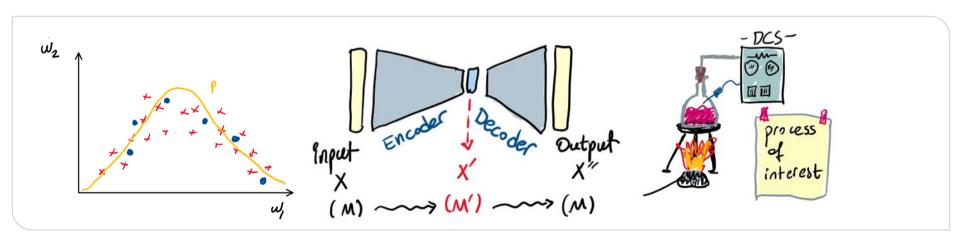




#### Data Driven Engineering I: Machine Learning for Dynamical Systems

### Introduction to Generative Learning: Autoencoders

Institute of Thermal Turbomachinery Prof. Dr.-Ing. Hans-Jörg Bauer







- \* Supervised learning \_\_\_\_\_ Classification Regression
- # Ursupervised learning > Clustering > Dim. Reduction
  - + Deep Learning + Time Series
    Analysis



- \* Supervised learning
- [x] { Learn a function to map  $[x] \rightarrow y$  } Discriminative models,

Unsupervised learning  $\Rightarrow$  Feature  $\Rightarrow$  Extraction  $\Rightarrow$  Extraction  $\Rightarrow$  Extraction  $\Rightarrow$  Promising  $\Leftarrow$  [X]  $\Rightarrow$  Promising  $\Rightarrow$  available,





## UL -> Generative Models:



- \* model tells how [X] is formed at the beginning
- \* It is probabilistic in nature

  - \* StyleGAN

    \* GPT language model

    \* Vertual training (RL)





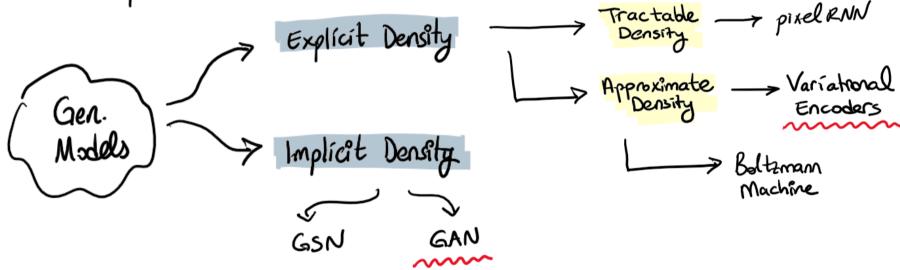




## UL -> Generative Models:



\* It is probabilistic in nature



# How does it work?

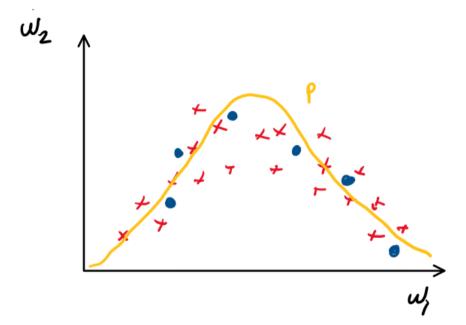


ø we have a dataset X.

we assume that it is generated according to a rule p

Model minics p to create new points.

Model should not reproduce what it has seen.



# How does it work?



- ① Sample space: Values an observation can take x = [....]
- 2 Probability Density Function: function maps X in sample space; PDF = [0, 1] it is well-defined  $\implies$  SPDF = 1-0
- 3 Parametric Modeling:  $p_{\theta}(\theta_{1},\theta_{2},\theta_{3}) \longrightarrow true p$   $fend(\theta_{i}) \Longrightarrow \text{maximum likelihood estimation},$

# How does it work?

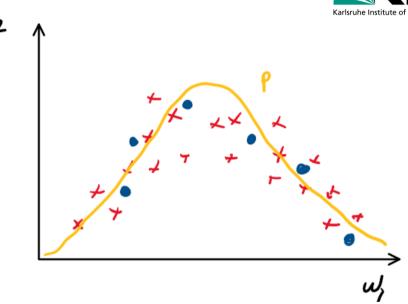
 $\mathcal{D}$  we have a dataset X.

we assume that it is generated according to a rule p

Model minics p to create new points.

Model should not reproduce what it has seen.





how can we infer the rules (po) from data?

Representation Learning



## Representation Learning



[X] 
$$\Longrightarrow$$
 [X'] } latest space  $\Longrightarrow$  learn  $\rho_{\theta} \Rightarrow$  learn  $\rho_{\theta} \Rightarrow$  learn  $\rho_{\theta} \Rightarrow$ 

## Representation Learning



[X] 
$$\Longrightarrow$$
 [X'] } latest space  $\Longrightarrow$  learn  $\rho_0 \Longrightarrow$  learn  $\rho_0$  igh dPm. (M) low dPm. space (M')



69/

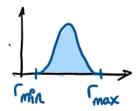
$$\mathcal{H}_0 = 'electe,$$

$$\mathcal{H}_1 = (lo, li, le, ... ln)$$

Perception in chess, 1973



$$[x] \rightarrow \emptyset \langle$$



# Autoencoders:



- \* unsupervised approch
- Hower dim representation (higher?)
- Input Encoder Output

  X

  (M)

  (M)

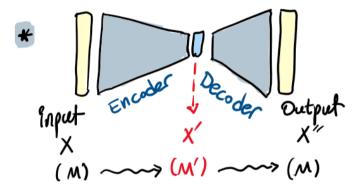
  (M)

D Reconstructed X"

- 0 By-product ⇒ X'
- Cost :  $\|x'' x\|^2$  function

# Autoencoders:





- \* Use cases:
- I Dimensionality Reduction
- ver Anomaly detection

- \* Use cases:
- I Forecasting ~ generalive
- I Sparse Representation
- Denoising dataset
- D"Interpolator,
- D Unsupervised pre-training
- D' "Generative Model, (+ pdf)

## Karlsruhe Institute of Technology

## Base model: Under-complete linear AE

- \* MLP -> Ilnear activation function

  L-> cost := MSE
  - S ≈ PCA
- \* Symmetrical

  M M' M layer (s)

- Many layers => Deep Antoenco der
- \* Good for large [X] with high M.
- \* can be used for outlier detection



#### Today's Agenda



### Basic Steps to Follow =

- o.) Understand the business/task-
- 1.) Understand the data.
- 2.) Explore & prepare the data.
- 3.) Shortlist candidate models.
- 4.) Training the model

  5.) Evaluate the model predictions
- 6.) "Serve, the model ?

#### **#0 Understanding the task**



- □ Problem: Manufacturing error in a production line
- Modified sensory input: 28 variables including sensory input
- □ 280,000 instances, where only a small fraction (~500) of products are defective.
- ☐ **Heuristic**: <0.5% is defective



#### A similar example for you:

"Bosch Production Line Performance Reduce manufacturing failures"



#### #1 Understanding the data



- ☐ Check the data source: understand what the data refers to
- □ Objective: understand the characteristics of the data
- □ Look at the feature columns:
  - Any missing values?
  - Any features with NaN values?
  - Uniqueness of the dataset? ("cardinality")



26.01.2021

23	S23	284807	non-null	float64				
24	S24	284807	non-null	float64				
25	S25	284807	non-null	float64				
26	S26	284807	non-null	float64				
27	S27	284807	non-null	float64				
28	S28	284807	non-nul	float64				
29	Class	284807	non-nul <mark>l</mark>	object				
dtypes: float64(29), object (1)								

memory usage: 65.2+ MB

time: 54.5 ms

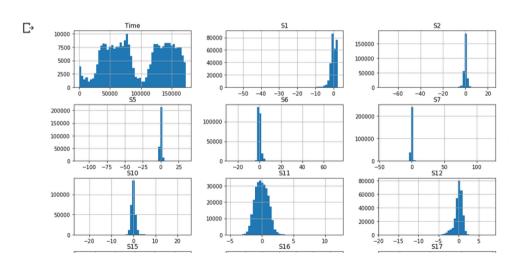
n →		Time	S1	S2	s3	S4	S5	S6	
	count	284807.000000	2.848070e+05	2.848070e+05	2.848070e+05	2.848070e+05	2.848070e+05	2.848070e+05	
	mean	94813.859575	1.758743e-12	-8.252298e-13	-9.636929e-13	8.316157e-13	1.591952e-13	4.247354e-13	
	std	47488.145955	1.958696e+00	1.651309e+00	1.516255e+00	1.415869e+00	1.380247e+00	1.332271e+00	
	min	0.000000	-5.640751e+01	-7.271573e+01	-4.832559e+01	-5.683171e+00	-1.137433e+02	-2.616051e+01	
	25%	54201.500000	-9.203734e-01	-5.985499e-01	-8.903648e-01	-8.486401e-01	-6.915971e-01	-7.682956e-01	
	50%	84692.000000	1.810880e-02	6.548556e-02	1.798463e-01	-1.984653e-02	-5.433583e-02	-2.741871e-01	
	75%	139320.500000	1.315642e+00	8.037239e-01	1.027196e+00	7.433413e-01	6.119264e-01	3.985649e-01	
	max	172792.000000	2.454930e+00	2.205773e+01	9.382558e+00	1.687534e+01	3.480167e+01	7.330163e+01	
	time:	447 ms							



#### #2 Exploring the data



- □ Objective: generate a data quality report
- ☐ Using standard statistical measures of central tendency and variation
  - □ tabular data and visual plots
  - ☐ mean, mode, and median
  - standard deviation and percentiles
  - □ bars, histograms, box and violin plots
- ✓ Missing values,
- ✓ Irregular cardinality problems,
  - 1 or comparably small
- ✓ Outliers
  - invalid outliers and valid outliers





#### #2 Exporing the data: Correlation Matrix



☐ Shows the correlation between each pair of features

$$Cov(a,b) = \frac{1}{n-1} \sum_{i=1}^{n} \left[ (a_i - \overline{a}) \times (b_i - \overline{b}) \right]$$
Features

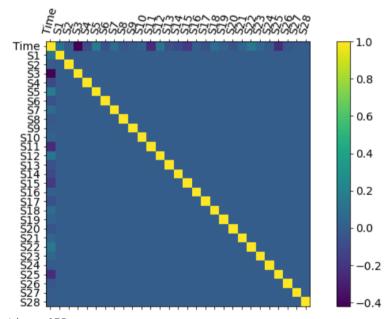
Features

Mean

mean

□ Normalized form of "covariance"

□Ranges between -1 and +1



time: 975 ms



#### **#2 Preparing the Data**



□ Clustering >> unsupervised >> training & test split not needed

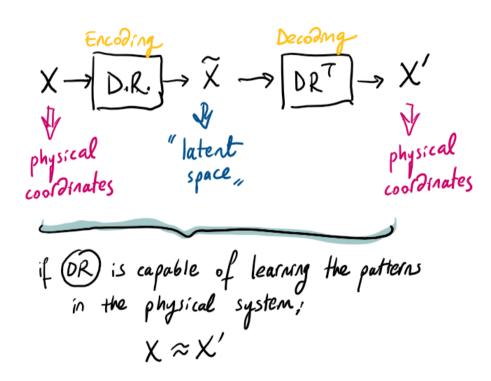


☐ We will use it to **reduce the volume of the data** when needed:



#### #5 Evaluating the Results: Reconstruction error





\* loss = 
$$\sum_{m=1}^{M} (\chi - \chi')^2 \Rightarrow N$$
elements

Normalization:

\* loss' =  $\frac{loss - min(loss)}{max(loss) - min(loss)} \Rightarrow [0, 1]$ 

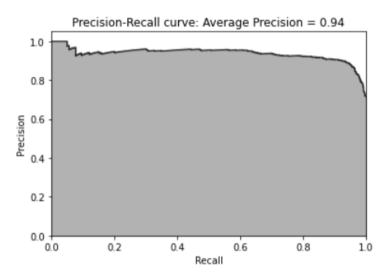
Interpretation:

\* loss' > 0 > Regular Product
loss' > 1 > Anomaly, defective

#### **#5 Evaluation of the predictions**



#### **Precision Recall Curve (for imbalanced data)**



- Precision captures how often, when a model makes a positive prediction, this prediction turns out to be correct.
- Recall tells us how confident we can be that all the instances with the positive target level have been found by the model.





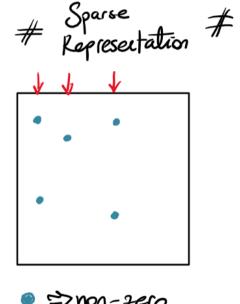
# colab



## Sparse Autoencoders:

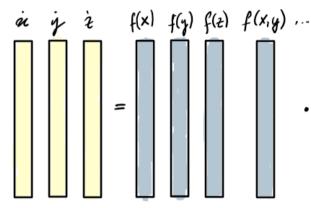


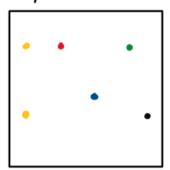
\* Sparse matrices



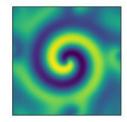
#### Data Driver Model Discovery.



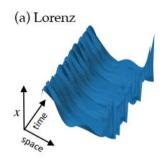




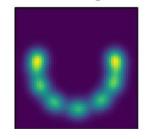
 $\dot{z}_1 = -10.0z_1 + 10.0z_2$  $\dot{z}_2 = 27.7z_1 - 0.9z_2 - 5.5z_1z_3$  $\dot{z}_3 = -2.7z_3 + 5.5z_1z_2$ 



$$\dot{z}_1 = -0.85z_2$$
  
$$\dot{z}_2 = 0.97z_1$$



#### (c) Nonlinear pendulum



$$\ddot{z} = -0.99 \sin z$$

$$\begin{aligned}
\dot{n} &= ax - bxy^2 + \beta_i \\
\dot{y} &= cy^2 + \beta_i \\
\text{Linear} \quad \dot{\epsilon} &= axy + \sin\beta_i \\
\text{Regions.}
\end{aligned}$$

## Sparse Autoencoders:



- Modify the cost function to enforce sparse "neurons,.

  - Ly ly regularization

    Sigmoid activation functions
  - → Large encoders

simpler tools

(1) have a target sparsity. (ii) measure actual sparsity

(iii) Give penalty

Check average neuron activity in batch.

[KL Divergence]

Add sparsity loss to total loss.







# colab

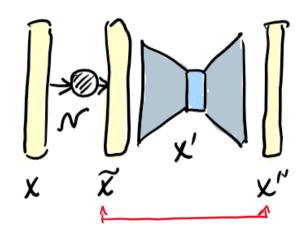


### De-noising your Data:



- D PIV Measurements
- □ Simulation data => FTLE -

O " Clean data , is needed.



Obj: Lean to clean the data from noise.



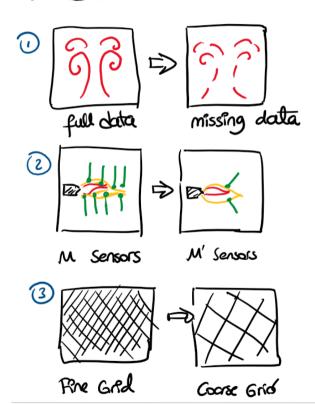


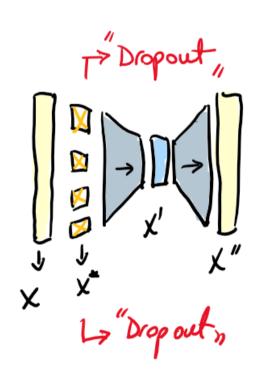
# colab



### Interpolation Tool2









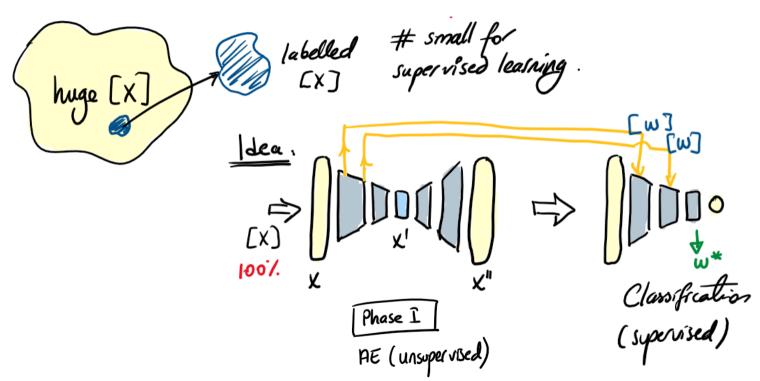


# colab





## Unsupervised Pretraining







# colab





#### **Additional Notes**





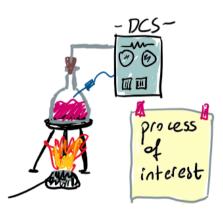
Dim. Reduction:

Computational —preprocessing — Feature Extraction

~ pattern recognition~

Visualization

Idea:

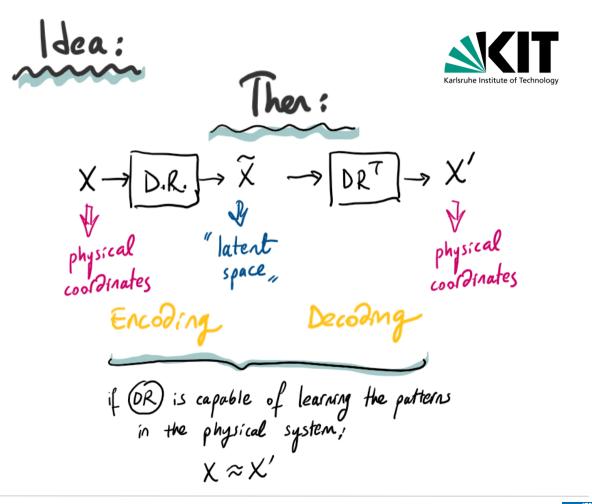


Institute of Thermal Turbomachinery (ITS)



• 
$$product = \sum_{i=1}^{n} process_i$$

· Features m is correlated to K steps in the production line;



# Idea:



# Interpretting Patherns



- Physical system is composed of logical steps;
- Logical steps => "Regular product,
- \* Failure at some > Defect "

(A.I.

"Outlier Detection, Something is wrong here.,

APM > Learn enough to detect outliers;