

$$f(t) = E \left(1 - \frac{|t|}{T} \right) = \begin{cases} E \left(1 - \frac{t}{T} \right) & (t \geq 0) \\ E \left(1 + \frac{t}{T} \right) & (t < 0) \end{cases}$$

$$F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt = \int_{-T}^0 E \left(1 + \frac{t}{T} \right) e^{j\omega t} dt + \int_0^T E \left(1 - \frac{t}{T} \right) e^{-j\omega t} dt$$

$$= \int_{-T}^T E \left(1 - \frac{|t|}{T} \right) e^{-j\omega t} dt$$

$$= 2 \int_0^T E \left(1 - \frac{t}{T} \right) \cos \omega t dt$$

$$= 2E \left(\left[E \left(1 - \frac{t}{T} \right) \cdot \frac{\sin \omega t}{\omega} \right]_0^T - \int_0^T \left(-\frac{1}{T} \right) \cdot \frac{\sin \omega t}{\omega} dt \right)$$

$$= 2E \left(-\frac{1}{\omega T} \left(\frac{\cos(\omega T)}{\omega} - \frac{\cos 0}{\omega} \right) \right)$$

$$= \frac{2E}{\omega^2 T} (1 - \cos \omega T)$$

$$F(\omega) = \frac{4E}{\omega^2 T} \sin^2 \left(\frac{\omega T}{2} \right)$$

$$= ET \frac{\sin^2 \left(\frac{\omega T}{2} \right)}{\left(\frac{\omega T}{2} \right)^2}$$

$$= ET \left(\frac{\sin \frac{\omega T}{2}}{\frac{\omega T}{2}} \right)^2$$