

演習

$$(1). \int_{2}^{2\pi} \sin 2\theta \cos 3\theta \, d\theta$$

$$= \int_{0}^{2\pi} \frac{1}{2} (\sin 5\theta + \sin \theta) \, d\theta$$

$$= \frac{1}{2} \left[ -\frac{1}{5} \cos 5\theta - \cos \theta \right]_{0}^{2\pi}$$

$$= \frac{1}{2} \left( -\frac{1}{5} - \left( -\frac{1}{5} \right) - 1 - (-1) \right)$$

$$= \boxed{0}$$

$$(2). \int_{2}^{2\pi} \sin 2\theta \sin 2\theta \, d\theta$$

$$= \int_{0}^{2\pi} \sin^2 2\theta \, d\theta$$

$$= \int_{0}^{2\pi} \frac{1 - \cos 4\theta}{2} \, d\theta$$

$$= \left[ \frac{\theta}{2} - \frac{1}{8} \sin 4\theta \right]_{0}^{2\pi}$$

$$= \boxed{\pi}$$