

演習

$$(1). \int_{\alpha}^{2\pi+\alpha} \sin 2\theta \cos 3\theta d\theta$$

$$= \int_0^{2\pi} \frac{1}{2} (\sin 5\theta + \sin \theta) d\theta$$

$$= \frac{1}{2} \left[-\frac{1}{5} \cos 5\theta - \cos \theta \right]_0^{2\pi}$$

$$= \frac{1}{2} \left(-\frac{1}{5} - \left(-\frac{1}{5}\right) - 1 - (-1) \right)$$

$$= \boxed{0}$$

$$(2). \int_{\alpha}^{2\pi+\alpha} \sin 2\theta \sin 2\theta d\theta$$

$$= \int_0^{2\pi} \sin^2 2\theta d\theta$$

$$= \int_0^{2\pi} \frac{1 - \cos 4\theta}{2} d\theta$$

$$= \left[\frac{\theta}{2} - \frac{1}{8} \sin 4\theta \right]_0^{2\pi}$$

$$= \boxed{\pi}$$