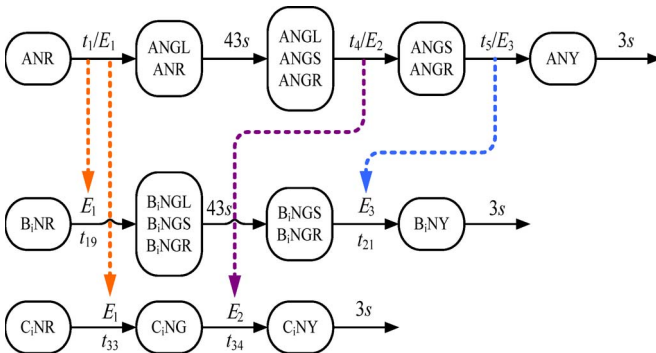
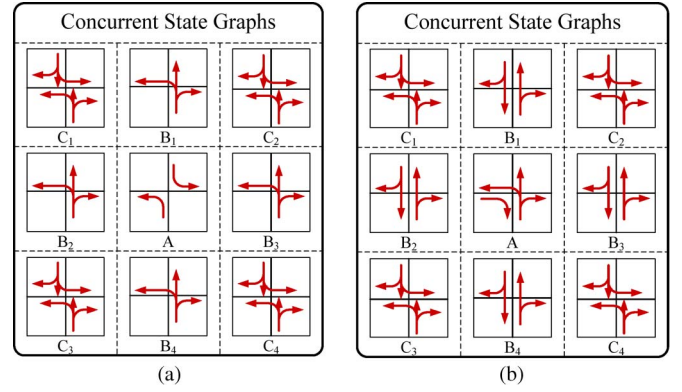


Fig. 17. Parts of the phase transitions of the controller.

(i.e., all the  $R$  signals are on). When  $t_1$  has fired for 2 s, event  $E_1$  is triggered such that the triggered transitions  $t_{19}$  and  $t_{33}$  fire immediately. Hence, event  $t_1/E_1$  causes the initial state configuration  $(ANR, B_iNR, C_iWR)$  to change to  $(ANGL, ANR, B_iNGL \wedge B_iNGS \wedge B_iNGR, C_iNG)$ . In the meantime, all the statuses of the traffic network are

Fig. 18. Phase transition of the traffic network control system. (a) *Phase\_1*. (b) *Phase\_2*.

shown in Fig. 18(a). After 43 s, the state configuration  $(ANGL, ANR, B_iNGL \wedge B_iNGS \wedge B_iNGR, C_iNG)$  can be then changed to  $(ANGL \wedge ANG S \wedge ANGR, B_iNGS \wedge B_iNGR, C_iNG)$ . At this moment, the nine pictures in Fig. 18(b) reflect the phase transitions of the traffic lights at nine intersections. Additionally, when  $t_4/E_2$  has fired for 42 s,  $E_2$  occurs such that  $t_{34}$  fires immediately. Because both state transitions are changed at the same time, the final state configuration becomes  $(ANG S \wedge ANGR, B_iNGS \wedge B_iNGR, C_iNY)$  after  $t_4/E_2$  fires.

### B. Analysis of Urban Traffic-Light Controller

Here, we attempt to analyze the urban traffic network. Based on the foregoing discussion, we know that the master-slave controller of the urban traffic system are all concurrent states. However, it is difficult to present all concurrent states together. Therefore, we try to construct the phase status configurations of the system model that contains the status of traffic-light signal  $Y$  called the transient state to present all the concurrent states. Here, an occurrence state shown in Table III is obtained from the urban traffic system state configuration. The occurrence state generates 17 phases in a system cycle. Each phase consists of nine elements, which are for the nine intersections of the urban traffic network. For example, the initial state, i.e.,  $phase\_state\_0 = (A, B_1, B_2, B_3, B_4, C_1, C_2, C_3, C_4)$ , means that the states of the traffic lights at intersections  $A, B_1-B_4$ , and  $C_1-C_4$  are in their initial states. It needs 360 s for the STPN to return to its initial state. It means that the urban traffic-light system needs 360 s for the system to return to the initial state. More precisely, the two-phase, six-phase, and eight-phase transitions need 180, 360, and 360 s for each set cycle time, respectively. Therefore, the eight-phase transition needs 45 s for each phase transition time.

Considering the STPN model of the urban traffic controller, the initial status configuration is represented by  $phase\_state\_0$ . It means that all the traffic lights signal  $R$  due to the initial status. According to the foregoing discussion, the system should be changed from  $phase\_state\_0$  to  $phase\_state\_1$  when event  $E_1$  occurs. More precisely,  $phase\_state\_1$  should be changed to  $transient\_phase\_state\_2$  after 40 s. We have to emphasize that all transient states should be held active for



TABLE III  
PHASE STATUS CONFIGURATIONS OF THE MODEL

Phase	Status configuration ( $N\_A$ , $S\_A$ , $W\_A$ and $E\_A$ ) of the intersections $A$ , $B_i$ and $C_i$ (i.e. $i = 1, 2, 3, 4$ )
State_0	(ANR, ASR, AWR, AER), ( $B_i$ NR, $B_i$ SR, $B_i$ WR, $B_i$ ER), ( $C_i$ NR, $C_i$ SR, $C_i$ WR, $C_i$ ER)
State_1	(ANR, ANGL, ASR, ASGL, AWR, AER), ( $B_i$ NGL, $B_i$ NGS, $B_i$ NGR, $B_i$ SR, $B_i$ WR, $B_i$ ER), ( $C_i$ NG, $C_i$ SG, $C_i$ WR, $C_i$ ER)
State_2	(ANR, ANGL, ASR, ASY, AWR, AER), ( $B_i$ NGL, $B_i$ NGS, $B_i$ NGR, $B_i$ SR, $B_i$ WR, $B_i$ ER), ( $C_i$ NG, $C_i$ SG, $C_i$ WR, $C_i$ ER)
State_3	(ANGL, ANGS, ANGR, ASR, AWR, AEGR, AER), ( $B_i$ NGS, $B_i$ NGR, $B_i$ SGS, $B_i$ SGR, $B_i$ WR, $B_i$ ER), ( $C_i$ NG, $C_i$ SG, $C_i$ WR, $C_i$ ER)
State_4	(ANGS, ANGR, ASGS, ASGR, AWR, AER), ( $B_i$ NGS, $B_i$ NGR, $B_i$ SGS, $B_i$ SGR, $B_i$ WR, $B_i$ ER), ( $C_i$ NY, $C_i$ SY, $C_i$ WR, $C_i$ ER)
State_5	(ANGS, ANGR, ASGS, ASGR, AWR, AER), ( $B_i$ NGS, $B_i$ NGR, $B_i$ SGS, $B_i$ SGR, $B_i$ WR, $B_i$ ER), ( $C_i$ NR, $C_i$ SR, $C_i$ WR, $C_i$ ER)
State_6	(ANY, ASGS, ASGR, AWR, AER), ( $B_i$ NY, $B_i$ SGS, $B_i$ SGR, $B_i$ WR, $B_i$ ER), ( $C_i$ NR, $C_i$ SR, $C_i$ WG, $C_i$ EG)
State_7	(ANR, ASGS, ASGR, AWR, AER), ( $B_i$ NR, $B_i$ SGS, $B_i$ SGR, $B_i$ WR, $B_i$ ER), ( $C_i$ NR, $C_i$ SR, $C_i$ WG, $C_i$ EG)
State_8	(ANR, ASGL, ASGS, ASGR, AWGR, AWR, AER), ( $B_i$ NR, $B_i$ SGL, $B_i$ SGS, $B_i$ SGR, $B_i$ WR, $B_i$ ER), ( $C_i$ NR, $C_i$ SR, $C_i$ WG, $C_i$ EG)
State_9	(ANR, ASY, AWR, AER), ( $B_i$ NR, $B_i$ SY, $B_i$ WR, $B_i$ ER), ( $C_i$ NR, $C_i$ SR, $C_i$ WY, $C_i$ EY)
State_10	(ANR, ASR, AWR, AWGL, AER, AEGL), ( $B_i$ NR, $B_i$ SR, $B_i$ WGL, $B_i$ WGS, $B_i$ WGR, $B_i$ ER), ( $C_i$ NG, $C_i$ SG, $C_i$ WR, $C_i$ ER)
State_11	(ANR, ASR, AWR, AWGL, AER, AEY), ( $B_i$ NR, $B_i$ SR, $B_i$ WGL, $B_i$ WGS, $B_i$ WGR, $B_i$ ER), ( $C_i$ NG, $C_i$ SG, $C_i$ WR, $C_i$ ER)
State_12	(ANR, ANGR, ASR, AWGL, AWGS, AWGR, AER), ( $B_i$ NR, $B_i$ SR, $B_i$ WGS, $B_i$ WGR, $B_i$ EGS, $B_i$ EGR), ( $C_i$ NG, $C_i$ SG, $C_i$ WR, $C_i$ ER)
State_13	(ANR, ASR, AWGS, AWGR, AEGS, AEGR), ( $B_i$ NR, $B_i$ SR, $B_i$ WGS, $B_i$ WGR, $B_i$ EGS, $B_i$ EGR), ( $C_i$ NY, $C_i$ SY, $C_i$ WR, $C_i$ ER)
State_14	(ANR, ASR, AWGS, AWGR, AEGS, AEGR), ( $B_i$ NR, $B_i$ SR, $B_i$ WGS, $B_i$ WGR, $B_i$ EGS, $B_i$ EGR), ( $C_i$ NR, $C_i$ SR, $C_i$ WR, $C_i$ ER)
State_15	(ANR, ASR, AWY, AEGS, AEGR), ( $B_i$ NR, $B_i$ SR, $B_i$ WY, $B_i$ EGS, $B_i$ EGR), ( $C_i$ NR, $C_i$ SR, $C_i$ WG, $C_i$ EG)
State_16	(ANR, ASR, AWR, AEGS, AEGR), ( $B_i$ NR, $B_i$ SR, $B_i$ WR, $B_i$ EGS, $B_i$ EGR), ( $C_i$ NR, $C_i$ SR, $C_i$ WG, $C_i$ EG)
State_17	(ANR, ASR, ASGR, AWR, AEGL, AEGS, AEGR), ( $B_i$ NR, $B_i$ SR, $B_i$ WR, $B_i$ EGL, $B_i$ EGS, $B_i$ EGR), ( $C_i$ NR, $C_i$ SR, $C_i$ WG, $C_i$ EG)
State_18	(ANR, ASR, AWR, AEY), ( $B_i$ NR, $B_i$ SR, $B_i$ WR, $B_i$ EY), ( $C_i$ NR, $C_i$ SR, $C_i$ WY, $C_i$ EY)

3 s. Then, *transient phase state\_2* should be changed into *phase state\_3* after 3 s. The physical meaning is that the phase's change of traffic lights is needed via *Y* lights. For example, *phase state\_1\_A*=(ANR, ANGL, ASR, ASGL, AWR, AER) is changed to *phase state\_2\_A*=(ANR, ANGL, ASY, ASR, AWR, AER) and is then changed to *phase state\_3\_A*=(ANGL, ANGS, ANGR, ASR, AWR, AER, AEGR). As aforementioned, we can infer that the occurrence state forms a cycle. As a result, the reversibility and liveness properties can be derived from the method.

## VI. CONCLUSION

Modular design is basically a method that is used to allow a specific type of unit to be broken down into smaller and easier-to-manage units. It can be applied in numerous areas to create efficiency in other types of design, from manufacturing and construction to computer programming. In this paper, we have proposed the master-slave configuration to model an urban traffic-light system. The advantage of the proposed approach is the clear presentation of the system behavior and readiness for implementation. Moreover, the analysis of the control models is performed through a reachability graph method to demonstrate how the models enforce the transitions of the lights. Their liveness and reversibility are verified.

We believe that our research using STPN to model traffic-light systems will become more and more important in this

field due to the increasing demands for more features on the traffic-light systems. The proposed STPN models can be extended for some other applications [28]–[34]. For example, our system model can be easily modified for an advanced traffic management system, which is able to interrupt the regularity of traffic lights if one allows emergency cars as the priority. The proposed method needs to be extended to deal with cases where the switching time of traffic lights is a function of the traffic intensity.

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