

## Research on active defense strategy of counter DDoS attacks based on Differential Games Model

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### Abstract

*In this paper, it is advocated that defenders should take active action to stop DDoS attacks. We propose a new model based on Differential Games theory. Four main actors are included, Attacker, Defender, Victim, and Botnet. It is our belief that Victims who experience an attack should cooperate with Defender to defend for a DDoS-attack. The model indicates the minimum number of Bots that should be blocked by Defender. A Differential Games model is used to determine how a Defender combats an Attacker and protect the servers. The feasibility and effectiveness of our approach is validated by measuring the performance of an experimental prototype against a series of attacks. The advantages of the scheme are discussed and further research directions are given.*

### 1. Introduction

Denial-of-Service (DoS[1,2,3]) attacks use legitimate requests to overload the server, causing it to hang, crash, reboot, or do useless work. The target application, machine, or network spends all of its critical resources on handling the attack traffic and cannot attend to its legitimate clients.

With the developing of computer technology, DDoS was first launched by worms or Botnet. Lately, DDoS has shown some new trends. It can be started automatically, controlled by a center computer which distributes the attacks.

For stopping DDoS, we need recognize and penetrate this remote control method, and then by using another method, to stop the attacks. Based on this idea, we bring our Differential Games Model (DGM).

### 2 Active defense strategy

Our defense strategy model (DGM) is composed of four components, namely: Attacker, Defender, Victim and Botnet. In our DGM model, four different actors can be distinguished: The first is Attacker. An Attacker uses all kinds of software exploits, worms and malicious code to conquer and control a large amount of computers, called Bots. The second one is Botnet, which is controlled by Attacker. Botnet consists of a large amount of computers, also called zombies or drones. The third actor is Victim. In general, Victim has a good immunity against worms, but is still vulnerable for DDoS attacks, performed by Botnet. The last actor is Defender, which serves as a DDoS protector. Before or during a DDoS attacks, it can combat with Attacker or Botnet. Our active defense model describes the battle between Defender and Attacker. Since the main task of Victim is to serve clients, for example as a game server, DNS server or VoIP authentication server, it is unacceptable to be burdened with the extra load of the DDoS defense. To overcome this problem, Defender could be a third party server, separated from the Victim. This task can be fulfilled by anything ranging from an internet administration, or governmental organization to commercial services. The aim of Defender is helping Victim to survive the DDoS attacks and keep it running during such an attack.

There are many parameters involved in the setup of a DDoS attack, where the number of Bots is the most important one. An Attacker will raise its number of Bots until it has sufficient resources at its disposal to overwhelm Victim. When the number of Bots reaches the critical point, a DDoS attack is available. Defender, at its turn, will set up honeypots or spread anti-worm software. Upon this we set up our DGM that can be used for controlling the Bots in a Botnet.

### 3 Differential Games Model and DDoS defense

It is supposed that Attacker and Defender, at time  $t$ , control the number of Bots  $x(t)$ ,  $y(t)$ . In the beginning  $t=0$ , Bots controlled by Attacker and Defender are  $x(0)$ ,  $y(0)$ . We assume that  $x(t)$  and  $y(t)$  are Continuous differentiable functions, i.e. changing only slowly. Whether a DDoS will succeed is directly decided by the number of Bots that is deployed. Both Attacker and Defender seek to minimize the use of resources and succeed in their tasks in the process of DDoS. Using these assumptions, we can design a Linear Quadratic Nonzero Sum Differential Games Model [3,4] as follow.

$$\begin{cases} \dot{x} = au_1 - bx \\ \dot{y} = cu_2 - dy \\ x(0) = x_0 \\ y(0) = y_0 \end{cases}$$

$$J_1(u_1, u_2) = -\frac{\xi}{2}(x(T_0))^2 + \frac{\eta}{2} \int_0^{T_0} u_1^2(t) dt$$

$$J_2(u_1, u_2) = -\frac{\beta}{2}(y(T_0))^2 + \frac{\gamma}{2} \int_0^{T_0} u_2^2(t) dt$$

$$H_1(x, y, u, \lambda) = \frac{\eta}{2} u_1^2 + \lambda_{11}(au_1 - bx) + \lambda_{12}(cu_2 - dy)$$

$$H_2(x, y, u, \lambda) = \frac{\gamma}{2} u_2^2 + \lambda_{21}(au_1 - bx) + \lambda_{22}(cu_2 - dy)$$

The necessary condition that  $(u_1^*(t), u_2^*(t))$  is

Open-Loop Nash Equilibrium[5,6,7] is  $(u_1^*, u_2^*)$  and its

Curve Track  $x^*, y^*$  can be met by equation as follow:

$$\begin{aligned} \left. \frac{\partial H_1(x^*, y^*, u_1, u_2^*, \lambda_1)}{\partial u_1} \right|_{u_1=u_1^*} &= \eta u_1^* + a \lambda_{11} = 0 \\ \left. \frac{\partial H_2(x^*, y^*, u_1^*, u_2, \lambda_2)}{\partial u_2} \right|_{u_2=u_2^*} &= \gamma u_2^* + c \lambda_{22} = 0 \end{aligned}$$

Where  $a$ ,  $c$  denote the Growth of Bots controlled by Attacker and Defender, and  $b$ ,  $d$  denote decline of Bots because many reasons of network.

$\xi$ ,  $\eta$ ,  $\beta$ ,  $\gamma$  are weighting coefficients,

describing Attacker and Defender. It should be noted that Hamiltonian functions [8] of Attacker and Defender are defined as follows.

$$\begin{aligned} \dot{\lambda}_{11} &= b \lambda_{11} \\ \lambda_{11}(T_0) &= -\xi x^*(T_0) \\ \dot{\lambda}_{12} &= d \lambda_{12} \\ \lambda_{12}(T_0) &= 0 \\ \dot{\lambda}_{21} &= b \lambda_{21} \\ \lambda_{21}(T_0) &= 0 \\ \dot{\lambda}_{22} &= d \lambda_{22} \\ \lambda_{22}(T_0) &= -\beta y^*(T_0) \end{aligned} \quad \begin{cases} x^* = au_1^* - bx^* \\ y^* = cu_2^* - dy^* \\ x^*(0) = x_0 \\ y^*(0) = y_0 \end{cases} \quad (\text{Equation 1})$$

We can get the adjoint vectors.

$$\begin{cases} \dot{\lambda}_{11} = -\xi x^*(T_0) e^{b(t-T_0)}, \lambda_{12} = 0 \\ \dot{\lambda}_{21} = 0, \lambda_{22} = -\beta y^*(T_0) e^{d(t-T_0)} \end{cases} \quad (\text{Equation 2})$$

The vectors of Investment Strategy are as follow.

$$u_1^*(t) = \frac{a}{\eta} \xi x^*(T_0) e^{b(t-T_0)} \quad (\text{Equation 3})$$

$$u_2^*(t) = \frac{c}{\gamma} \beta y^*(T_0) e^{d(t-T_0)} \quad (\text{Equation 4})$$

From Equation 3, we find that  $\frac{a}{\eta} \xi x^*(T_0)$  is the number of Bots that are being deployed by Attacker before DDoS attack (namely, at  $T_0$ ). This amount is

directly proportional to the total number of Bots  $x^*(T_0)$ .

Optimal deployment grows exponentially. Deployment

of Bots will occur only gradually, much similar to a rush time on the internet. In this way, in the first day,

Bots deployed can be described by  $\frac{a}{\eta} \xi x^*(T_0) e^{-bt_0}$ , similarly, in the second day it

deployed  $\frac{a}{\eta} \xi x^*(T_0) e^{-b(1-T_0)}$ , Using this principle,

Equation 4 can be explained in the same way. From Equation 1 to 4, we can derive an expression for the optimal deployment of Bots for both Attacker and Defender.

$$x^*(t) = x_0 e^{-bt} + \frac{a^2 \xi}{b\eta} x^*(T_0) e^{-bt_0} \sinh(bt) \quad \text{Equation 5}$$

$$y^*(t) = y_0 e^{-dt} + \frac{c^2 \beta}{d\gamma} y^*(T_0) e^{-dT_0} \sinh(dt) \quad \text{Equation 6}$$

$$v_1 = J_1(u_1^*, u_2^*) = -\frac{\xi}{2} (x_0 e^{-bt_0} + \frac{a^2 \xi}{b\eta} x^*(T_0) e^{-bt_0} \sinh(bt))^2 + \frac{(a \xi x^*(T_0))^2}{4b\eta} (1 - e^{-2bt_0})$$

$$v_2 = J_2(u_1^*, u_2^*) = -\frac{\beta}{2} (y_0 e^{-dT_0} + \frac{c^2 \beta}{d\gamma} y^*(T_0) e^{-dT_0} \sinh(dt))^2 + \frac{(c \beta y^*(T_0))^2}{4d\gamma} (1 - e^{-2dT_0})$$

From Equation 5 and 6 we can derive:

$$\begin{cases} x^*(T_0) = \frac{b\eta x_0}{b\eta e^{-bt_0} - a^2 \xi \sinh(bt_0)} \\ y^*(T_0) = \frac{b\eta y_0}{d\gamma e^{-dT_0} - c^2 \beta \sinh(dT_0)} \end{cases}$$

Such that

$$u_1^*(t) = \frac{ab\xi x_0}{b\eta e^{bt_0} - a^2 \xi \sinh(bt_0)} e^{b(t-T_0)}$$

$$u_2^*(t) = \frac{db\eta y_0}{d\gamma e^{-dT_0} - c^2 \beta \sinh(dT_0)} e^{d(t-T_0)}$$

Obviously,

$$\left. \frac{\partial H_1(x^*, y^*, u_1, u_2^*, \lambda_1)}{\partial u_1} \right|_{u_1=u_1^*} = \eta > 0$$

$$\left. \frac{\partial H_2(x^*, y^*, u_1^*, u_2, \lambda_2)}{\partial u_2} \right|_{u_2=u_2^*} = \gamma > 0$$

Positively,  $(u_1^*(t), u_2^*(t))$  is in an Open-Loop Nash Equilibrium. analogously, we conclude that

Equation 5 highlights that, with time elapsing, on one hand, the Bots originally used by Attacker ( $x_0$ ) is depleting exponentially, while on the other hand, it is being complemented, which can be described by a sinh law. Furthermore, it is directly proportional to the number of Bots which is the ultimate expectation. In a very long time (for high values of  $t$ ), the rate of change

for  $x^*(t)$  is close to  $a^2 \xi x^*(T_0) e^{b(1-T_0)} / (2b\eta)$ ,

namely, the number of Bots grow exponentially. And it is directly proportional to the number of Bots of

ultimate expectation  $x^*(T_0)$ . With Equation 1 to Equation 6, we can conclude that the equilibrium value of Attacker and Defender Bots:

$$x^*(T_0) = x_0 e^{-bt} + \frac{a^2 \xi x_0 \sinh(bt_0)}{b\eta e^{-bt_0} - a^2 \xi \sinh(bt_0)}$$

$$y^*(T_0) = y_0 e^{-dt} + \frac{c^2 \beta y_0 \sinh(dT_0)}{d\gamma e^{-dT_0} - c^2 \beta \sinh(dT_0)}$$

$$v_1 = -\frac{\xi}{2} \left[ \frac{b\eta x_0}{b\eta e^{bt_0} - a^2 \xi \sinh(bt_0)} \right]^2 \left[ -1 + \frac{a^2 \xi}{2b\eta} (1 - e^{-2bt_0}) \right]$$

$$v_2 = -\frac{\beta}{2} \left[ \frac{d\gamma y_0}{d\gamma e^{dT_0} - c^2 \beta \sinh(dT_0)} \right]^2 \left[ -1 + \frac{c^2 \beta}{2d\gamma} (1 - e^{-2dT_0}) \right]$$

During the DDoS attacks, the Defender considers the number of Bots controlled by the Attacker, at the same time, The Defender configures resources by the speed of worm propagation for the best profit.

#### 4 Performance evaluation and comparison

For evaluating our system, we analyze Net-Worm.Win32.Dasher as an example for DDoS attacks. We simulate China Education and Research Network, CERNET. In our model, the smallest network cell is a campus network, and the whole network model comprised by 500 campus networks. For each spread, we examined the impact on the

networks. From figure 1, we can see, at the start of each outbreak, the number of Bots, using the DGM is a little more, but in the long run, the total Bots are much less, as compared to other methods. In the

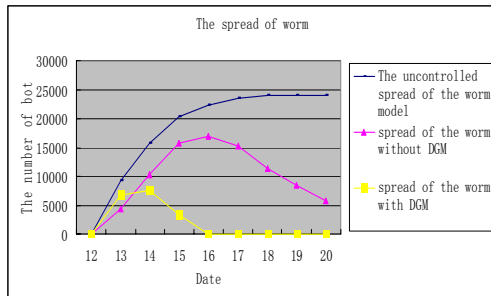


Figure 1. Bots in different models-

every beginning, DGM impacts network more than other models, but in a long-term, it is better than normal strategy (Figure 2).

Our experiments show that our DGM is a useful way to fight off worm infections and control the Botnet. The DGM results in a lower load on the network.

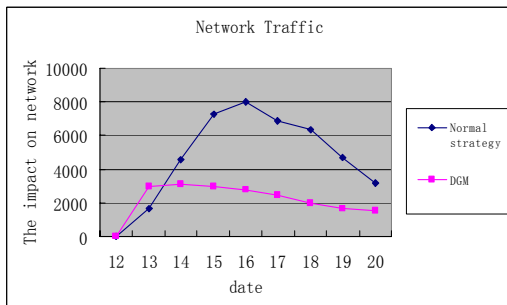


Figure 2. Infection to network

## 5 Conclusions

This paper discusses and implements the use of the Differential Game Model (DGM) to compete with an Attacker.

Our mechanism is characteristically distinct from current methods in the following ways:

(1) It utilizes few resources and does not require participation from all ISP routers, while saving the high burden of DDoS firewalls.

(2) The method is cost-effective, while resulting in a high performance. Furthermore, it is easy to deploy.

(3) The impact of the model on the network is only minor, while the survival of the server during a DDoS attack is greatly improved.

Our future work will focus on other issues in our DGM implementation. One challenging issue for us is to reduce a large number of Bots controlled by Botnet.

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